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**CUSTOM ORTHODONTIC APPLIANCE
FORMING METHOD AND APPARATUS**

The present invention relates to the design, manufacture and use of orthodontic appliances for the straightening of teeth, and more particularly, to the automated design, manufacture and use of custom orthodontic appliances based on individual patient anatomy and to the diagnosis of patients therefor and the treatment of patients therewith.

Background of the Invention:

The orthodontic treatment of patients has as its fundamental objective the repositioning or realignment of the teeth of a patient in the patient's mouth to positions where they function optimally together and occupy relative locations and orientations that define a pair of opposed and cooperating planar, or nearly planar, smooth arches. The teeth of the two arches, the maxillary arch of the teeth of the upper jaw and the mandibular arch of the teeth of the lower jaw, when in an optimal or ideal position, contact the teeth of the opposite arch along a surface that is usually flat or slightly upwardly concave and commonly referred to as the plane of occlusion.

The treatment applied to patients who have been diagnosed as having teeth insufficiently close to the ideal positions to require orthodontic correction includes an initial or rough procedure to overcome the more serious defects of tooth positioning followed by a finish treatment designed to bring the teeth as closely as possible or practical to their ideal positions. The rough treatment usually involves the movement of certain teeth through the use of any of a number of recognized techniques performed by an orthodontist, and sometimes procedures such as the extraction of certain teeth or surgery on the patient's jaw performed by an oral surgeon.

In the finish treatment, the orthodontist applies an appliance, or set of braces, to the teeth of the patient to exert continual forces on the teeth of the patient to gradually urge them toward their ideal positions. The application of the appliance usually involves the attachment of brackets to the teeth, either with the application of adhesive to the teeth or the securing of bands around the teeth. The brackets are usually each provided with a slot through which an archwire is extended. One archwire is provided for the upper teeth and one for the lower teeth. Typically, the slots in the brackets are of rectangular cross-section and the archwire is of rectangular cross-section. The archwire installed in the slots of the brackets interconnects the teeth, through the brackets, and exerts forces on the teeth to translate or rotate them toward a finish position envisioned by the orthodontist.

It has been recognized in the design and application of orthodontic appliances that an ideally designed and installed orthodontic appliance will present the slots of the brackets in a position to initially receive a preshaped archwire that will elastically deform to exert corrective forces on the teeth to urge them toward their finish positions. When in their finish positions, the archwire of the ideally designed appliance will no longer be elastically deformed, and will no longer exert forces upon the teeth. Achieving this objective has been inhibited by certain problems in the prior art.

One problem presented by the prior art is that current orthodontic products are designed and manufactured to average anatomy. As a result, orthodontists are faced with the need to select what they perceive to be the brackets and archwires of the closest design to those required by a particular patient, and to modify the designs for treatment of the patient. Some of this modification may be performed when the appliance is initially installed, but almost inevitably modification is required during the course of treatment of the patient. This modification may take the form of the replacement of brackets, but most commonly requires a periodic bending and reshaping of the archwire as the treatment progresses. Thus, the treatment of the patient has become a manual feedback system in which the orthodontist monitors the progress of the patient's treatment and then readjusts the appliance, usually by bending the archwires, to correct the forces being applied to the teeth to bring the teeth to their ultimate positions, which are less than ideal. As a result, the patient may be subjected to treatment over a period that is longer than would be necessary if the appliance were initially made to the optimum design. In addition, the time required of the orthodontist for implementation of the treatment may be several times greater than it would be if modification of the appliance were unnecessary. Thus, the orthodontist is able to treat fewer patients and the cost of the treatment to the patient or to the orthodontist is increased.

Location of the connection points for the appliance to the teeth also presents a problem in the prior art. Typically, brackets are bonded to the teeth and then interconnected by the installation of the archwires. This is done when the teeth are in their maloccluded positions, with the orthodontist having only a mental vision of where the finish positions of the teeth will be and where the brackets are to be placed to move the teeth to those finish positions. For more effective use of the appliance and to promote ease in cleaning the teeth, the orthodontist prefers to locate the brackets and archwires away from the gums. If they are placed too close to the tips of the teeth, however, they may interfere with the teeth of the opposite arch as the teeth approach their finish positions.

Another problem of the prior art that has inhibited the selection or design of an ideal orthodontic appliance for the patient is the difficulty in arriving at an expression of the ideal finish position of the teeth. Orthodontists typically make models of the patient's mouth and, with the models and the aid of x-rays, determine a treatment to move the teeth to finish tooth positions. This process is time consuming and presents a source of error and inaccuracy. From the measurements and based on the judgment of the orthodontist, appliance components are selected to implement the prescribed treatment. In reality, the treatment of patients is in many cases more of an art than a science, with results ranging from poor to excellent, and generally variable.

The need for custom manufactured orthodontic appliances and the use of automatic design techniques has been recognized by some, while others have advocated adherence to standard components and manual techniques in view of a perceived lack of practical custom appliance manufacturing and automated appliance design systems of the art.

The development of automated custom appliance design systems has encountered several difficulties. These difficulties have included the task of developing an automated system that includes reliable and efficient

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decision making algorithms and techniques for automatically determining an ideal finish position of the teeth. Further, these difficulties have included arriving at an expression of appliance geometry in terms that can be efficiently produced by automated appliance manufacturing equipment. Furthermore, the prior art has not provided a way to accurately manufacture an appliance on an individualized basis in accordance with the appliance design. An additional problem in the automated design and manufacture of orthodontic appliances lies in the difficulty in designing the custom design system to take into account the professionally recognized parameters and criteria, derived over many years from the knowledge and experience of the practicing and clinical orthodontist, upon which diagnosis and treatment is based.

Accordingly, there is a great need in orthodontics for a practical, reliable and efficient custom appliance automated design and manufacturing system, and method of providing custom appliances and treating patients therewith.

Summary of the Invention:

A primary objective of the present invention is to provide a practical, reliable and efficient custom appliance automated design and manufacturing system and methods of automatically designing custom orthodontic appliances and treating patients therewith.

It is a particular objective of the present invention to provide an automated custom orthodontic appliance design and manufacturing system that can be easily and reliably used by practicing orthodontists and that will make best use of the skills, knowledge and experience that the orthodontist possesses. It is a further objective of the present invention to increase the accuracy of the orthodontist's treatment, to render the use of the orthodontist's time more efficient, to eliminate sources of error and guesswork from the orthodontist's treatment of patients, and to efficiently, repeatedly and reliably perform automatically the many of the routine steps in the diagnosis, prescription and implementation of orthodontic treatment and in the design and manufacture of orthodontic appliances.

It is a further objective of the present invention to improve the practice of orthodontics by aiding the practitioner in achieving optimal finish treatment of patients and in more accurately determining and precisely achieving the finish placement of a patient's teeth. An additional objective of the present invention is to provide for the accumulation of data from individual patients for the analysis of the data to advance the orthodontic art.

It is still another objective of the present invention to apportion the tasks involved in the design and manufacture of custom appliances most efficiently between orthodontist and appliance manufacturing facility in accordance with the scale and other particulars of the individual practitioner operation.

According to the principles of the present invention, a system and method are provided which depart from traditional design and manufacture by designing orthodontic appliances around the anatomy of the individual patient. Further, unlike current orthodontic products that are designed and manufactured to average anatomy, the orthodontic products of the present invention and the methods of manufacturing and using them are tailored to the individual anatomy of the patient.

In accordance with the preferred embodiment of the present invention, there is provided a computerized system and method with which finish positions of the teeth of a patient are derived from digitized information of anatomical shapes of the patient's mouth, an orthodontic appliance is automatically designed from the digitized shape information and the derived tooth finish positions, machine code is

generated for production of the orthodontic appliance and communicated to NC machines, and the appliance is automatically fabricated with the machines in response to the machine code.

In accordance with the preferred and illustrated embodiment of the invention, the digitized information is generated from measurements from the mouth of the patient, either taken directly or from a model thereof, and preferably includes information of the shapes of the individual teeth of the patient and of the patient's lower jaw.

In the preferred embodiment, the finish tooth position derivation includes the derivation of one or more archforms, preferably conforming to a skeletal archform defined by the shape of the lower jaw. The appliance is also configured in accordance with the shape of the derived archform, preferably with a mandibular skeletal archform having size and shape conforming to that of the trough of the lower jaw. In the preferred embodiments, additional archforms are constructed using information of the shapes of the individual teeth and the lower jaw skeletal archform to define the positions of the buccal cusps and incisal tips of the mandibular teeth, the marginal ridges of the upper posterior teeth, and the lingual points of occlusion of the upper anterior teeth to position the teeth according to a preferred treatment plan.

In certain preferred embodiments of the invention, the digitized data is taken by measurements of the patient's individual teeth and the data is reduced to certain landmark data that becomes key to effective and efficient arrival at highly preferred finish tooth positions. The individual teeth are arranged on the various derived archforms with mesial and distal contact points of adjacent teeth in contact. The spacing between the opposite contact points of each tooth are preferably extracted from a computerized image formed in horizontal plan views of the patients teeth. Furthermore, relative locations of the incisal tips, marginal ridges, gingival contact points and the external surfaces of the teeth to which the appliance connects, for example, by the mounting of brackets, and which occlude with teeth of the opposite jaw, are determined by digitizing vertical profiles of the surfaces of the crowns of the teeth. This data is reduced to define contact points of the mandibular teeth with the lower jaw, such as the gingival center points, to define crown axes of the teeth, and other parameters that are amenable to manipulation with a simple and reliable algorithm in calculating the finish positions of the teeth. The landmarks also include intercuspal and inter ridge spacing measurements that provide a basis for prescribing arch expansion treatment with exactness based on the computer aided calculation of precise finish tooth positions. Further, the tooth position calculations provided improve upon prior orthodontic practice by preserving crown long axis inclination angles and setting the teeth to preferred crown long axis inclination angles for population groups according to seed values that are statistically improved upon by the present invention.

In certain embodiments of the invention, images are digitized to produce the tooth and jaw shape data. Preferably, the images include a scanner which, in one form, generates a video image from which selected points are digitized to produce data from which finish tooth positioning and appliance design is carried out. Alternatively, three dimensional imaging of the teeth and jaw of the patient is carried out with laser or other scanner to form full three dimensional images of the teeth and jaw of the patient. The images may be formed from the patient's teeth and jaw or from a model thereof. Additional data is digitized by taking vertical profiles of the patient's teeth, either by tracing with a computer the three dimensional images generated with other scanners, or by scanning with a mechanical contact probe or with a non-contact probe the individual teeth of the patient, or model thereof. The data may be taken directly from the patient using CAT scans, MRI, positron emission tomography or other technique.

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Also in accordance with certain embodiments of the invention, the finish tooth positioning includes the establishment of cuspid rise criteria by rigorous calculations made from measured and statistical anatomical data so that the height of the cuspids and other teeth can be adjusted relative to each other so that the teeth can be positioned to guide the jaws into proper occlusion. With the present invention, numerical relationships are provided for cuspid rise that are an improvement of the prior art.

In accordance with certain preferred embodiments of the invention, an archwire forming machine that is responsive to NC code is driven by signals generated by a computer that reads input data of anatomical shapes of the patient's mouth, is provided to automatically form an arcuate appliance that interconnects the teeth to move them toward their finish positions by rotational and translational forces applied in three dimensions each by the arcuate appliance. Generally, the arcuate appliance is an archwire, and the machine for forming the appliance includes an archwire forming machine that is responsive to NC code is driven by signals generated by a computer that reads input data of anatomical shape of the patient's mouth, preferably of the patient's jaw and teeth, derives the tooth finish positions and archwire and bracket designs that will move the teeth to the calculated finish positions, and generates the machine code to produce the archwire in accordance with the design. Preferably, the archwires have shapes that conform to archforms related to the finish tooth positions, particularly to the shape of the patient's lower jaw, and is represented as a series of segments of a continuous archwire that each have a constant radius of curvature over the length of the segment, and that preferably join adjacent segments in a smooth transition, with the segments tangent where they join.

Further in accordance with certain preferred embodiments of the invention, a bracket fabrication machine, also responsive to NC code, is driven by similar signals from a computer responsive to computer generated finish tooth position calculations and digitized tooth shape data. Preferably, the brackets have bases that mount on computer determined positions on the teeth and have slots to receive archwires that are inclined at computer determined angles. The fabrication of the brackets may include the formation of a slope and/or curvature to the mounting surfaces of the bases of the brackets, or, as with the illustrated embodiment, by cutting custom slots in the brackets. In the preferred embodiment, the design and manufacture of the archwires and brackets are interrelated so that the curve of the archwire is optimized to minimize curvature changes and the brackets are optimized to minimize their profiles, or the distances from the bases to the archwire slots. The calculations provide a basis for the selection of appropriate bracket blanks for the optimized appliance design.

Additionally, in accordance with other aspects of the invention, one or more placement fixtures are manufactured from the input data and the calculated tooth positions for locating points on the teeth, preferably determined by the computer, for the connection of the appliance to the teeth, such as for the mounting of the brackets to the teeth. The fixtures preferably include a set of bracket placement jigs, one for each bracket that is to be mounted on a tooth, to position and hold the bracket to the tooth so that it can be secured thereto in a precise mounting location. The jigs of the preferred embodiment include a tooth profile or three dimensional surface that fits against the tooth to precisely locate the jig on the tooth and hold a bracket at a precise position and inclination thereon so that it can be secured to the tooth with adhesive.

With the present invention, a custom orthodontic appliance is fabricated under the control of a computer directly from data taken from the teeth and/or jaw of a patient or a model thereof. The appliance so formed, when connected to the teeth of the patient, moves the teeth of the patient to precise calculated

finish positions without the need for the orthodontist to bend archwires over the course of the treatment. As a result, the orthodontist's time is conserved, the treatment of the patient is achieved in a shorter amount of time and the finish positions of the teeth are more nearly ideal, and consistently so, than those achieved with the procedures of the prior art. Furthermore, the appliance fabricating processes result in the generation of data useful in establishing treatment techniques and criteria that will improve the practice of orthodontics.

Further, movement of the teeth to the finish positions calculated in accordance with the present invention results in far more stable placement of the teeth than with other methods of the prior art which often experience movement of the teeth to inferior positions after the orthodontic treatment is terminated.

These and other objectives and advantages of the present invention will be more readily apparent from the following detailed description of the drawings in which:

Brief Description of the Drawings:

Figs. 1-1F are diagrams illustrating the preferred embodiments of the system of the present invention, of which:

Fig. 1 is a block diagram illustrating one preferred embodiment of an automated system for the design and manufacture of custom orthodontic appliances for the treatment of patients therewith according to the principles of the present invention.

Fig. 1A is an elevational diagram of a video graphics image forming embodiment of the data input portion of one embodiment of the scanner of the system of Fig. 1.

Fig. 1B is an elevational diagram of a laser scanner version of a three dimensional graphics imaging embodiment of a scanner of the system of Fig. 1.

Fig. 1C is an elevational diagram of a mechanical tooth profile probe scanner version of a two dimensional imaging portion of one embodiment of the scanner of the system of Fig. 1.

Fig. 1D is an isometric diagram of one embodiment of a bracket cutting device of the system of Fig. 1.

Fig. 1E is an isometric diagram of one embodiment of a wire forming device of the system of Fig. 1.

Fig. 1F is an isometric diagram of a bracket placement jig forming device of the system of Fig. 1.

Figs. 2-2Z are flow chart diagrams of the preferred methods of carrying out the present invention, of which:

Fig. 2 is a flow chart of one preferred embodiment of the process of the present invention performed with the system of Fig. 1.

Fig. 2A is a more specific flow chart illustrating the steps of the input procedure of automated tooth positioning and appliance design and manufacturing operation of the process of Fig. 2.

Fig. 2B is a more specific flow chart illustrating the steps of the analysis and tooth finish position calculating procedure of the automated tooth positioning and appliance design and manufacturing operation of the process of Fig. 2.

Fig. 2C is a more specific flow chart illustrating the steps of the custom appliance design procedure of the automated appliance design and manufacturing operation of the process of Fig. 2.

Fig. 2D is a more specific flow chart illustrating the steps of the custom appliance manufacturing procedure of the automated tooth positioning and appliance design and manufacturing operation of the process of Fig. 2.

Fig. 2E is a detailed flow chart illustrating the substeps of the identification data input step of the input procedure of Fig. 2A.

Fig. 2F is a detailed flow chart illustrating the substeps of the patient history and treatment data input step of the input procedure of Fig. 2A.

5 Fig. 2G is a detailed flow chart illustrating the substeps of the mandibular bone and horizontal tooth dimension data input step of the input procedure of Fig. 2A.

Fig. 2H is a detailed flow chart illustrating the substeps of the maxillary horizontal tooth dimension data input step of the input procedure of Fig. 2A.

10 Fig. 2I is a detailed flow chart illustrating the substeps of the individual tooth vertical profile data input step of the input procedure of Fig. 2A.

Fig. 2J is a detailed flow chart illustrating the substeps of the individual tooth profile analysis and landmark identification step of the analysis procedure of Fig. 2B.

Fig. 2K is a detailed flow chart illustrating the substeps of the cuspid rise calculation step of the analysis procedure of Fig. 2B.

15 Fig. 2L is a detailed flow chart illustrating the substeps of the mandibular preliminary horizontal tooth finish position calculation step of the analysis procedure of Fig. 2B.

Fig. 2M is a detailed flow chart illustrating the substeps of the best fit mandibular cusp arch equation calculation step of the analysis procedure of Fig. 2B.

20 Fig. 2N is a detailed flow chart illustrating the substeps of the calculation step of the mandibular tooth finish position on the best fit mandibular cusp arch equation of the analysis procedure of Fig. 2B.

Fig. 2O is a detailed flow chart illustrating the substeps of the maxillary horizontal tooth finish position calculation step of the analysis procedure of Fig. 2B.

Fig. 2P is a detailed flow chart illustrating the substeps of the mandibular archwire plane calculation step of the appliance design procedure of Fig. 2C.

25 Fig. 2Q is a detailed flow chart illustrating the substeps of the mandibular bracket slot inclination calculation step of the appliance design procedure of Fig. 2C.

Fig. 2R is a detailed flow chart illustrating the substeps of the maxillary archwire plane calculation step of the appliance design procedure of Fig. 2C.

30 Fig. 2S is a detailed flow chart illustrating the substeps of the maxillary bracket slot inclination calculation step of the appliance design procedure of Fig. 2C.

Fig. 2T is a detailed flow chart illustrating the substeps of the mandibular archwire and bracket slot in-out dimension calculation step of the appliance design procedure of Fig. 2C.

Fig. 2U is a detailed flow chart illustrating the substeps of the maxillary archwire and bracket slot in-out dimension calculation step of the appliance design procedure of Fig. 2C.

35 Fig. 2V is a detailed flow chart summarizing the substeps of the bracket placement jig shape calculation step of the appliance design procedure of Fig. 2C that is illustrated in more detail in the flowchart of the jig modification step of Fig. 2Z described below.

40 Fig. 2W is a detailed flow chart illustrating the substeps of the cubic spline curve fitting, spline to circle conversion and tooth placement calculation subroutines employed in placing teeth on calculated archforms in certain steps of the tooth positioning and appliance design and manufacturing operation of Fig. 2C.

Fig. 2X is a detailed flow charts illustrating the NC code generation and slot cutting substeps of the bracket manufacturing step of the procedure of Fig. 2D, and Figs. 2X-1 through 2X-4 are more detailed flowcharts illustrating substeps of Fig. 2X.

Fig. 2Y is a detailed flow chart of the substeps of the wire bending code generation and wire manufacturing step of the appliance manufacturing procedure of Fig. 2D.

Fig. 2Z is a detailed flow chart illustrating the substeps of the jig manufacturing step of the appliance manufacturing procedure of Fig. 2D. Figs. 2Z-1 through 2Z-6 are more detailed flowcharts illustrating details of substeps of Fig. 2Z.

Figs. 3-3C are illustrations of graphics computer images produced in the input procedure, in which:

Fig. 3 is an example of a computer display of a video image generated by the scanner of the system of Fig. 1 illustrating in a top plan view a mandibular model produced by the scanner of the type shown in Fig. 1A.

Fig. 3A is an example of a portion of a three dimensional digital image, illustrated in perspective, and produced by the scanner of the type shown in Fig. 1B.

Fig. 3B is an illustration similar to Fig. 3A of another portion of a three dimensional digital image produced by the scanner of Fig. 1B.

Fig. 3C is an example of a set of vertical tooth profile images produced by the scanner of Fig. 1C.

Figs. 4-4E are plan views of the teeth of the patient on tooth placement archforms at various stages of the tooth position calculation procedure of Fig. 2B, of which:

Fig. 4 is a geometric diagram illustrating a horizontal plan view data input screen showing diagrammatically the video image of Fig. 3 used as a template, with variables relevant to the digitization of data from the mandibular video image marked thereon.

Fig. 4A is a geometric diagram similar to Fig. 4 for the maxillary teeth.

Fig. 4B is a geometric diagram plotting horizontal mandibular archforms calculated through the analysis procedure of Fig. 2B.

Fig. 4C is a geometric diagram plotting horizontal maxillary archforms calculated through the analysis procedure of Fig. 2B.

Fig. 4D is a horizontal plan diagram showing the maxillary teeth in their finish positions.

Fig. 4E is a horizontal plan diagram showing the mandibular teeth in their finish positions and with the custom appliance in place.

Figs. 5-5P are mathematical calculation diagrams for reference in connection with spline to circle conversion and tooth placement routines of Fig. 2W, in which:

Fig. 5 is a horizontal plan diagram illustrating the placement of a tooth on an archform equation described in circle segment form.

Figs. 5A-5J are detailed diagrams of the spline to circle conversion and tooth placement subroutines.

Figs. 5K-5P are detailed diagrams of the tooth placement subroutine.

Figs. 6-6I are diagrams of tooth profiles illustrating landmark determination, tooth inclination and vertical positioning, in which:

Fig. 6 is an isometric image of a three-dimensional computerized representation, similar to Fig. 2B, of a molar showing the locations of alternative vertical labial-lingual profile planes and tooth profiles.

Fig. 6A is a mathematical tooth profile plot as illustrated on the computer screen of a the system of Fig. 1 of a mandibular molar showing selected landmark parameters.

Fig. 6B is a mathematical tooth profile plot, similar to Fig. 6A, of a mandibular cuspid or incisor showing selected landmark parameters.

5 Fig. 6C is a mathematical tooth profile plot, similar to Fig. 6A, of a maxillary molar or bicuspid showing selected landmark parameters.

Fig. 6D is a mathematical tooth profile plot, similar to Fig. 6A, of a maxillary cuspid or incisor showing selected landmark parameters relevant thereto.

10 Fig. 6E is representation of a display, similar to Fig. 3C, of an array of mathematical tooth profile plots of all of the teeth, angularly oriented, with landmark parameters marked thereon.

Fig. 6F is representation of a display of an array of mathematical tooth profile plots, similar to a portion of Fig. 6E, of the mandibular teeth with working horizontal placement planes marked thereon.

Fig. 6G is mathematical tooth profile plot, similar to Fig. 6A, of a mandibular posterior tooth with relevant dimensional variables for placement of the tooth marked thereon.

15 Fig. 6H is mathematical tooth profile plot, similar to Fig. 6B, of a mandibular anterior tooth with relevant dimensional variables for the placement of the tooth marked thereon.

Fig. 6I is mathematical tooth profile plot, similar to Fig. 6H, of a the tallest mandibular tooth.

Figs. 7-7D are diagrams for reference in connection with the finish tooth position calculation, of which:

20 Fig. 7 is an elevational diagram of the relationship of the jaws of a patient for illustration of cuspid rise occlusion calculation.

Fig. 7A is an enlarged view of a portion of Fig. 7.

Fig. 7B is a plan mathematical diagram illustrating certain of the mathematics of tooth placement on the mandibular offset arch.

25 Fig. 7C is a perspective diagram illustrating the relationship of the vertical tooth profile planes and relevant horizontal arch planes in the course of tooth finish position calculation.

Fig. 7D is a set of related elevational profiles of mandibular and maxillary teeth showing occlusal and overlap relationships in the course of tooth finish position calculations.

30 Figs. 8-8H are diagrams for reference in connection with the steps of the custom appliance design procedure, of which:

Fig. 8 is a diagram similar to Fig. 7D illustrating archwire plane and bracket slot design on positioned teeth.

Fig. 8A is an elevational diagram illustrating a bracket and slot configuration in connection with the diagram of Fig. 8.

35 Fig. 8B is a top view illustrating the relation of a tooth to an archform by placement routine of Fig. 2W.

Fig. 8C is a tooth profile diagram illustrating the slot in-out dimension calculation.

Fig. 8D is a perspective diagram illustrating the placement of a custom bracket onto a tooth with the use of a custom placement jig.

40 Fig. 8E is a plan diagram of a custom archwire for the appliance required to move the mandibular teeth to the finish positions illustrated in Fig. 4E.

Fig. 8F is a plan diagram illustrating the labial installed appliance on the teeth of the patient in their initial positions.

Fig. 8G is a plan diagram, similar to Fig. 8F, illustrating a lingual appliance installed on the teeth of the patient.

5 Fig. 8H is an elevational diagram illustrating an orthodontic lingual bracket of the appliance of Fig. 8G.

Fig. 8I is a top view of a bracket having a base slot curvature conforming to that of an archwire supported therein.

Figs. 9-9W are diagrams relating to appliance manufacturing steps, of which:

10 Figs. 9-9H relate to substeps of the bracket slot cutting code generation and bracket manufacturing step.

Figs. 9I-9W relate to the substeps of the bracket placement jig manufacturing step.

Detailed Description of the Drawings:

15 The preferred embodiment of the invention provides a system and method for designing and manufacturing orthodontic appliances and for employing the appliances to orthodontically treat patients for the straightening of teeth. Unlike traditional orthodontic products, however, the appliances resulting from the practice of the present invention are designed around the anatomy of the individual patients. It further incorporates in its design criteria the parameters and professional treatment approaches of the treating orthodontists, and applies automated decision making processes in the appliance design that take into account

20 the professionally recognized characteristics and anatomical landmarks of the patients.

The overall configuration of the system 10 is illustrated diagrammatically in Fig. 1. The overall operations of the preferred method of the invention are illustrated in the flowchart of Fig. 2.

25 In accordance with the preferred embodiment of the invention as illustrated in Figs. 1 and 2, examination of a patient is performed by an orthodontist at the orthodontist's office for the purpose of assembling the information necessary to determine the patient's condition, prescribe the appropriate treatment, and specify the type of orthodontic appliance to implement the treatment. The information is then communicated to a remotely located appliance design and manufacturing facility where the design of a custom appliance for use in administering the treatment is carried out with the use of computer analysis. The appliance design, together with the information necessary for the orthodontist to install the appliance on the

30 patient is then transmitted back to the orthodontist, who installs the appliance and administers the treatment in accordance with the appliance manufactures instructions and his own professional expertise.

35 In accordance with alternative embodiments of the invention, digitization of anatomical information for computer input is performed either at the appliance design and manufacturing facility, by the orthodontist at his office, or preferably divided between the two. Similarly, the present invention contemplates the manufacture of the appliance to be performed at either the appliance manufacturing facility, at the orthodontists office, or preferably divided between the two locations and in accordance with the analysis and design provided by the system of the present invention.

40 The practice of the present invention involves the use of certain system hardware, tangible records of information, and communications paths described below in connection with Fig. 1 and related illustrations, and the performance of operations, procedures and steps described in connection with the flowchart of Fig. 2 and related diagrams, all as set forth in detail below.

Terminology and Conventions

Throughout the description, references are made to tangible elements illustrated in the drawings and to actions performed by hand and by computer. In the description, numbers used to refer to structure or other tangible items illustrated in the drawings of the preferred embodiment appear in conventional form in the text, while numbers that refer to method steps in the illustrated flowchart are enclosed in parentheses in the following description. Letter symbols are used to refer to geometric or mathematical representations of variables, parameters, dimensions and values, input into or calculated by a computer, tie into equations and diagrams illustrated in the drawings, or correspond to computer codes or conceptual items set forth in the disclosure.

Throughout this description, the various teeth of the patient, up to thirty-two in number, may be identified as $T_{J,S,I}$ or $T(J,S,I)$, where J designates the jaw (upper: $J = U$; lower: $J = B$), where S designates the side (patient's right: $S = R$; patient's left: $S = L$), and I designates the tooth by position relative to the jaw centerline as follows:

- $I = 1$: Central Incisor
- $I = 2$: Lateral Incisor
- $I = 3$: Cuspid
- $I = 4$: First Bicuspoid
- $I = 5$: Second Bicuspoid
- $I = 6$: First (6 year) Molar
- $I = 7$: Second (12 year) Molar
- $I = 8$: Third (Wisdom Tooth) Molar

The wisdom teeth are, however, customarily not involved in orthodontic procedure and usually are not yet present in the mouth of patients of treatment age. Furthermore, the second molars are often not involved in orthodontic treatment. To simplify the description and drawings, however, these designations are eliminated except where they are necessary to avoid ambiguity. Instead, the description below states verbally when it relates to, for example, the lower jaw (thus making use of the J subscript unnecessary) or where it relates to data or calculations relevant to a particular or either side of a jaw (thus making use of the S subscript unnecessary).

Further, many values are calculated or measured for each tooth I , or for each of a limited group of teeth, as, for example, the mesio-distal width MDW or the mesial and distal extremities $M_{X,T}$ and $D_{X,T}$ as in the description of step (300) below. Wherever possible, the I designation is also eliminated and the description instead describes how the variables relate to the various teeth. In addition, where some values such as MDW discussed above relate to a tooth dimension or the distance between two points on a tooth (and may be represented by a scalar value in a computer), other values such as the points $M_{X,T}$ and $D_{X,T}$ relate to points M and D , respectively (and may be represented by a pair of X and Y coordinates in a computer). Usually, the subscripts designating the two coordinates are omitted, and where helpful to clarify the description, a single one of the subscripts X or Y may be used, such as with D_X or D_Y , to designate that only the X or Y coordinate is employed, for example, in a calculation.

SYSTEM CONFIGURATION

Referring to the system diagram of Fig. 1, an orthodontic appliance manufacturing and patient treatment system 10 is illustrated. The system components are distributed between two locations, a doctor's

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office 11, and an appliance design and manufacturing facility 13. At the doctor's office 11, a patient 12, who requires orthodontic treatment, is examined by an orthodontist 14, who makes a diagnosis 15 of the condition of the patient and of the treatment, if any, needed. The examination involves the traditional application of the skill, knowledge and expertise of the orthodontist 14, and results in the preparation of detailed records 16 of the anatomy and condition of the mouth 18 of the patient, of the treatment proposed, and of other information necessary to the preparation of an orthodontic appliance.

The records 16 prepared by the orthodontist include a physical model 20 from a mold of the patient's mouth 18, which includes a mandibular model 21 of the patient's lower jaw or mandible 22 and a maxillary model 23 of the patient's upper jaw or maxilla 24. The records 16 also include prescription 27 wherein the orthodontist sets forth a treatment to be applied to the patient and a result to be achieved by the treatment. The prescription 27 may also include a specification of techniques that are to be included in the treatment and a designation of an orthodontic appliance to be employed. The records 16 will further include identification information 17 and patient history information 19.

In the illustrated embodiment of the invention, the records 16 are transmitted to the appliance manufacturing facility 13, at which the finish position of the teeth are calculated and a custom appliance 25 is designed and manufactured. The facility 13 is provided with one or more trained operators 28. In some embodiments, the physical model 20 itself is transmitted in the information 16 to the facility 13. In such cases, one of the primary functions of the operators 28 is to input digital information 26 from the records 16 into a computer 30a. Another function is to operate the same or another computer 30b to design the custom appliance 25, and to operate NC equipment 38 controlled by one of the same or another computer 30c to manufacture the appliance 25. Where the inputting, design and manufacture are performed at the appliance facility 13, the computers 30a, 30b and 30c may be the same computer 30.

In other embodiments of the invention, the orthodontist 14 digitizes data from the model 20, in which case the inputting computer 30 is located at the orthodontist's office 11. In these embodiments, the digitized information 26, rather than the physical model 20, is transmitted to the appliance facility 13. The analyzing and appliance design computer is nonetheless preferably at the appliance facility 13.

The entry of the information into the input computer 30 involves a digitizing of the information 16 to produce the digitized anatomical information 26 in machine readable form for analysis by the analyzing computer 30b. The input computer 30 connected thereto by a scanner 33, which, in the alternative embodiments of the invention, includes equipment that employs one or more video cameras, mechanical probes, laser scanners, ultrasonic scanners, moire image scanners or other forms of imaging or measurement hardware that alone, or in combination with other such components, produce anatomical geometric information that describes the patient's teeth and jaw. The images may be three-dimensional or be made along a plurality of planes or other surfaces that can ultimately be combined to provide information in three dimensions.

The combined information from the scanner 33 of the illustrated embodiment provides a basis for three dimensional analysis of the patient's teeth and from which calculations of finish tooth positions can be made. From the final positional calculations and tooth anatomy data, automatic design and manufacture of the custom orthodontic appliance 25 is carried out. In the illustrated embodiment, the data is imaged in a plurality of differently oriented two dimensional planes in the computer 30, then mathematically manipulated

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and combined in the computer 30b to construct a three dimensional solution to the tooth positioning and appliance design problems.

In a configuration in which the scanner 33 is connected to a separate dedicated inputting computer 30 is herein described, the functional equivalent of the inputting computer 30 may be included in circuitry within the scanner 33 itself.

Preferably, the digital input process utilizes interactive methods by which an operator 28 uses a pointing device and digitizer to select particularly useful orthodontic parameters from graphics images produced by the scanner 33 on a screen 35 of a display connected to the inputting computer 30.

In embodiments where some or all of the extraction of the digitized anatomical information 26 from the model 20, which may also be derived directly from the mouth 18 of the patient 12, is accomplished by the orthodontist 14 at the orthodontist's office 11, the information 26 is digitized by the orthodontist 14 then transmitted as part of the information 16 to the appliance design center 13. The transmitted information 16 is preferably transmitted from the orthodontist's office 11 to the appliance facility 13 by modem, but may be transmitted in any other available manner.

An analysis and design computer 30b, preferably at the appliance design facility 13, produces an archive diskette 34 that is formatted and written with all of the relevant information of the analysis and the history and prescribed treatment of the patient 14.

The computer 30b at the appliance facility 13 calculates, based on the digitized information 26, the final position of the patient's teeth, and the configuration of the appliance 25 required to move the patient's teeth to this final or finish position. As a result, calculated information for the patient is stored in a patient data file 36. From the calculations the computer 30c produces CNC machine readable code 42 for operating NC manufacturing equipment 38 to produce the appliance 25. An instruction document or file 37 is also produced, either by the computer 30b or the computer 30c, of information to aid the orthodontist 14 in treating the patient 14 with the custom appliance 25.

The manufacturing equipment 38 includes an appliance bracket cutting or forming machine 39 which produces custom brackets for the appliance 25 by cutting slots calculated angles and to calculated depths in slotless generic brackets. The machine 39 may also or alternatively shape the surfaces of the bracket bases. This provides the bracket design option of torquing the teeth by either the bracket slot or base, as may be best for various bracket materials.

The equipment 38 also includes an appliance archwire bending or forming machine 40 which produces custom shaped archwires for the appliance 25 by feeding and bending wire of any one of several available materials and stiffnesses into the custom archwire shape. The equipment 38 may also include a machine for forming patient treatment components and hardware to aid in the manufacture or installation of the appliance 25. In the illustrated embodiment, this includes a machine 41 for the making of bracket placement jigs, which cuts each tooth crown portion of the tooth profile into a plastic form, along with a superimposed cutout of the positioned bracket, for use in accurately installing the custom brackets in their calculated positions on the teeth.

The appliance manufacturing machines 38 may be connected directly to the analyzing computer 30b or one or more may be connected to a separate manufacturing equipment controlling computer or machine controller 30c. The computer 30c may be located at the appliance facility 13 or, together with one or more of the appliance manufacturing machines 38, 40 or 41, be located at the orthodontist's office 11. In one

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preferred embodiment of the invention, one manufacturing computer 30c and the bracket cutting machine 40 are located at the orthodontist's office, along with the scanner 33 and input computer 30, which may be the same computer as the manufacturing computer 30c, while another manufacturing central computer 30c, which may be the analyzing computer 30b, the wire bending machine 40 and the jig forming machine 41 are located at the appliance facility 13. The optimum distribution of the computers 30, 30b and 30c and the scanner 33 and appliance manufacturing machines 38, 40 and 41 will be determined by the scale of the orthodontist's practice and the orthodontist's preferences. In the illustrated embodiment, the computers 30-30c are IBM PC clones, with Intel 80386 or 80486 microprocessors and equipped with 80387 or 80487 math coprocessors, respectively.

Certain components of the system 10 of Fig. 1 are described below in further detail.

Scanning Assembly 33

Three steps in the information input procedure (82), described below, involve the inputting into the computer 30, for analysis in digital form, of data concerning the shape of the mouth 18 of the patient 12 and of the shapes of the individual teeth therein. In these steps, digitized images and measurement data of the mouth 18 of the patient 12, preferably taken indirectly from the model 20, and digitized to form a three dimensional mathematical model of the patient's mouth 18. The mathematical model includes, in the preferred embodiment of the invention, the definition of certain parameters of the patient's lower jaw and individual teeth, and may include some information of the initial position and orientation of the teeth in the mouth 18 of the patient 12 for evaluating the magnitude of the treatment.

The input information 26 is, in some embodiments of the invention, input as a full three dimensional image, and then simplified by reducing it to a plurality of curves in a plurality of differently oriented planes or fairly flat curved surfaces, each defined in the independent X-Y coordinate system of the respective surface or plane. In subsequent analysis, these planes are oriented, translated and rescaled with respect to each other in arriving at a derivation of the ideal finish positions of the teeth and the design of the custom appliance 25. In accordance with the preferred embodiment of the invention, curves and points on the contours of the jaw and teeth of the patient 12 are expressed in terms of accepted or generally applicable orthodontic parameters so that manual and automated decision making can combine and coordinate the best of orthodontic knowledge and experience with the efficiency and precision of computer analysis to minimize the use of the orthodontist's time, shorten the patient's treatment period and optimize the final treatment result.

The various types of and components of the scanner 33 of various embodiments of the invention are described below.

Video Scanning Data Input Assembly 43:

One preferred form or component of the scanner 33 includes a video imaging assembly 43 as illustrated in Fig. 1A. The video imaging assembly 43 includes one or more video cameras 44 which each produce two dimensional images of the patient's mouth 18, preferably by forming an image of the model 20. When two or more are used together, the video assembly 43 produces stereo images capable of being resolved in three dimensions. In the illustrated embodiment of the invention, a single video camera 44 is employed to produce two dimensional video images of a plan view of the patient's lower or upper jaws 22 and 24, from the models 21 or 23, respectively, in generally horizontal X-Y planes. In accordance with this embodiment, other forms or components of the scanner 33 are preferably employed to produce information in a third dimension as described below.

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Referring to Fig. 1A, the video imaging assembly 43 is shown diagrammatically in side elevation at the appliance manufacturer's facility 13. The video imaging assembly 43, in its preferred form, is an operator-computer graphical interface that includes the video camera 44 connected to a video interface board 44a in the input computer 30. The camera 44 is mounted on a stand 45 to face downwardly to form a top plan view one of one of the halves 21 or 23 of the model 20, shown as the mandibular portion 21 in Fig. 3, on a horizontal support 46 attached to a base 45a of the stand 45. The model half 21 or 23 is positioned on the support 46 such that the teeth face upwardly toward the camera 44 and so that the tips thereof lie generally in a horizontal plane that is maintained at a known fixed distance from the camera 44, so that the scale of the image formed by the camera 44 is known. This may be accomplished by mounting the support 46 on springs 46a to urge the model half 21 or 23 upwardly against a transparent horizontal plate 45b.

The input computer 30 has connected thereto a pointing device which may be a mouse 47a or, as shown, a mouse equipped digitizer board 47. The camera 44 produces a graphics image display 48 on the screen 35 of the computer 30, which an operator 28 may align with the assistance of a positioning grid G (Fig. 4A). With the digitizer 47, the operator selects points by positioning a cursor 48a on the screen 35 with the mouse 47a. The selection results in the storage of X,Y coordinate data for each of the points selected. The points selected, in the description of the preferred process below, correspond to preselected boundary points of the teeth and, from the mandibular model 21, the lower jaw. From these top view boundary points, tooth and mandibular jaw dimensions are calculated. The calculated dimensions are used in analysis steps to calculate equations for the mandibular bone structure or mandibular trough MT and to calculate from the trough equation and the calculated horizontal dimensions and relative positions of features on individual teeth the finish positions of the teeth.

In the alternative to selecting points from the video image display 48, the same points may be selected in the same manner from a plan view video image of a digitized three-dimensional computerized image of the teeth and jaws, such as an image formed by a laser scanner, moire interference pattern scanner, ultrasonic scanner, stereo video cameras, or other three-dimensional imaging apparatus. Sectional displays 55a and 55b of such a three-dimensional computerized image made with a laser scanner are shown in perspective in Figs. 3A and 3B, respectively. Such a laser scanner is described in connection with Fig. 1B below.

Laser Three-dimensional Image Input Assembly 51:

One preferred form or component of the scanner 33 is the laser generated three-dimensional image forming assembly 50 illustrated in Fig. 1B. Referring to Fig. 1B, one of the halves 21 and 23 of the model 20 is mounted on a support 51 while laser 52 directs a laser beam 52a onto the model 21 or 22. The laser beam 52a is reflected and the reflected beam is detected by a sensor 53 composed of a photoelectric pixel array which uses a triangulation method to convert a change in position on the sensor into a change in distance between the assembly 50 and the model 21 or 23 mounted to translate parallel to the model 21 or 23 on a support 54 so as to scan the model with the laser beam. Equipment for producing images using laser technology in this manner is commercially available for forming computerized representations in three dimensions of manufactured and other objects. An example of equipment suitable for this purpose are the Cyber Scan™ Measurement System manufactured by Cyber Optics Corporation of Minneapolis, Minnesota. The images formed by such equipment would preferably include full detailed three-dimensional image data of the patient's lower and upper jaws 22 and 24, taken from the model 20, with the teeth in their original

positions. The data is written in standard ASCII files by the equipment described and is readable by the input computer 30a into the digitized information files 26.

Illustrated in Figs. 3A and 3B are two sections of the mandibular digitized model, and include a section 55a showing the front mandibular incisors T_{22L} and T_{22R} of the patient 12, and a section 55b showing the right mandibular second bicuspid T_{23R} and first molar T_{24R} of the patient 12. When such images are rotated to a horizontal plan view, a derivation of the same information that is available from the video imager 43 of Fig. 1A may be derived, and points may be selected therefrom for digitization automatically with software, or through an operator/computer interactive process as with the video scanner 43. The three-dimensional image 55 may be rotated into other orientations for the derivation of other information in various planes such as vertical tooth profile information that is derived with the mechanical scanner 57 described below. Additionally, other computerized procedures may be used to automatically derive information from the three dimensional image 55 with or without intervention or interaction by an operator.

Mechanical Probe Digital Scanner Assembly 57:

The scanner may also include, alternatively or in combination with other scanning equipment such as the video scanner assembly 43 of Fig. 1A or the laser scanning assembly of Fig. 1B above, a mechanical probe assembly 57 as illustrated in Fig. 1C. This entire assembly 57 is used in the illustrated embodiment of the invention in combination with the video scanner 43 to derive labial-lingual vertical profiles of the individual teeth of the patient from the model 20 to supplement jaw and horizontal tooth dimensional and shape information derived from a video image produced by the video scanner 43 from the model 20. Alternatively, portions of this assembly can be used to produce the same information from a three dimensional image 55 produced by equipment such as the laser scanning assembly 50.

Referring to Fig. 1C, the probe assembly 57 includes a measurement probe 60 which is moveable over the individual teeth of the model 21 to produce an electrical signal that is digitized for computer input of point locations or profiles of the surfaces of the teeth in separate X-Y for each tooth. In the illustrated embodiment of the process of the invention, the information 26 preferably derived from the model 21 includes the tooth profiles curves PF_i in a labial-lingual plane viewed in a mesial-to-distal direction.

The probe assembly 57 further includes a magnetic base 59 upon which is mounted the model 20, and from which extends an upstanding vertical support 58 on which the probe 60 is mounted. The probe tip 60a is freely rotatable about a vertical axis on which its tip lies, while the probe itself is hooked to allow the tip to track recesses in the surfaces of the teeth of the model 21. The probe 60 is mounted on the support 58 to move in X and Y directions in a vertical plane preferably that extends through the support 58 and the probe 60. In this manner, the probe tip 60a is positioned to scan the surface of a tooth of the model 21 along this plane. The probe 60 is linked to the support 58 through a pair of orthogonal measurement position transducers 61, which respectively generate electrical analog measurements of the positions of the tip of the probe 60 along respective ones of the X-Y orthogonal coordinates. The outputs of the transducers 61 are connected to circuitry that generates a sequence of periodic readings of the transducer measurements of the probe tip positions which are then digitized. These outputs are sent in along lines 61a connected to input computer 30, preferably to a serial port thereof.

In use, a half of the model 20, for example, the mandibular model 21, is mounted upon the magnetic base 59 on a steel surveyor's mount 62 which slides on the base 59 when lightly urged, but which otherwise holds its place thereon for precise positioning. The mount can be raised, lowered or tilted for and for

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leveling. In operation, the probe 60 is manually moved by an operator 28 or automatically to scan the surface of each selected tooth of the model 21 to produce profile curves *PF* of a section of each tooth as illustrated in Fig. 3C. The profile *PF* may be generated by any one of a number of commercially available off-the-shelf CAD/CAM or illustration software packages, such as VERSACAD™ available from Prime Computers, Inc. of Bedford, Massachusetts. The computer programs described in the flowcharts herein is written for use with VERSACAD™ in CPL™, the programming language of therefor. The video images 63 of the profiles *PF* are displayed on the screen 35 and the digitized profiles are stored as part of the input information 26 in non-volatile memory of the computer 30.

With the curves such as the profile *PF* so formed, an operator can, with the use of the pointing device 47, select, by positioning the cursor on the formed profile on the screen 35, point parameters of the tooth, the coordinates of which can be thereby input digitally into the computer 30.

Appliance Manufacturing Equipment 38

The manufacturing equipment 38 of the preferred embodiment of the invention includes: an appliance bracket cutting or forming machine 39 that custom forms the bracket bases to mount to the teeth and cuts archwire slots in the brackets at precise calculated positions and angles; an appliance archwire bending or forming machine 40 that precisely bends archwires to a shape that will cooperate with the custom brackets to apply corrective forces to the teeth until they are in their calculated finish positions; and a bracket placement jig forming machine 41 that manufactures bracket placement jigs that conform to the contours of the patient's teeth, as recorded in the profiles *PF*. These jigs are used by the orthodontist to precisely place the custom brackets at calculated positions on the teeth.

The manufacturing equipment 38 is controlled by NC computer generated programs based on the data from the digitized input information files 26 and the calculated patient data files 36.

Bracket Cutting Machine 39:

Referring to Fig. 1D, a bracket slot cutting machine 39 is illustrated. The machine 39 includes a stationary base 72 on which is fixed a pair of upwardly extending workpiece support brackets 72a to the top of which is pivotally mounted a workpiece or bracket support 73. On the support, a full set 80a of brackets 80 for the custom appliance 25 is mounted, prearranged in an assembly or cartridge of twenty or twenty-four brackets. The support 73 pivots about an axis 73a extending between the brackets 72a. Connected to the axis 73a is an angular positioning motor 74 which positions the support 73, and the brackets 80 mounted thereto, to any angular orientation with respect to the horizontal. The motor 74 has an input connected to the computer 30c to set the inclination to the slot inclination angle of the bracket design in response to NC command codes.

Also fixed to the base 72 and extending upwardly therefrom is a saw support bracket 72b. To the top of the support bracket 72b is a saw drive motor 75 and a set of three saw blade positioning linear drive actuator 76, including an X-drive actuator 76x, a Y drive actuator 76y, and a Z drive actuator 76z through which a saw support arm 77 is supported to move respectively in the X, Y and Z directions, that is, in an X direction horizontally perpendicular to the axis of rotation 73a of the bracket holder 73, in a Y direction horizontally parallel to the axis of rotation 73a of the workpiece holder 73, and in a vertical Z direction. The actuators 76 have inputs connected to the computer 30c to receive positioning signals from the computer 30c to cut arcuate slots in the X-Y plane of the machine 39 in response to NC commands generated in accordance with a custom appliance design.

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At the remote end of the moveable arm 77 is a slot cutter assembly 77a, drivably linked to the motor 75. The assembly 77a has extending downwardly therefrom a rotatable cutter blade drive shaft 77b, which has fixed to the lower end thereof a circular slot cutter blade 77c. The blade 77c lies in the horizontal X-Y plane and is of the thickness of the slot needed for the thickness of archwire selected. The archwires are typically rectangular in cross-section so that they are able to exert torque on the bracket, which accordingly will be provided by the saw blade 77c with a slot of rectangular cross-section. The base of the slot will be cut, in accordance with the command signals from the computer 30c, at an angle in the X-Y plane of the machine 39 that is tangent to the final curve of the archwire that it will receive. The base of the slot will be convex to accommodate the curve of the wire in the horizontal plane. The base of the slot will be convex to accommodate the curve of the wire in the horizontal plane. The inclination of the bracket slot is achieved by the angle of the support 73 in response to control signals from the computer 30c. The computer 30c is programmed to account for changes in elevation of the bracket 80 due to the offset of the brackets from the support axis of rotation 73a.

Wire Bending Machine 40:

The wire bending apparatus 40 is illustrated diagrammatically in Fig. 1E. Primary control of the apparatus 40 is preferably by an IBM PC clone, preferably with an 80386 or 80486 microprocessor with a math coprocessor, and with motion controller board 65 installed. The controller board 65 is, for example, an MC300 Motion controller 3-axis card manufactured by Motion Engineering, Inc. The MC300 is a dedicated motion control card which sends and received signals to and from MC-OLS stepper interfaces 66a and 66b. MC-OLS stepper motor interfaces 66a and 66b send control signal commands to the stepper motor power supplies 67a and 67b, such as Compumotor S-Drive stepper power supplies #88-011483D, regarding rate and direction of motion of the motors.

The power supply 67a has an output connected to wire feed rollers 68, positioned on opposite sides of a wire guide 68a, which guides archwire 69 to feed it from a continuous coil supply. The power supply 67b has an output connected to a wire bending roller assembly or wire anvil 70.

The controller 66b additionally is adapted to receive feedback signals regarding position from a disc encoder 70a, such as a Dynapar/Veeder Root #E1000A76500, which monitors the position of wire forming roller 70b, providing closed loop control of a wire bending roller 70b. The roller is driven by a wire anvil motor 70c, such as a Compumotor #S/SX 57-102, through a drive screw 70d, such as an Industrial Devices Corp. Electric cylinder #X995A-2-M56-MT1-200-PS. The screw 70d converts the angular position of the motor 70c into linear motion of the roller 70b to deflect and bend the wire 69 as it is fed through the guide 68a by the rollers 68.

By coordinating the anvil 70 and the wire feed 68, formed archwires 64 of any planar shape are fabricated. The rollers 68 pinch the wire, forcing it to advance into the anvil 70. The roller 70b of the anvil 70 moves up and down varying the radius and thus controlling the radius to which the wire is permanently deformed. If the formation of archwires with inflection points, that is that have bends in opposite directions, a second anvil would be provided opposite the wire 69 from the anvil 70 and controlled in synchronism therewith.

A wire position sensor 71 is provided that inspects the finished archwire by comparing the width of the formed wire 64 to the desired width. The sensor 71 is mounted with respect to the anvil 70 and feed rollers 68 to detect the position of the formed archwire 64 when it is at the end of its forming cycle. This

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measurement provides a feedback signal that provides compensation for material property variations that effect the formed shape and the amount of overbending required. The sensor 71 sends information back to the computer 30c as to whether the wire 64 is acceptable or over-bent or under-bent. If the wire is either over or under-bent, the computer 30c calculates the correction required and incrementally modifies the signals through the interfaces 66a and 66b to provide compensation to progressively correct successive archwires 64 until the result of the signal from the sensor 71 is deemed acceptable by the computer 30c.

Bracket Placement Jig Forming Machine 41:

The bracket jig forming equipment 41 is preferably a standard NC mill configured as illustrated in Fig. 1F. The machine 41 includes the standard mill 81, having a downwardly projecting rotary tool head 81a on which is mounted an endmill tool 81b of, for example, 0.020 inches in diameter, where 0.022 inch archwire is used, and, for example 0.016 inches in diameter where 0.018 inch archwire is used.

The mill 81 is either connected to an controller which will have been loaded with CNC program code 42 prepared by the computer 30c or will be directly connected to the computer 30c. The mill 81 is provided with a tool support 81c to which a set of circular ABS plastic jig blanks 83, usually twenty or twenty-four in number, are fed by a feeding mechanism 81d, equipped with a magazine 81e of the sets 83a of jig blanks 83. The tool head 81a is moveable vertically to bring the tool 81b into contact with the blanks 83 and horizontally in the X-Y directions in accordance with the tool path instructions from the code 42.

GENERAL OPERATIONS AND PROCEDURES

In the preferred and illustrated embodiment of the invention, the overall configuration of which is illustrated diagrammatically in Fig. 1, the full custom system 10 is operated to produce the orthodontic appliance 25 based on the individual anatomy of the patient 12. One preferred method of the invention is represented by the operations and procedures illustrated in the flowchart of Figs. 2.

The method of the present invention, in its preferred embodiment, includes three general operations. The first operation, is (85) a patient evaluation operation performed by the orthodontist 14 at the doctor's office 11 on the patient 12. This operation includes the traditional professional diagnosis and general prescription of treatment. According to the present invention, the evaluation operation (85) is followed by (87) a computer aided analysis and appliance design and manufacturing operation performed, preferably at least in part, at the appliance facility 13 to produce the custom appliance 25, and in turn followed by a patient treatment operation (89), which includes treatment of the patient 12 by the orthodontist 14 at the doctor's office 11, with the installation and use of the appliance 25.

(85) Patient Evaluation Operation

Referring to the system diagram of Fig. 1 and the flow chart of Fig. 2, the orthodontic evaluation operation (85) is performed at a doctor's office 11. The operation (85) includes the procedures (90) of the examination of a patient 12, (91) the preparation of the model 20 of the patient's mouth and teeth, (92) the prescription by the orthodontist 14 of treatment, (93) and communication the appliance facility 13.

The examination procedure (90) the patient 12, who requires orthodontic treatment, is examined by an orthodontist 14, who makes a diagnosis 15 of the condition of the patient and of the treatment, if any, needed. Based on the diagnosis 15, the orthodontist or doctor 14 assembles the information 16 that is necessary to implement the prescribed treatment.

In assembling the information 16, the orthodontist 14 (91) prepares a model of the patient's mouth 18, usually a physical model 20 from a mold of the patient's mouth, in its initial condition at the time of the

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diagnosis 15. The model 20 includes the mandibular model 21 of the patient's lower jaw or mandible 22 and the maxillary model 23 of the patient's upper jaw or maxilla 24.

Then, further based on the diagnosis 15, the orthodontist 14 (92) prescribes a particular treatment and generates a prescription 27 in a tangible record form.

5 The orthodontist 14 then (93) communicates the information 16, for example, by transmitting the model 20, the prescription for treatment 27, a record of information 17 identifying the doctor 14 and the patient 12, together with information 19 containing statistical and historic data of the patient 12, to an appliance design facility 13, at some remote location. At the appliance design facility 13, the information 16 is digitized and input into the computer 30 for analysis.

10 Alternatively, the orthodontist 14 may convert the information 16 to digital computer readable form and transmit the digitized information to the appliance design facility 13. In this alternative, the system 10 would be configured with the input computer 30 located at the orthodontist's office 11, and the orthodontist 14 or assisting personnel would perform portions of an data input procedure (94) described below.

(87) Analysis, Design and Manufacture Operation

15 When the information 16, which includes, for example, the model 20, the prescription 27 and the information 17 and 19, are received either at the appliance system manufacturer 13 or is ready to be digitized at the orthodontist's office 11, (87) an analysis, finish tooth position calculation, and orthodontic appliance design and manufacturing operation is begun. In the operation (87), the information 16 is processed and the custom appliance 25 for moving the patient's teeth to an optimum final or finish position in accordance with treatment prescribed by the orthodontist 14 is produced.

20 The operation (87) includes the procedures of (94) inputting into a computer the information 16 from the orthodontist 14, in digital form, (95) analyzing with the aid of computer 30b the input digitized information to arrive at the finish position of the teeth, (96) designing with a computer a custom orthodontic appliance in accordance with the computer analysis, (97) manufacturing the custom appliance 25 in accordance with the computer assisted design with the aid of computer controlled machinery, and (98) communicating the custom appliance 25 and accompanying instructions to the orthodontist 14.

25 In accordance with certain embodiments of the present invention, some or all of the appliance manufacturing step (97) can be performed at the facilities 11 of the orthodontist 14, in which case the communicating step (98) would involve the communication of machine readable code, in lieu of some or all of the completed custom appliance 25, from the design facility 13 to the orthodontist 14.

(94) Input Procedure:

30 In the input procedure (90) is illustrated in the flowchart of Fig. 2A. In the procedure (94), the received information 16 is input, in the illustrated embodiment by operator 28 at the design facility 13, into a computer 30 in digital form. Even where the inputting is performed by operator at the design facility 13, some information 16, such as the information 17 and 19, may be supplied by the orthodontist 14 in machine readable form and input directly into the computer 30. The input procedure (94) includes five steps (100)-(500), the substeps of which are described in detail in connection with the flowchart details of Figs. 2E-2I below. The steps of the input procedure (90), in the illustrated embodiment, also include certain substeps that are part of the function of the analysis step (92) but are more conveniently performed at the time of the information is entered into the computer.

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The input steps (100) and (200) involve the entry of background information assembled by the orthodontist 14. In the input steps (300), (400) and (500), tooth and jaw positions and profiles are defined in terms of orthodontic parameters and landmarks that can be later analyzed by computer to best implement the orthodontic knowledge, skill and experience embodied in the prescription 27 and of the orthodontic profession while efficiently automatically producing a optimum result. These steps of the input procedure (90) include:

(100) The inputting of the doctor-patient identification information 17 in digital form into the computer 30a:

This information is used to identify the records of the patient and the products produced.

(200) The inputting of patient background information 19 in digital form into the computer 30a:

This information is used in part in the calculating the finish position of the patient's teeth in accordance with genetic characteristics. Sex and race, for example, are used to assign certain seed values such as the inclination of the axes of the individual teeth of the patient 12 to an arch plane in step (625), which is used to determine an offset for tips of the teeth from the jaw bone or gum line.

This information also includes diagnostic determinations and treatment option decisions made by the orthodontist 14, such as determinations to extract teeth, or employ optional treatment norms.

(300) The inputting into the computer 30, from a top view image of the patient's mandibular model 21, the mandibular jaw shape and tooth dimensional information:

In implementing a treatment to correct the tooth alignment of the patient 12, the mandible 22 is the logical starting point because it is a solid bone and has relatively little pliancy. By contrast, the maxilla or upper jaw 24 is composed of segments held together by sutures which do not fuse until mid or late teens. Furthermore, these sutures can be separated by the orthodontist even after the point of initial fusion by simple and commonly known clinical techniques. These anatomical factors require that the orthodontist 14 make relatively small changes in the mandibular bone 22 and the preponderance of skeletal changes in the maxilla 24. For this reason, the position of the mandibular trough *MT* therefore taken as a constraint on the positions of the roots of the lower teeth.

In step (300) information is input for use, in part, to define from the patient's lower jaw bone the shape of the mandibular trough *MT*, which serves as the first constraint in arriving at the finish position of the teeth. In one embodiment, this is accomplished by superimposing a predefined grid *G* on a video or graphics image of the mandibular trough (from Fig. 3) in the manner illustrated in Fig. 4. In addition, the distances between the mesiodistal extremities, or mesiodistal widths *MDW*, that is, their contact points with adjacent teeth, in a horizontal plane, are input. These determine the total length of the dental arch and the relative center-to-center spacings of the teeth along the arch.

A mandibular trough equation *MTE* is derived, and may be converted to a symmetrical equation *SMT*. As a starting point toward calculating finish tooth position, the mesio-distal widths of the mandibular teeth are mathematically placed on the trough equation. This is explained more fully below in connection with Fig. 4.

In the above and in many archform calculations below, a cubic spline equation form is used initially in fitting a curve to data points, then converted to a circle segment equation that provides advantages in the analysis and design process and in the final calculations needed to operate NC manufacturing equipment. This is explained below in connection with Figs. 5 et seq.

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Measured initial contra-lateral cusp spacing data are generated for use by the orthodontist 14 in evaluating the custom design and treatment parameters resulting from the final calculations below.

In some embodiments, horizontal profile data of the lower jaw may be input in this step, additional landmarks in the horizontal plane may be identified, or full three-dimensional images of the teeth and lower jaw may be made, for example, as discussed in the descriptions of Figs. 1A-1C above.

(400) The inputting into the computer 30, from a bottom view image of the patient's maxillary model 23, maxillary tooth dimensional information:

The shape of the maxilla, which is made of a segmented bone, is a variable capable of being altered orthodontically in response to final tooth position calculations as set forth below. Therefore, its initial shape and initial maxillary tooth position is relevant only in evaluating the feasibility of the amount of alteration required and the type of treatment to be used.

In step (400), information is input into the computer 30c of maxillary jaw shape and tooth dimensional information from the maxillary model 23. This information is used in part to determine the mesiodistal widths *MDW* of each upper tooth, in a horizontal plane, and to determine the total length of the dental arch and the relative center to center spacings of the teeth along the arch.

Measured initial contra-lateral cusp and central groove/fossa spacing data are generated for use by the orthodontist 14 in evaluating the custom design and treatment parameters resulting from the final calculations below.

As with step (300) above, in some embodiments, horizontal profile data of the upper jaw may be input in this step, additional landmarks in the horizontal plane may be identified, or full three-dimensional images of the teeth and lower jaw may be made, for example, as discussed in the descriptions of Figs. 1A-1C above. In these embodiments, techniques such as those described in step (500) may be employed in the horizontal plane in steps (300) and (400).

(500) The inputting of individual tooth elevational profile information from the two halves of the model

The tooth profile information can be generated using computer analysis or interactive computer imaging from three-dimensional images, if employed, as illustrated in Fig. 3A formed with scanners such as illustrated in Fig. 1B, or with the use of the probe assembly 57 of Fig. 1C from the physical model 20 of the jaw. Use of the probe assembly 57 is herein described.

Rapid reduction of tooth shape information to important dimensions and landmark data for efficient and realizable calculations of finish tooth position is achieved by imaging carefully selected profiles of the teeth. Profiles are produced by outlining the tooth crown surfaces along a vertical plane or other similarly oriented surface that extends in a labial-lingual direction generally perpendicular to the arch of the teeth in the respective jaw. For the single cusp anterior teeth, this surface is generally a surface bisecting the tooth and through the crown long axis *CLA* of the tooth. For multiple cusp teeth, the same generally applies except modification or displacement of the surface is intelligently made on some teeth to pick up the highest cusp or a marginal ridge that is relevant to development of the proper occlusion.

For most calculations, as set forth in the detailed explanation below, the tooth features profile can be assumed to be on a plane through the tooth centerline, even when they are not. With the features selected herein, such assumptions result in errors that are still much smaller than those accepted in

conventional methods. In other calculations, the precise position of a feature must be considered, and provision for such considerations are made in the certain embodiments of the invention.

For each tooth, profile data is taken in separate X-Y coordinates that relate only to the selected surface or plane. In the course of the analysis and calculation of finish tooth position, these planes are separately translated and reoriented with respect to those of the other teeth and those of the trough and archforms, in several steps, until the ultimate interplane relationships are established.

(95) Analysis and Tooth Positioning Procedure:

The computer analysis procedure is illustrated in the flowchart of Fig. 2B. In the computer analysis procedure (95), the digitized information input by the input procedure (94) is analyzed to calculate the finish position of the teeth, so that the custom appliance 25 can be designed in computerized design procedure (96) and manufactured in computer controlled manufacturing procedure (97). The analysis procedure (95) includes six steps and subroutines (600)-(1100), the substeps of which are described in detail in connection with the flowchart details of Figs. 2J-2O below. These steps include the following:

(600) The dental analysis step in which the orthodontic landmarks of the teeth are identified:

A minimum number of points on the tooth profiles are selected that are sufficient for determining the contact points between teeth that are relevant to finish tooth position calculation and appliance design. These points are selected such that the calculations made from them are relatively insensitive to measurement errors in the input of the data in step (500). From the selected points, for each tooth, other parameters are derived, including an incisal center point *ICP*, a gingival center point *GCP* and the crown long axis *CLA* through the *ICP* and *GCP*, as explained below in connection with step (600) and Fig. 6 et seq.

In order to determine the relationship between the crown long axes and archwire planes, twenty-four of each crown type were removed from a set of orthodontic casts and sectioned along the mid-sagittal plane. These crowns were then mounted and projected at twenty times magnification on an optical comparator. Tracings were then made of these profiles. As a result, a procedure was determined for use to establishing the crown long axis inclination angles to produce the desired occlusion, and seed values were tabulated that and correlated with data such as the sex and race of the patient as entered in step (200). As a result of this analysis, preferred crown long axis inclination angles are produced with the present invention that are an improvement over the facial inclination angles employed in the prior art.

From the tabulated data, angles of inclination *LAI*s of the crown long axes *CLAs* of each of the teeth of each jaw are set relative to the plane that contains the mandibular trough equation *MTE*. This plane is parallel to a facial axis plane *FAP* used in clinical studies through a clinically defined facial axis *FA* of a tooth. These *LAI*s are later used to determine the horizontal offsets from the *MTE* of the tips of the lower teeth in step (1000) below, as well as the maxillary tooth placement in step (1100). The rotation of the inclination angle places new *Y* coordinates of each of the tooth profile planes established in step (500) parallel, and the *X* axes of these planes parallel to the same plane but of with their relative horizontal orientations and relative vertical positions yet to be determined. Once the teeth are rotated to their finish inclinations, precise crown heights, incisal and cusp tip locations, and other points and contours of the tooth surface are precisely defined for intertooth contact and appliance design and positioning calculations.

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As an example, for the maxillary bicusps and molars, a marginal ridge elevation *MRE* is determined for later use in calculations relative finish positions of the upper and lower teeth.

(700) The cuspid rise determination step in which the occlusion of the upper and lower teeth is defined:

The orthodontist 14 will have selected the technique to be used to guide the teeth of the patient into occlusion as the jaws come together. Depending on the selected occlusion technique, either all or part of the occlusion is brought by a rise of the cuspids above that of the other teeth, to thereby initiate contact between the upper and lower teeth which aligns the two arches as the jaw closes. Most orthodontists prefer to accomplish this with the rise of the cuspids.

From anatomical studies, data is employed and the amount of cuspid rise, or other cusp rise if selected, that is necessary to clear the buccal cusp height *BHC* of the teeth, which is determined from the landmark data of step (600).

(800) The mandibular tooth placement step in which the plane of the mandibular teeth is defined and the teeth are positioned with respect to the mandibular trough:

The step (800) accomplishes the preliminary mathematical construction of the mandibular occlusion. This step first calculates the positions of the mandibular teeth to place their tips in an occlusal plane pending final refinement of the placement.

The starting point for the mandibular tooth placement is to assume tooth positions that place the teeth with their crown long axes *CLAs* intersecting the plane of the mandibular trough on the mandibular trough equation *MTE*. This satisfies the condition that the mandibular teeth are set in the bone of the lower jaw. The *CLAs* of the teeth are also inclined at the seed value angles *LAI*s established in step (600).

Next, the positions of the teeth are adjusted vertically to place the tips of all of the mandibular teeth, except the cuspids, in the same plane. The tips of the mandibular cuspids are set to extend above the plane of the tips of the other mandibular teeth by a distance according to the cuspid rise criteria selected, preferably by setting the distance equal to one third of the total cuspid rise, as calculated in step (700).

Then, a horizontal *OFFSET* from the *MTE*, generally in the labial direction, is calculated trigonometrically for each mandibular tooth from its crown height above the mandibular trough and its long axis inclination angle *LAI*. This calculation results in a mandibular trough offset equation *MO*, which is an outward radial expansion of the *MTE*. The *MTE* was defined in the form of a series of circle segments in step (300). The expanded *MO* equation is a discontinuous arch constructed by adding the respective *OFFSET* of each tooth to the radius of the circle segment of the *MTE* with which the midpoint of the width of the tooth is associated.

The teeth are then placed on the offset equation *MO* beginning with the placement of the central with its mesial contact point on the mandible centerline and the tooth midpoints on the *MO*. Then moving distally, the remaining teeth on the same side of the mandible are placed on the *MO* with their mesial contact points *HCP* in contact with the distal contact point *DCP* of the previous tooth. The same procedure is employed for the teeth on the other side of the mandibular arch.

An alternative further refinement would consider the vertical position on the teeth of their widest points and, considering the also the inclinations of the teeth, make a trigonometric adjustment so that the tooth contact points are spaced by the tooth widths *MDW* at the height of their actual widest points, rather than assuming the teeth contact in the plane of their tips.

(900) The best fit cusp step in which the best fit equation is derived for mandibular arch:

In this step, a continuous curve is derived using statistical methods to produce a best fit buccal cusp equation *BFBCE* from the disconnected line segments of the *MO*. This is also illustrated in Fig. 4A. In the embodiment described below, a Bezier equation is used. A cubic equation is then generated from resulting data points that define the best fit equation. The cubic equation of the *BFBCE* is then converted to circle segment form as with the *MTB* above.

(1000) The mandibular teeth placement step in which the positions of the mandibular teeth are calculated for placement on the best fit arch equation:

The positions of the lower teeth are then recalculated to move the teeth horizontally, parallel to the *MOC*, such that the incisal center points *ICP* lie on the *BFBCE*. For incisors and cuspids, the *ICPs* are the tips of the teeth in the profile planes of steps (500) and (600). For the bicusps and molars, the *ICPs* are the buccal cusp tips of the teeth. For purposes of placement of the teeth on the *BFBCE* or other archform, the *ICPs* are assumed to lie midway between the mesial and distal contact points of the respective teeth. Accordingly, tooth placement is achieved by moving the teeth normal to the circle segment associated with these *ICPs*. This recalculation of position has the effect of moving the roots of the teeth normal to the arch associated with their *ICPs*, either labially or lingually, such that their *ICPs* fall on *BFBCE*, when viewed from above.

This placement is the finish position of the mandibular teeth.

(1100) The maxillary placement step in which the maxillary arch is derived for occlusion with the placed mandibular teeth:

This step fits the positions of the maxillary teeth to the already positioned mandibular teeth. The maxillary teeth have not yet been positioned with respect to any equation, but the inclination angles of their dimensions and crown long axes *CLAs* have been determined in step (600). This positioning involves setting the tips of the maxillary teeth on the *BFBCE*, with certain modifications to the equation and the placement criteria to account for the way the different types of teeth occlude.

In adjusting maxillary tooth positions, the cuspids, the anterior teeth and the posterior teeth are treated separately to bring their relevant contact surfaces into three different respective arches that are then aligned relative to each other.

Since the anterior teeth do not occlude incisal edge to incisal edge, the *BFBCE* is modified to take into account the distance from the *BFBCE* to the labial contact points of the mandibular incisors and laterals, plus a horizontal or labial clearance, with the maxillary teeth. This defines the points of occlusion with the maxillary anteriors, at the intersection of their lingual surfaces with the plane of occlusion *MOC*. These points lie in a maxillary anterior contact arch form *MAAF*. This equation is calculated by expanding the *BFBCE*, by enlarging the radii of the circle segments of which it is made up, to account for these tooth dimensions and the clearances.

The vertical positioning of the maxillary anteriors and cuspids is then performed based on the vertical occlusion methods that have been prescribed, establishing an overlap for the incisors and cuspid rise as determined in step (700). This defines the vertical position of the maxillary cuspids and anteriors with respect to the *MOC*, and thereby defines the incisal overlap or overbite.

Placement of the maxillary posterior teeth places the intersections of the marginal ridges and the central grooves from steps (400) to (600) the cusps of the mandibular teeth with which they will occlude.

The maxillary tooth movements needed to achieve this occlusion are applied to calculate a central groove marginal ridge arch form *CGMRAF* by modifying the *BFBCF*. The cusp tips of the maxillary cuspids are placed between the archforms of the incisors and of the posteriors, for example, by averaging the distance from the *BFBCF* to the *MAAF* and to the buccal cusp of the first maxillary bicuspids, by placing the cuspid mesial and distal contact points in contact with the adjacent teeth, by calculating a clearance as was done for the incisors or by some other criteria. The archforms for the maxillary tooth placement are illustrated in Fig. 4B.

The vertical positioning of the remaining teeth takes into account the occlusion and other prescription information input in step (200). The remaining calculations are set forth in detail below.

(96) Appliance Design Procedure:

The appliance design procedure (96), as illustrated in the flowchart of Fig. 2C, calculates the dimensions of the appliance components in a form capable of being translated into NC codes for operating NC machinery for production of the appliance components, such as the brackets and archwires and also placement jigs for installing the brackets in the proper positions on the teeth of the patient. In the appliance design procedure (96) includes the following steps (1200) through (1800), which are further illustrated in the detailed flowcharts of Figs. 2P-2V:

(1200) The mandibular archwire plane step in which the plane of the archwire for the mandibular teeth is defined in relation to the teeth of the mandible:

Where labial brackets are to be applied, as illustrated in Fig. 8, a plane is selected for the mandibular archwire that avoids interference with the mandibular archwire and brackets with the maxillary teeth, which overlap on the labial side of the mandibular teeth. Where lingual brackets are to be applied, this step is performed to define a maxillary archwire plane to avoid interference between the lingually mounted maxillary archwires and brackets with the mandibular teeth that overlap on the lingual side of the maxillary teeth.

This step involves the selection of the archwire plane and defines it in mathematical relation to the *MOC*. Once defined, the bracket positions on the teeth are determined such that the archwire slots will lie within the dimensional limits of the bracket. Where possible, it is preferable that the archwire lie in a literally flat plane and be symmetrical about the midline of the arch. As such, the archwire will be properly shaped for installation with either side facing upward.

(1300) The mandibular slot inclination step in which the angles of the slots of the mandibular tooth brackets of the appliance are calculated:

The slot inclination angle for the mandibular brackets is calculated from the angle between the mandibular archwire plane and the angle of the mandibular tooth surface to which the base of the bracket is to be mounted. The slot inclination angle may be achieved by cutting the full angle into the slot, by inclining the bracket base, or by both of these methods.

(1400) The maxillary archwire plane step in which the plane of the archwire for the maxillary teeth is defined in relation to the teeth of the maxilla:

The maxillary archwire plane in the case of labial appliances, and the mandibular archwire plane in the case of lingual appliances, has few constraints on its position and may be selected based on cosmetic considerations. It is usually selected as a plane midway on the crown of the maxillary teeth. It is therefore normally not parallel to the mandibular archwire plane. Once defined, the bracket positions

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on the teeth are determined such that the archwire slots will lie within the dimensional limits of the bracket.

(1500) The maxillary slot inclination step in which the angles of the slots of the maxillary tooth brackets of the appliance are calculated:

5 The slot inclination angle for the maxillary brackets is calculated from the angle between the maxillary archwire plane and the angle of the maxillary tooth surface to which the base of the bracket is to be mounted. The slot inclination angle may be achieved by cutting the full angle into the slot, by inclining the bracket base, or by both of these methods.

10 (1600) The mandibular archwire and bracket in-out dimension calculation step in which the slot depth and bracket geometry is calculated for the mandibular tooth brackets:

For each bracket, the deepest and shallowest slot depths is determined to develop a window into which the archwire must pass, as illustrated in Fig. 8A. Then the smoothest archwire curve that will pass between the depth limits is determined. The smoothest curve is considered to be one with the least variation in radius changes along the curve, and preferably with no inflection points. A cubic spline equation is used to fit the points and the equation is then converted to one of circle segment form.

15 (1700) The maxillary archwire and bracket in-out dimension calculation step in which the slot depth and bracket geometry is calculated for the maxillary tooth brackets:

As with the mandibular slot depth calculations, for each maxillary bracket, the deepest and shallowest slot depths is determined to develop a window into which the archwire must pass. Then the smoothest archwire curve that will pass between the depth limits is determined. Here to, the smoothest curve is considered to be one with the least variation in radius changes along the curve. A curve with no, or the least number of inflection points is preferred. A cubic spline equation is used to fit the points and the equation is then converted to one of circle segment form.

20 (1800) The bracket placement jig designing step in which placement jigs are designed for use in properly positioning the custom designed brackets on the patient's teeth:

After the brackets and archwires are completely defined as in the above steps, with the depth and angle of the slots finalized for in the positioning of the brackets on the teeth and the shape of the desired archwires are described mathematically, bracket placement jigs are designed that will be used to assist the orthodontist in placing the brackets at the proper locations on the teeth. The designing of the jigs, in the preferred embodiment, is carried out in the software that generates the NC machine code in the performance of the jig manufacturing step (3500) below. This deferring of the jig design allows for consideration of appliance hardware modifications that may be made in the course of the bracket and archwire forming steps (3000) and (3200), respectively.

30 The provision of the bracket placement jigs furthers a goal of the practice of orthodontics to treat cases to occlusal perfection with the least amount of effort, discomfort and time expended. The portion of this goal that can be accomplished by appliance design and manufacture has been described above. While the individualized appliance geometries thus defined will be fabricated, the ability to place the bracket portion of the appliance system on the teeth with sufficient accuracy to allow the appliance system to deliver the desired orthodontic relationship, heretofore not realized clinically, is provided as follows:

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The brackets are placed according to the three criteria:

1. Height: The height is established so that the appliance causes the upper and lower teeth to contact each other in the prescribed manner.

2. Mesio-Distally: The mesio-distal location is established so that the mesial and distal ridges of the teeth are parallel to the archform for that patient.

3. Long Axis: The bracket is aligned relative to the long axis of the tooth so that the appliance system tips the tooth to the desired angle relative to the archwire.

From the vertical profile data of step (500), and horizontal or three dimensional profile data of steps (300) and (400), the shape and size of each tooth is extracted, including particularly the profile in a mesio-distal view at the height of contour or along a plane perpendicular to the greatest prominence of the central developmental lobe of each tooth. Additionally, the geometry of the archwire slot has been accurately related to the respective teeth. This geometry includes the intersection of the archwire plane with the tooth profile curve, the slot inclination angle and the slot in-out dimensions. In addition, the wire size and bracket geometry information are assembled, and tool size and clearance information are taken into account.

With this information, a bracket placement jig is designed for NC controlled manufacture to position the slot, and thereby the bracket, precisely on the tooth.

In Fig. 8D, a plastic jig 82 is shown which engages the walls and bottom of the bracket slot fully. Additionally, the portion of the jig 82 contacting the tooth designed to be formed to precisely fit the known contour of the tooth, as determined by the profiles input in step (500). This assures that the bracket slot and hence the bracket is placed at precisely the correct height when bonded to the tooth.

Brackets are placed so that the slots are not necessarily perpendicular to the long axis of the tooth but at varying degrees of cant. The jig 82 accomplishes this goal by the use of an adapter 84 that fits into the bracket slot 82b and a coplanar slot 84a (Fig. 9T) to engage the plastic blade jig 82, as illustrated in Fig. 8D. The jig design substeps, which are preferably performed in step (3500) and included in the detailed flowchart of the jig manufacturing step of Fig. 2Z, are summarized in the flowchart of Fig. 2V. The design is converted into CNC code in step (3500) for controlling the jig forming machinery 41 primarily to cut a contoured surface that conforms the profiles of the tooth so that the jig fits in a precise position on the tooth to position the bracket for adhesion to the teeth.

In installation performed in the treatment operation (89), the jig 82 is lined up with the long axis of the tooth crown when viewed from either the front or facial surface of the tooth and from the biting or occlusal surface. A plastic blade form of jig 82 offers visual reference to the height of contour of the tooth and alignment of the bracket with the marginal ridges.

(97) Appliance Manufacturing Procedure:

The appliance manufacturing procedure (97), as illustrated in the flowchart of Fig. 2D, entails the generation of controller codes for NC machinery to produce the brackets, archwires and bracket placement jigs designed in the appliance design procedure (96), and the manufacture of the appliance components with the use of the machinery controlled by the codes. The procedure (97) includes the steps of:

(3000) Controlling and operating the bracket forming machinery 39 to produce the custom brackets:

The bracket manufacturing procedure of the preferred embodiment involves the generation of NC code for the bracket slot cutting mill 39 of Fig. 1D, as illustrated in the flowchart of Fig. 2X. The step

involves the geometric relating of the tooth profile information *PF* for each tooth, and other tooth contour information of the shape of the surface of the tooth to which the bracket is to be attached from steps (300) and (400), and the archwire plane, slot inclination angle and slot depth information from steps (1200) through (1700). In addition, the bracket forming step performs the function of selecting the bracket blank from which the bracket is to be fabricated. The bracket blank is made up of a base or pad that is attached to the tooth and an outwardly projecting support into which an archwire slot is formed.

The preferred embodiment includes the forming of brackets by cutting custom slots in bracket blanks while preserving the base inclination angle. Brackets could be alternatively fabricated by inclining the bracket bases or pads. Additionally, bracket bases may be contoured to conform to the surfaces of the teeth, or a bonding agent may fill the space between the bracket base and the tooth. Furthermore, while in the preferred embodiments, a mechanical cutter blade forms the bracket, other means such as wire EDM, machining, casting or stereo lithography may be employed.

(3200) Controlling and operating the Wire-bending machinery 40 to produce the custom archwires:

The software that operates the computer 30c to drive the wire bending apparatus 40 reads data files generated for the mandibular and maxillary archwires in steps (1600) and (1700) respectively. Also read by the computer 30c are data on the characteristics of the unformed wire 69, including that relating to the material of which the wire is made, as well as its cross-sectional shape and dimension. The file that is read contains coordinated data regarding calculated archwire segment lengths and radii which cumulatively describes geometrically the desired archwire shapes. As explained above, the archwires consist of a sequence of tangential arc segments with each segment a particular length and radius.

The arch forming software determines the position of the roller 70b of the anvil 70 that is required to produce a given radius in the particular wire material and cross-section by going to a look-up table, previously derived and stored in a file accessible by the computer 30c, containing constants necessary to correct for each wire material and cross-section. The anvil 70 is driven to the desired position to produce the required radius and the feed roll motor 70c is driven to create the desired length of wire at that radius. By adjusting the position of the anvil roller 70b and length of wire fed for with the roller 70b so adjusted, archwires 64 of the calculated final sequential tangential radii are fabricated.

(3500) Controlling and operating the jig forming machinery 41 to make custom placement jigs for the location of the brackets on the patient's teeth:

The machine control codes for controlling the jig forming machinery 41 are produced directly from the tooth profiles generated in step 500 and from the archwire plane location of steps (1200) and (1400), the slot inclination steps (1300) and (1500), and the slot in-out dimensions from the steps (1600) and (1700). As stated above, the jig design step (1800) is preferably performed in the course of, and is described herein as part of, the jig manufacturing step.

The profile data, which represents the profile curves with a fairly high resolution of data points is a series of straight line segments for developing the codes for driving the NC equipment. Tool and bracket dimensions and design clearances are also taken into account, and CNC codes are generated to cut jigs from circular plastic wafers on a standard CNC mill using a small carbide endmill tool. The details of the substeps of the step (3500) are included in the flowchart of Fig. 2Z.

(98) Appliance Transmission Procedure:

One of the ultimate objectives is to place the custom orthodontic appliance 25 into the hands of the orthodontist 14, along with the tools and information necessary for the proper installation of the appliance 25 in the mouth of the patient 12 to treat the patient by moving the patient's teeth to the calculated finish positions. This is best understood by reference to Fig. 1.

Referring to Fig. 1, as set forth above, the configuration of the preferred system 10 will vary depending on the nature and scale of the orthodontist's practice. Preferably, all or much of the appliance design portion of the procedure (87) takes place at an appliance design facility 13, although in a large scale orthodontic clinic, the entire process could be carried out at the patient treatment location. Usually, however, the functions performed in the design computer 30b, or design portion of the computer 30, are carried out at the appliance facility 13, together with some of the manufacturing functions performed by the manufacturing control computer 30c and the appliance manufacturing equipment 38.

In the configuration where, as illustrated, some or all of the appliance 25 is made at the appliance facility 13, the custom appliance 25 is transmitted to the orthodontist 14. Along with the appliance 25 is communicated documentation in the form of a hard copy printout of information 37 generated by the design computer 30b, which could also include documentation of the input data that made up the data 26 and the prescription information 27, and a printout of parameters recorded by the manufacturing computer 30c.

The transmitted appliance 25 includes a set of archwires 64, as illustrated in Figs. 8E and 8F, a complete set of custom brackets 80, as illustrated in Figs. 8D and 8F, and the placement jigs as illustrated in Figs. 8D and 9T through 9W. Along with the jigs 82 are included a set of adapters 84 that are used to align the slots 80b of the brackets 80 with coplaner slots 84a of the jigs 82. The appliance and the bracket placement jigs therefor are similar in the case of lingual appliances, a bracket for which is illustrated on a tooth in Fig. 8G while the lingual appliance is shown positioned on the mandibular teeth in Fig. 8H.

In addition, custom archwires 64 are transmitted to the orthodontist 14. These archwires include archwires in the exact form, as illustrated in Fig. 8E, to move the teeth to their finish calculated positions, as illustrated, for example for the lower teeth, in Fig. 4D. In Fig. 4D, the archwire 64 is shown in the unstressed state (or having nominal residual stress sometimes motivating some orthodontists to prescribe overcorrection) that it will attain when the appliance 25 has moved the patient's teeth to the calculated finish positions. This is the same shape as the archwire of Fig. 8E shipped to the orthodontist 14. This finish archwire will be of a material and stiffness determined to be appropriate for the final positioning of the teeth. Depending on the severity of the initial malpositioning of the patient's teeth, however, less stiff archwires, or temporary archwires may be desired for beginning the orthodontic treatment. Thus, additional archwires 64 of various properties but in the shape shown in Fig. 8E will be provided the orthodontist 14. In addition or in the alternative to the provision of these additional archwires, an actual size drawing or template having thereon the shape shown in Fig. 8E will be provided the orthodontist 14 to enable him to form archwires for preliminary treatment and rough positioning.

In alternative configurations, information may be sent from the design computer 30b in machine readable form, for example by diskette 34 or modem, to a manufacturing computer 30c to which is attached one or more of the appliance component manufacturing machines 38.

(89) Patient Treatment Operation

The patient treatment involves, first, the assembly of the respective bracket 80, jig 82 and adapter 84 combinations, as illustrated in Fig. 8D, and the application of the brackets 80 thereby to the patient's teeth. This involves the application of adhesive to the area generally in the center of the face of the tooth, either labial or lingual, to which the brackets 80 are to be applied. This is illustrated in Fig. 8D, for example, with the application of a bracket 80 to the labial face of a maxillary incisor T_{2L} . The assembly is positioned on the tooth with the blade of the jig 82 positioned on a generally vertical labial lingual cross section through the approximate center of the tooth, in the plane that may be said to contain the crown long axis *CLA* of the tooth.

When the bracket adhesive has set, the bracket placement jig 82 is removed by first sliding out the adapter 84 mesiodistally and then sliding the jig 82 off of the incisal edge of the tooth, leaving the bracket in the calculated position.

Then, with the brackets 80 set on the teeth the archwire 64 is installed. Often, the first archwire installed will be one of lower stiffness than the final archwire. In the example of Fig. 8F, the mandibular teeth in their initial position as illustrated in Figs. 4 and 4A are shown. The brackets 80 are positioned on the teeth in the exact same positions as shown in the calculated finish position diagram of Fig. 4D. Because the teeth are not yet in this ideal finish position, the archwire 64, when inserted into the archwire slots and tied to the brackets 80, will be stressed into the elastically deformed condition shown in Fig. 8F. This stressed condition of the archwire 64 operates, without the need of the orthodontist to artfully bend the wire, to apply the forces to the teeth to urge them toward the ideal positions of Fig. 4D. This force will continue to be applied until the teeth have moved to the finish positions. In some prescribed forms of treatment, the wire and brackets are designed to move the teeth to a slightly overcorrected position to allow for a relaxation movement of the teeth when the appliance 25 is removed.

**DETAILS OF STEPS OF APPLIANCE ANALYSIS,
TOOTH POSITION CALCULATION, AND APPLIANCE
DESIGN AND MANUFACTURING OPERATION (87)**

The analysis, design and manufacturing operation (87), as stated above, includes the (94) input, (95) analysis, (96) design, (97) manufacturing, and (98) transmission procedures of a computerized custom designed appliance manufacturing operation. The steps of those procedures, as outlined above, include the following:

Digitized Input Procedure (94)

The input of digitized information includes the (100) input of patient and doctor identifying information, (200) the input of patient background information, (300) the input of digitized information of the horizontal dimensions of the mandibular teeth and the mandibular bone, (400) the input of horizontal dimensions of the maxillary teeth, and (500) the input of vertical labial-lingual profile information of each of the individual teeth.

(100) Identification Information Input Step:

The first step in the procedure (82), as illustrated in flowchart of Fig. 2A, is (100) to input the doctor-patient identification information 17. This step (100), as illustrated in the detailed flowchart of Fig. 2E, includes the substeps, performed by an operator 28 in response to prompts for text input at a terminal of the computer 30, of (105) input of the doctor's name, (110) input of the doctor's identification

number, and (115) input of the patient's name. Then, the computer 30 (120) assigns a patient identification number. With this information, (125) a patient-specific floppy disk or diskette 34 is automatically formatted.

(200) Patient Background Input Step:

The next step in the information input procedure (94), as illustrated in Fig. 2A, is (200) the entry, in response to prompts, of the patient background information 19, and the prescribed treatment information 27 from the doctor. This step, as illustrated in the detailed flowchart of Fig. 2F, involves the substeps of (205) entering, from the background information 19, the patient's age as numerical data, and selecting (210) the patient's sex and (215) the patient's race from options on the screen. Then, from the prescription information 27, the data are entered, by selecting choices from multiple choice prompts, from information such as the following:

(220) Whether or not the treatment is to include an extraction, and if so, which teeth are to be extracted;

(225) Whether the occlusion type is a group function or a cuspid rise, and if a cuspid rise, whether averages or individual head film is to be used;

(230) Whether the prescribed procedure is to preserve lower intercuspid distance or allow expansion, and if expansion is to be allowed, how much expansion;

(235) Whether or not the occlusion is mutilated;

(240) Whether a Steiner compromise is to be allowed to accommodate skeletal discrepancy;

(245) Whether a Roth or Ricketts insect is to be used on upper laterals, and if so which;

(250) Whether a Roth or Andrews upper lateral overbite is indicated, and if so, which;

(255) Which is the preferred slot size, from traditional sizes 0.018" or 0.022" (0.45 mm or 0.55 mm), or other available size, of which 0.20" (0.50 mm) would often be acceptable;

(260) Whether the case is to be treated with labial or lingual appliances;

(265) Whether the case is to be diagnosed using symmetry or not;

(270) How inter-incisal angle is to be determined, using the Andrews Norms, the Parallel Upper Central to Facial Axis Norm, or Ricketts Norm.

(300) Mandible Digitized Video Input Step:

The forming of the computerized mathematical model of the teeth of the patient 12 begins with (300) the inputting of video or other graphics top view image of the patient's lower jaw, including the teeth, as illustrated in the detailed flowchart of Fig. 2G. Such an image as input by the video scanner 43, is illustrated in Fig. 3.

The step (300) includes the digitizing and processing of the data of the widths of the mandibular teeth and size and shape of the mandibular bone or bone of the lower jaw 22 of the patient 12 from the horizontal plan view of the lower jaw as in Fig. 4. The mandible 22 is composed of hard or cortical bone on the external surface and soft or cancellous bone in the interior. This bone is not as orthodontically alterable as is the maxilla. Since the lower teeth must remain in the mandible, determination of its shape and boundaries is made so that a skeletal arch can be defined to be used as a starting point in the calculation of the finish position of the teeth.

The lower teeth must lie on the mandible 22 in an arch that may be defined as the mandibular trough *MT*, as illustrated in Fig. 4. The roots of the lower teeth of the patient are contained within the mandibular trough *MT*, which is defined as the space between boundaries B_L and B_R of Fig. 4. The outer, or buccal,

and inner, or lingual, boundaries B_s and B_L , respectively, are preferably digitized by interactive selection by the operator 28 from an image 48 of the cortical bone of the mandible 22 on the screen 35. Furthermore, the mandibular teeth must lie in the arch in contact with one another. They each occupy a portion of the arch equal to the distances between their mesial and distal contact points with the adjacent teeth. These tooth extremities are also preferably digitized by interactive selection from the image 48.

To (300) input data of the patient's mandibular teeth and lower jaw 22, as illustrated in the detail flow chart of Fig. 2G, (305) a video graphics image 48 (Fig. 3) of mandibular model 21 is first input to the screen 35 of the computer 30c. Then (310) a grid G is overlaid on the video image of the mandibular 22 as illustrated in Fig. 4. The grid G presents grid lines that intersect the image 48 on the screen. The operator 28 (315) resizes the grid G , if necessary, and orients the image relative to grid G to define X, Y coordinates with a Y axis on a midline ML of the lower jaw 22 and an X axis perpendicular to the Y axis through a selected intersection point or origin $0,0$, preferably set at the mesial contact points of the lower central incisors.

Next, the computer 30 prompts the operator sequentially to select each point, first for the individual tooth contact points, then the jaw bone boundaries. With the pointing device 47, (320) the operator 28 moves the cursor on the screen 35 and selects (e.g., clicks with a mouse on) the prompted point, thereby initiating the software for digitizing the X, Y cartesian coordinates of the mesial and distal extremities $M_{x,r}$ and $D_{x,r}$, respectively, for each mandibular tooth. The mesial extremity $M_{x,r}$ of a tooth is the point on its surface closest the midline ML along the mandibular arch (the mesial direction m) while distal extremity of a tooth is the point on its surface closest the rear of the mouth along the mandibular arch (the distal direction d). From the X, Y coordinates of $M_{x,r}$, M_y and M_r , and of $D_{x,r}$, D_x and D_r , (325) the mesio-distal width MDW , of each tooth I , on each side of the mandible 22, is calculated using Pythagorean theorem:

$$MDW = \sqrt{(M_x + D_x)^2 + (M_r + D_r)^2}$$

where:

M_x is mandibular X coordinate.

M_y is mandibular Y coordinate.

D_x is distal X coordinate.

D_r is distal Y coordinate.

These widths are then summed to calculate the total length MAL required of the arch to accommodate the mandibular teeth. Since all of the teeth will be finally positioned to be in contact with the adjacent teeth, this length remains a constant length of any arch on which the mandibular teeth are placed in the calculations.

Then, by moving the pointing device 47 to the intersections of the lines of the grid G with the visible boundaries B_s and B_L and selecting the intersection points, data is input for determination of the shape of the mandibular trough MT . The point selection function can be made with conventional available CAD/CAM, imaging or illustration software and the pointing device 47. (330) From the selected intersections of the lines of the grid G with the mandible boundaries B_s and B_L , cartesian coordinates $La_{x,r}$ and $Ll_{x,r}$ of labial and lingual limits, respectively, of cortical bone on both sides of mandibular jaw are generated. The X, Y coordinates La and Ll so chosen are digitized as above on the boundary lines B_L and B_s of the cortical bone, between and interproximate the teeth.

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After the points La and Li are chosen representing the cortical bone limits, (335) midpoint coordinates MP_{xy} are calculated between each of the individual labio-lingual pairs of La and Li . Also, calculated are the bone width distances between each of the respective labio-lingual pair DLL , as follows:

$$MP_x = La_x + \frac{Li_x - La_x}{2} ; MP_y = La_y + \frac{Li_y - La_y}{2}$$

$$DLL = \sqrt{(La_x + Li_x)^2 + (La_y + Li_y)^2}$$

where:

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La_x is labial X coordinate of point La .

La_y is labial Y coordinate of point La .

Li_x is lingual X coordinate of point Li .

Li_y is lingual Y coordinate of point Li .

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These midpoints MP_{xy} , one of which is the designated origin $MP_{0,0}$, lie on an arch that describes the size and shape of the center of the cancellous portion of the mandibular bone 22.

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At this point, the beginning of the analysis for the calculation of the finish positions of the teeth is carried out. The coordinates of points MP_{xy} are recalculated relative to a new origin $0,0$ at the calculated midpoint between the mandibular centrals, to normalize the mandibular trough equation to its own independent midpoint when calculated below. The sum of the individual mandibular tooth widths MDW equals the total dental length or mandibular arch length MAL contained in the mandibular trough equation MTE that will be constructed through the points MP_{xy} . MAL is referred to as the arch perimeter.

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At this stage, (340) the midpoints are typically averaged right to left to eliminate any asymmetry that may be present due to slight measurement errors. If, however, the patient has been diagnosed by the orthodontist 14 to be of asymmetrical anatomy, the averaging process is not performed. Such a determination will have been made by the orthodontist 14 in the examination procedure (90) described above and specified of the prescription 27 in step (265) of the procedure (92) described above. An advantage of the averaging process is that, when used, it assists the final positioning of the teeth symmetrically about the midline ML and will make it easier for an archwire to be produced that is symmetrical from right to left, and thus can be made such that it can be installed in inverted orientation.

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The midline ML shown in Fig. 4 is the axis of such symmetry corrections. These corrections for each point MP_{xy} are calculated as follows:

$$S_x = MP_x + \frac{PR_x - PL_x}{2} ; S_y = MP_y + \frac{PR_y - PL_y}{2}$$

where:

30

S_{xy} is the symmetricalized point MP_{xy}

MP_{xy} is mid-point of mandibular trough

PR_{xy} is a point MP_{xy} on the right side

PL_{xy} is the corresponding point on left side of the trough

With the completion of this symmetricalization process, a mathematical equation *MTE*, which describes the size and shape of the mandibular trough according to steps (345), (350) and (355), is derived by fitting a curve to the points $MP_{x,y}$. Preferably, this curve is derived by fitting a series of cubic equations, such as a cubic spline equation, to pass smoothly through the points, for example, through the averaged midpoints $S_{x,y}$. The cubic equations allow the determination of the slope of the curve at each of the midpoints.

The cubic equations are then preferably converted in form to a series of segments of tangent circle equations with slopes equal to the slopes of the cubic spline at the midpoints, and equal to the slopes of the adjacent circle segments at the segment end points, or their points of intersection, along the curve. To fit a cubic equation with quadratics, two circles *CS* and *CL* are used to describe each segment of the *MTE* between midpoints, as illustrated in Fig. 5. This allows a smooth curve consisting of tangential circles to represent the mandibular trough.

The cubic equation calculations are preferably those performed by (345) calculating cubic spline parameters required to pass a smooth curves through symmetricalized midpoints $S_{x,y}$ as illustrated in Fig. 5A. This includes (350) calculating the slope of the cubic spline curve at each symmetricalized mid-point $S_{x,y}$ or $S_{x,y}$, and (355) calculating a series of tangential circle equations whose slopes are equal at the mid-points and at points of intersection along the curve.

(345) The cubic spline method preferred uses a cubic, or third degree, polynomial to interpolate between each pair of data points $S_{x,y}$. A different polynomial is used for each interval, and each one is constrained to pass through the original data with the same slope as the data. (350) The slopes of the cubic equation are computed by solving the slope of a parabola that passes through each data point and its two nearest neighbors points. The cubic spline method is described in more detail in the discussion of the cubic spline subroutine (2000) below.

(355) Any point on the cubic spline equation can now be calculated by using a cubic spline interpolation. Using this, the cubic spline equation is subjected to a circle segment conversion by which the form of the equation *MTE* is converted to a series of circle segments that interconnect tangentially. Once the spline equation is derived, the slopes at each data point are calculated using the point slope method. These slopes are utilized to derive, between each pair of data points on the spline equation, the description of two circle segments, each from one of two circles as illustrated in Fig. 5, to convert the *MTE* to a series of circle segments throughout its length. This facilitates the setup of the teeth, the description of the configuration of archwires, and the generation of NC code for the manufacture of the appliance. The spline-to-circle conversion routine is described in further detail under routine (2100) below.

The input procedure continues. (360) Cartesian coordinates are input for right and left mandibular cuspid cusp tips *CR* and *CL*, respectively, as illustrated in Fig. 4. (365) A distance *DCT* between the cusp tips *CR* and *CL* of the two mandibular cuspids is then calculated:

$$DCT = \sqrt{(CR_x + CL_x)^2 + (CR_y + CL_y)^2}$$

where:

CR_x = right cuspid X coordinate.

CR_y = right cuspid Y coordinate.

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CL_x = left cuspid X coordinate.

CL_y = left cuspid Y coordinate.

This information is used to calculate if and how much the mandibular intercusp distance is to be altered, and to evaluate whether the calculated final position is acceptable. Similarly, (370) cartesian coordinates of right and left mesio-buccal cusp tips, MR and ML , respectively, of mandibular first molars are calculated, and (375) the distance between these points DMT is calculated:

$$DMT = \sqrt{(MR_x + ML_x)^2 + (MR_y + ML_y)^2}$$

where:

MR_x = right first molar cusp X coordinate.

MR_y = right first molar cusp Y coordinate.

ML_x = left first molar cusp X coordinate.

ML_y = left first molar cusp Y coordinate.

This information is used to determine if and how much the mandibular intermolar distance is to be altered.

(400) Maxilla Digitized Video Input Step:

As with the mandibular jaw information described in connection with Fig. 4, (400) a computer image is made from input in the same manner from the upper model 23 of the maxillary jaw 24 of the patient 12, as illustrated in the flowchart detail of Fig. 2H. This involves the substeps of (405) inputting a video image 48a of maxillary model 23 to the computer screen 35. The image 48a is illustrated in Fig. 4A. With the maxilla, it is not necessary to overlay the grid G on maxillary image on the screen, since the bone of the maxilla is a variable that will be altered orthodontically to accommodate the finish positions of the teeth. The orientation of the axes and position of the origin are immaterial to the calculation of the relative distances such as MDW of the teeth. Only the scale must be maintained. As with the mandibular information, the image of the maxillary jaw 24 is displayed at a scale predetermined by the scanner 33. The scale is involved in the calculation of the maxillary tooth widths MDW .

(420) Cartesian coordinates of mesial and distal extremities M_x and D_x of each maxillary tooth are then input as with the mandibular teeth and (425) the mesio-distal width MDW of each maxillary tooth is calculated using Pythagorean theorem, thus:

$$MDW = \sqrt{(M_x + D_x)^2 + (M_y + D_y)^2}$$

where:

M_x is mesial X coordinate.

M_y is mesial Y coordinate.

D_x is distal X coordinate.

D_y is distal Y coordinate.

This information is used first to determine whether the maxillary and mandibular teeth are correct in proportion to the mesiodistal widths MDW of the other. If the proportions are incorrect, a tooth size discrepancy TDS is said to exist, and the information is recorded to report to the orthodontist. The MDW 's of the maxillary teeth are later used to place the maxillary teeth upon the mandibular arch.

Next, (430) coordinates of the central fossae of right and left maxillary first molars are input. Then, (435) the distance between central fossae *DCF* is calculated as follows:

$$DCF = \sqrt{(R_x + L_x)^2 + (R_y + L_y)^2}$$

where:

R_x is right side central fossa *X* coordinate.

5 *R_y* is right side central fossa *Y* coordinate.

L_x is left side central fossa *X* coordinate.

L_y is left side central fossa *Y* coordinate.

This information is recalculated after the tooth finish positions are calculated to coincide with the *DMT* spacing of the mandibular first molars, and compared with this initial measurement as an indicator of whether the intermolar width will be changed by treatment and the amount of such change, if any.

10 (500) Digitized Probe Tooth Profile Input Step:

The next input step (500) involves an analysis of the dentition, as illustrated in the detailed flowchart of Fig. 21. In this step, selected profiles of each of the teeth are generated from either the model 20, or from a digitized three dimensional representation of the patient's teeth or the model 20 as illustrated in Figs. 3A and 3B. In the illustrated embodiment, the use of the probe assembly 57 of Fig. 1C is used in this step.

Where the full three dimensional scan has been employed in step (300), as could be produced with the use of the laser image generator (Fig. 1B), or as could be produced with moire image generator or other technique, a digitized computer model is produced. From such a computer model, which is an electronic version of the model 20 in the form illustrated in Figs. 3A and 3B, planes or other cross-sections through the teeth are selected that contain extremities of the teeth. The three dimensional images may be displayed on the screen 35 and profiles generated either with the pointing device 47 in a manner similar to the use of the mechanical probe described below, or automatically using available CAD or illustration imaging software. Whether the profiles are generated from a physical model 20 or an electronic version thereof, much of the input step (500) and/or the landmark selection step (600) may be similarly employed.

25 In the preferred use of the information from the probe assembly 57, a single digitized profile curve *PF* is constructed for each tooth in a generally vertical plane extending in an approximately labial-lingual orientation generally along the central developmental lobe perpendicular to the marginal ridges. While other profiles can be taken, the need to do so is reduced by intelligent plane selection made with an understanding of tooth anatomy, depending on the data required by the tooth positioning and appliance design criteria employed. The selection of the profile plane is illustrated in Fig. 6 where a first profile *PF_A* through the center of the tooth is shown as missing the buccal cusp tip which is the maximum crown highpoint of the tooth. Profile *PF_B* is then selected to include the buccal cusp, and the ridge of the profile is found to generally align with the lowpoint of *PF_A*. Alternatively, the profile may be non-planar to pick the important features of both planes. As such, the profile produced will be comparable to a projection onto a plane of the relevant tooth extremities.

30 The step (500) of analysis of the dentition includes, first (505) examination, by the operator 28 of the computer 30a, of the marginal ridges of the upper central and upper lateral teeth. If ridges are excessive, a determination is made to take a profile twice with the probe 60, once by smoothing the teeth, for example

with wax, for arch coordination and once without smoothing for placement jig geometry. Otherwise, a single profile taken across the buccal cusp will contain information of the crown height of the tooth as well as approximating the profile of the tooth through its mesiodistal center with accuracy that is usually sufficient. Then, (510) a determination is made as to whether one or two traces of maxillary incisor teeth are to be input as in step (505) above.

(515) The computer 30a is configured to receive sequential cartesian coordinate pairs through an RS-232C serial port representing tooth profile anatomy from the orthogonally positioned displacement transducers 61. (520) The computer 30a prompts the operator 28 to enter the profiles of each tooth sequentially. In response to the prompts, data points of each tooth are input, beginning with lower left molar $T(B,L,6)$ and ending with upper right molar $T(U,R,6)$, and a display 63 of profile PF_i image is generated. The output circuits associated with the transducers 61 are configured to digitize data values at periodic time intervals as the probe 60 is moved across the teeth from the time the probe first starts to move across the tooth until the operator enters a command or key stroke indicating that the scan is complete. Then (525) the input profile data of each of the teeth is stored in memory by the computer 30. The resulting profiles PF_i are illustrated in Fig. 3C. These profiles, at this stage, are not related to the positions of the teeth within the mouth or with respect to other teeth. Thus, each of the X-Y coordinates of the individual tooth profiles are independent of each other. In step (600) below, the coordinate axes of each tooth will be oriented with respect to each other, and thereafter, in later steps (800)-(1100), the coordinates of each profile are translated vertically for proper occlusion and horizontally for placement on their respective arches.

(95) Analysis and Finish Tooth Position Calculation Procedure

The calculation of the finish positions of the teeth, as illustrated in the flowchart of Fig. 2B, includes (600) determining the relative positions of geometric landmarks on the surfaces of the teeth and establishing the axis inclinations of the teeth, (700) calculating cuspid rise, (800) initially positioning the mandibular teeth vertically and in relation to the mandibular trough, (900) calculating a best fit cusp tip equation for the mandibular teeth, (1000) calculating the finish positions of the mandibular teeth on the best fit equation, and (1100) calculating the finish positions of the maxillary teeth on three arches related to the best fit equation.

(600) Tooth Landmark Identification Analysis Step:

After the individual teeth have been digitized, the inputting of tooth shape data (94) is complete, with the digitized information 26 stored a file. Then, referring again to the flowchart of Fig. 2, (95) the input data 26 is analyzed to develop or derive further parameters for calculating the final positions of the teeth and for (96) the design of the appliance 25. In the tooth positioning analysis (95), as illustrated in the flowchart of Fig. 2B, (600) a tooth profile analysis is made in which, for example, certain anatomical landmarks are chosen, depending on the tooth to be analyzed. The details of the tooth profile analysis are illustrated in the flowchart of Fig. 2J.

In the tooth profile analysis step, (605) individual images 63 of the profile curves PF_i of each tooth (Fig. 3C) are recalled separately to the screen of the computer 30b for selection of the landmarks.

Using the displayed images 63 of the profile curves PF_i , (610) specific landmark points are chosen, first on the mandibular molars and bicusps. The selected points are digitized as illustrated in Fig. 6. The selected points are:

- Point P_l : The Lingual (tongue side) gum/tooth intersection.
- Point P_c : The prominence of the lingual cusp.

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Point P_2 : The prominence of the buccal (check side) cusp.

Point P_4 : The buccal gum/tooth intersection.

From these landmarks, (615) the crown long axis *CLA* of each molar and bicuspid profiled is determined. The determination is made by constructing a first line L_1 between points P_2 and P_3 and a second line L_2 between points P_1 and P_4 . The crown long axis *CLA* of a tooth is the line between the midpoints of L_1 and L_2 .

Line L_1 is constructed through point P_2 and point P_3 by the following equation:

$$\frac{Y - Y_2}{X - X_2} = \frac{Y_3 - Y_2}{X_3 - X_2}$$

where:

$X_2, Y_2 = X$ and Y coordinates of point P_2 .

$X_3, Y_3 = X$ and Y coordinates of point P_3 .

Line L_2 is constructed through point P_1 and point P_4 by the following equation:

$$\frac{Y - Y_1}{X - X_1} = \frac{Y_4 - Y_1}{X_4 - X_1}$$

where:

$X_1, Y_1 = X$ and Y coordinates of point P_1 .

$X_4, Y_4 = X$ and Y coordinates of point P_4 .

A point equidistant between points P_2 and P_3 along line L_1 is then calculated and defined as P_{2-3} :

$$P_{2-3_{x,r}} = \frac{X_2 + X_3}{2} ; \frac{Y_2 + Y_3}{2}$$

where:

$X_2, Y_2 = X$ and Y coordinates of point P_2 .

$X_3, Y_3 = X$ and Y coordinates of point P_3 .

A point equidistant between points P_1 and P_4 along line L_2 is also calculated and defined as the Gingival Center Point *GCP*:

$$GCP_{x,r} = \frac{X_1 + X_4}{2} ; \frac{Y_1 + Y_4}{2}$$

where:

$X_1, Y_1 = X$ and Y coordinates of point P_1 .

$X_4, Y_4 = X$ and Y coordinates of point P_4 .

The line defining the crown long axis *CLA* is constructed using the following equation:

where:

$X_{2-3}, Y_{2-3} = X$ and Y coordinates of the center point P_{2-3} .

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$$\frac{Y - Y_{2-3}}{X - X_{2-3}} = \frac{Y_{GCP} - Y_{2-3}}{X_{GCP} - X_{2-3}}$$

X_{GCP}, Y_{GCP} = X and Y coordinates of gingival center point $GCP_{X,Y}$.

For molars and bicusps, point P_1 , the buccal cusp tip, is defined as the Incisal Center Point ICP .

Similarly, (610) the anatomical landmarks and crown long axis CLA for the mandibular cuspids, laterals and central teeth are determined, as illustrated in Fig. 6B. The points P_1 through P_4 , as labeled in Fig. 6B, are selected as follows:

Point P_1 : The lingual gum/tooth intersection.

Point P_2 : The lingual aspect of the incisal edge.

Point P_3 : The buccal aspect of the incisal edge.

Point P_4 : The facial gum/tooth intersection.

As with the bicusps and molars, lines L_1 and L_2 are constructed. The landmarks in the cases of the teeth as illustrated in Fig. 6B, are chosen because they are relatively tolerant to operator error in selection. This can be seen by the set of broken lines that are possible alternatives to L_1 in Fig. 6B. From these landmarks (615) the crown long axis CLA is determined as defined above, by connection of the midpoints of L_1 and L_2 .

The next step in the analysis is the determination of maxillary dentition for each upper molar and bicuspid. (610) Anatomical landmarks are identified and chosen as illustrated in Fig. 6C, which requires (612) the selection of a fifth point, P_5 , defined as follows:

Point P_1 : The lingual gum/tooth intersection.

Point P_2 : The prominence of the lingual cusp.

Point P_3 : The prominence of the buccal cusp.

Point P_4 : The buccal gum/tooth intersection.

Point P_5 : The mesial marginal ridge of the tooth at central groove.

Referring to Fig. 6C, from the landmarks, (615) the crown long axis CLA of each applicable maxillary tooth is determined.

The (610) anatomical landmarks for the maxillary cuspids, laterals and central teeth are determined as illustrated in Fig. 6D. The points labeled P_1 through P_4 are selected, as follows as illustrated in Fig. 6D:

Point P_1 : The lingual gum/tooth intersection.

Point P_2 : The lingual aspect of the incisal edge.

Point P_3 : The buccal aspect of the incisal edge.

Point P_4 : The facial gum/tooth intersection.

From each of these sets of landmarks, the crown long axis CLA of each such tooth is also determined as described (615) above.

This completes the loop (620) for all of the teeth.

Next, as further illustrated in Fig. 6D, (620) seed values for setting the crown long axis inclinations LAI of the teeth. Initially, such seed values may be derived from analyses that identified the facial axis plane FAP through the facial axis point FA of the tooth (the midpoints of the height of the clinical crowns along the facial axes of the clinical crowns) as described by Dr. Lawrence Andrews. It is, however, contemplated

that *CLA* seed values for various population groups will be statistically derived in the course of the practice of the present invention, and will produce improved treatment results.

The seed values shown in Table 1 below are typical for caucasian males. These seed values for tooth *LAI*, tabulated in degrees from the horizontal lingual (-X) axis, will vary to reflect known variations due to such things as sex,

The preferred seed values are shown in Table 1 below are typical for caucasian males. These seed values will vary to reflect known variations due to such things as sex, race or treatment plan.

Tooth Type	Maxillary Crown <i>LAI</i>	Mandibular Crown <i>LAI</i>
Central	117	107
Lateral	112	107
Cuspid	108	100
1 st Bicuspid	94	83
2 nd Bicuspid	94	80
1 st Molar	x	x
2 nd Molar	x	x

TABLE 1

The computer images as summarized in Fig. 3C for each tooth (630) are then rotated so that the *CLA* is oriented at the angle *LAI*, the long axis inclination angle, to the mandibular trough plane *MT* according to the values in Table 1. This computes the final inclinations of the teeth that will be preserved in the calculations below. This produces the oriented profiles *PF* summarized in Fig. 6E.

In the analyses of Andrews referred to above, the *LAI*s were established with a line L_{PA} drawn tangent to the facial surface at *FA*, and line representing the relative inclination of the archwire plane drawn through *FA* point. The angle between the lines was established at the inclinations reported by Andrews for patients with no skeletal discrepancies. The angle *LAI* between the crown long axis *CLA* and a line representing the maxillary arch plane in which lies the mandibular trough equation *MTE* is related to the facial inclination angles of Andrews' studies by taking into account statistically the thicknesses and contours of the teeth. Table 1 above was derived, after statistical processing, to produce the seed value used for the final inclination of the crown long axis in preferred occlusal design.

Once the tooth profiles have been rotated to the inclination angles *LAI*, certain precise vertical dimensions and extremities can be determined. From the digitized profile curves, which are stored in memory in the form of a series of closely spaced points, the precise incisal tip *IC*, as illustrated in Figs. 6F, 6H and 6I, are identified on the cuspids, laterals and centrals.

Additionally the elevation of the marginal ridge *P₂* is identified. The marginal ridge elevation *MRE*, which is the vertical distance from *P₁* to *P₂*, is identified on the maxillary posterior teeth because they are the centric stops for the buccal cusps of the mandibular molars and bicuspids. In other words, point *P₂* on the mandibular molars and bicuspids contacts point *P₂* on the maxillary molars and bicuspids when the teeth are together, as illustrated in phantom line *PH₂*, in Fig. 6C. For a more precise placement in a less common

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case where the maxillary ridge is narrow in relation to the mandibular tip (phantom line *PH*), a more detailed three dimensional analysis of the tooth shape can take into account additional correction needed. The calculation of *MRE* (Fig. 6C) is made after rotation of the teeth to their proper *LAI* inclinations so that *MRE* will be a vertical distance, where *LAI* is measured relative to the plane of the dental arch. The *MRE* is used as the buccal cusp height *BCH* in the calculation of cuspid rise and archwire plane placement as described below in the discussion of Figs. 7A and 8, respectively.

(700) Cuspid Rise Determination Step:

The next step of the analysis procedure (87) is (700) the calculation of cuspid rise, illustrated in detail in the flowchart of Fig. 2K.

Most orthodontists currently desire a cuspid rise occlusion, in which, in lateral movement of the lower jaw, the cuspids cause the other teeth to disclude or to come apart. In order for this to happen, the overlap of the cuspids must be greater than that of the other teeth when the teeth are together. This is complicated by the fact that the cuspids ($I=3$) are close to the front of the mouth and are therefore further from the condyle or pivot point *PP* of the jaw than are the posterior teeth ($I>3$), as illustrated by distances *DJ*, in Fig. 7. This results in the teeth closer to the back of the mouth moving less than the cuspids on opening. This differential rate of movement must be included in the calculation of cuspid rise or the back teeth will remain in contact after the cuspids have cleared each other. Also, the distance *DPP* from the occlusal plane to the pivot point *PP* of the condyle of the jaws must be considered, as illustrated in Fig. 7. A failure to provide for this distance results in what is known as working interferences.

According to the preferred embodiment of the present invention, where cuspid rise is prescribed to control occlusion, the contribution of cuspid rise is distributed between the maxillary and mandibular cuspids, with two parts of the cuspid rise provided by the maxillary cuspids and one part by the mandibular cuspids. This distribution is applicable where occlusion is solely to be a cuspid rise function. Where occlusion is to be a group function, as specified by the orthodontist 14 in the prescription 27, the distribution between the upper and lower teeth is generally equal.

In the substeps performed in the calculation of the cuspid rise (700), illustrated in detail in the flowchart of Fig. 2K, the first substep is (705) to acquire the initial vertical distance or buccal cusp height *BCH* from *P*, to the marginal ridge for each of the right and left maxillary first bicuspid *T(U,4)*, second bicuspid *T(U,5)*, first molars *T(U,6)*, and second molars *T(U,7)*, as illustrated in Fig. 6C. This is the marginal ridge elevation *MRE* calculated for each of these teeth in substep (615) of step (600). Then, from anatomical study, (710) the cuspid rise vertical height *CR* required to clear each respective pair of teeth is determined by first computing the values in Table 2, which are derived from the jaw dimensions *DPP* and *DJ*, in Fig. 7. required to clear each respective pair of teeth is determined by first computing the values in Table 2.

$$\begin{aligned}
 &1.67 \times BCH \text{ of } T(U,7) \\
 &1.50 \times BCH \text{ of } T(U,6) \\
 &1.36 \times BCH \text{ of } T(U,5) \text{ and} \\
 &1.20 \times BCH \text{ of } T(U,4).
 \end{aligned}$$

TABLE 2

Then, (715) from the products of the buccal cusp height *BCH* for each such tooth multiplied by the rise factor listed above, the largest value is selected. This selected product is the cuspid rise required to clear

the most prominent cusp and provide group function occlusion. This is illustrated as *BCH*, in Fig. 7A for the case where the first molars are the last to clear.

(720) If the group function has been selected in the prescription 27 provided by the orthodontist 14, the calculated rise is used as is. If cuspid guidance has been selected in the prescription 27 of the orthodontist 14, the calculated cuspid rise factor must further be modified to give typically 0.5 to 0.75 mm of clearance over the largest rise factor by multiplying the buccal cusp height *BCH* for each tooth by the rise factor listed above and selecting the largest figure, then adding 0.5 to 0.75 mm additional cuspid overlap to obtain an adjusted cuspid guidance cuspid rise.

(725) Calculation of cuspid overlap or cuspid rise *CR* for maxillary and mandibular cuspids is preferably as follows: If group function has been selected, mandibular rise equals 50% total group function rise, and maxillary rise equals 50% of the total group function rise. If cuspid function has been selected, mandibular rise equals 34% of the total cuspid guidance rise, and maxillary rise equals 66% of the total cuspid guidance rise.

(800) Mandibular Tooth Placement Step:

The next step in the analysis procedure (87) is (800) the mathematical construction of the mandibular occlusion to calculate the position of the mandibular teeth. The details of this step are illustrated in the flowchart of Fig. 2L. The first calculation places the tips of the mandibular teeth on an occlusal plane pending final refinement of the placement, as diagrammatically illustrated in Fig. 6E. In this step, the inclinations of the mandibular tooth crown long axes *CLA* are preserved, and the teeth are moved upward along their *CLA*'s until their tips are in alignment with the plane of the top of the tallest tooth. The *CLA*'s are placed to intersect the *MTE* below the tooth *GCP*. Because the teeth are inclined at different *LAIs*, or long axis inclination angles, the tooth tips will each be differently offset from the *MTE*, and thus not in a smooth arch.

The substeps of the mandibular placement step (800), illustrated in the flowchart of Fig. 2L, are as follows:

(805) The tallest mandibular tooth, with the exception of the cuspids, is identified. In Fig. 6F this is illustrated as the left mandibular central. The tallest tooth is the tooth with the greatest crown height *CH*. The crown height *CH* is the distance, in the *Y* direction (with the teeth profiles oriented as described in step (600)), from the *GCP*, the point of intersection of line *L₂* and crown long axis *CLA*, to highest point on buccal cusp, e.g. *P₂* (for posterior teeth) as illustrated in Fig. 6F and (for the anterior teeth) to either the incisal center point *ICP* or, preferably to the incisal tip *IC*, as illustrated in Fig. 6G. The crown height *CH* of the tallest tooth, shown as the left mandibular central incisor in Fig. 6F, is the maximum crown height *MCH* of the mandibular teeth.

Then, (810) three parallel planes are established:

a) an *MCH* reference plane *MCHP* parallel to the *X*-axis, and passing through an origin *0,0*, set at the *GCP* of the tallest tooth (Figs. 6F and 6I);

b) a Buccal Cusp Plane *BCP* parallel to *X*-axis and passing through coordinates *0, MCH* on the tallest tooth (Figs. 6F and 6I); and

c) a Cuspid Rise Plane *CRP* parallel to *X*-axis and passing through coordinates *0*, where *CR* is the cuspid rise calculated in step (700), where the cuspid rise option has been selected.

With the planes defined, (815) the oriented mandibular teeth are placed such that the highest point on buccal cusp tip P_3 or incisal tip IC of each contacts the buccal cusp plane BCP , for all teeth except the cuspids, as illustrated further in Fig. 6F. The BCP thereby is established as the occlusal plane MOC . The reference plane $MCHP$ is set equal to the plane of the mandibular trough MT . This sets the GCP of the tallest tooth on the MT , with the GCP 's of the remaining mandibular teeth above it. It also sets the occlusal plane MOC a distance MCH from the mandibular trough MT . The absolute highest point on a tooth crown is preferably used to align the teeth with the BCP . Such a point can be determined by additional point selection in step (500), such as by the direct selecting of the point IC for the precise incisal tip, or preferably by calculating the highest point directly from the profiles of Fig. 3C or from three dimensional images as in Figs. 2A, 2B after rotation of the teeth to their final inclination angles LAI , at the end of step (600).

The next stage in this step is to establish the mandibular component of cuspid rise. This involves (820) vertically moving the cuspids by, for example, sliding the cuspids along their crown long axes, such that the cuspid cusp tips are at the appropriate height above the mandibular occlusal plane, that is, in the plane CRP .

At this stage, the vertical positions of the mandibular teeth relative to each other are calculated, providing a basis for relating the Y coordinates of the individual mandibular tooth profiles with respect to each other as illustrated in Figs. 6F and 7C.

Then, with the mandibular teeth vertically positioned, the teeth are horizontally set at temporary positions with respect to the MTE , which lies in the plane of the mandibular trough MT ($MCHP$). This horizontal positioning, in effect, relates the X axes of the individual tooth profiles in a horizontal in-out direction with respect to the mandibular arch and special mesiodistally along the mandibular arch.

Because the preferred goal, however, is to position the tips of the teeth in the smoothest arch in an occlusal plane MOC rather than their gingival aspects in a smooth arch at the mandibular trough MT , (825), a horizontal distance $OFFSET$ for each tooth is calculated, based on the tooth and the crown long axis inclination LAI determined in step (600). This offset is the horizontal distance from the MTE to the tooth tips when their GCP 's are placed on the MTE .

For mandibular centrals and laterals and cuspids, the $OFFSET$ is calculated by dividing, by the tangent of LAI , the vertical distance from (1) the intersection of crown long axis CLA and the incisal tip IC to (2) the intersection of CLA and maximum cusp height reference plane $MCHP$. The vertical distance may be calculated from the IC to the $MCHP$ (equal to the Y coordinate of point IC , producing the incisal center vertical distance ICD .) For mandibular laterals and centrals, ICD equals MCH . For mandibular cuspids, ICD equals the mandibular cuspid rise component, which is $MCH + (Total CR)/3$ when cuspid rise function occlusion has been selected. The calculation of the $OFFSET$ for centrals, laterals and cuspids would thus be as follows for the incisors and laterals:

$$OFFSET = ICD / \tan(LAI)$$

(831) For mandibular bicuspid and molars, referring to Fig. 6F, the $OFFSET$ is calculated as the horizontal distance from point P_3 to the intersection of the CLA and the $MCHP$ as follows:

$$OFFSET = [MCH / \tan(LAI)] + HD$$

where HD equals the horizontal distance from point P_3 to incisal center point ICP .

Then, (835) the mandibular trough placement point $MTTP$ is defined as the intersection of $MCHP$ and CLA , as illustrated in Figs. 6G and 6H. For the tallest tooth, $MTTP$ is its GCP , as illustrated in

Fig. 6I. The *MCHP* is at the level of the mandibular trough and contains the *MTE*. The *MTPP* is the point on the tooth that is initially placed on the *MTE*.

Next, referring to Fig. 7B and 7C, the teeth are placed with their *MTPP*'s on the mandibular trough, one side at a time. To achieve this, (840) the subroutine (2200) is called twice, once for the left side, and
 5 once for the right side, as follows:

The mandibular trough equation *MTE* is first adjusted for the mandibular centrals to increase the radii by the amount of the central *OFFSET* for that particular tooth, as defined above, to form a mandibular trough offset curve *MO(I)* of Fig. 4B. The radii of the *MTE* referred to are those of the *MTE* defined in the circle segment form of the equation generated in step (300) with the spline to circle conversion routine
 10 (2100). Since the *OFFSET*'s of the teeth differ, the *MO* may be viewed as a discontinuous equation when constructed in this manner, made up of segments, each containing the tip of one tooth and spaced labial-lingually from the *MTE* by the amount of the individual tooth's *OFFSET*.

Beginning with the left side, the central is placed, as illustrated in Fig. 7B, by placing its mesial contact point *MCP* at the intersection of the midline *ML* with the offset curve *MO* for the tooth. This has
 15 the effect of the placing *MTPP* of the tooth, which is the intersection of the *CLA* with the *MCHP* or *MT*, on the *MTE* and the incisal tip *IC* of the tooth on *MO*. The tooth placement on the circle segment form of an equation is explained in detail in the description of the tooth placement routine (2200) below. In the placement of the central, a circle *C₁* is constructed with a radius equal to the mesiodistal width *MDW*, of the central tooth and with the center of the circle *C₁* at the mesial contact point *MCP* of the tooth at intersection
 20 of the midline *ML* with the offset curve *MO*. Then, circle *C₂* is constructed with a radius equal to *MDW/2* and with its center coincident with the center of circle *C₁*. Then, the intersections of trough offset curve *MO* with the circles *C₁* and *C₂* are found, its intersection with the circle *C₁* being the distal contact point *DCP* of the tooth and its intersection with the *C₂* being the tooth midpoint *TMP* of the central tooth. The tooth midpoint *TMP* is here defined as the midpoint of the mesiodistal width of the tooth placed on an archform,
 25 which is the intersection of the archform with a vertical labial-lingual plane that contains the *CLA*. This midpoint *TMP* of the central tooth on the *MO* is the approximate position of the incisal tip *IC*.

Determining the intersections of the circles with the offset trough curve *MO*, or expanded mandibular trough, requires identification of which circle sector lines (Fig. 5) the circles *C₁* and *C₂* intersect. These are
 30 identified by comparison of the *X* coordinates of the intersections with the *X* coordinates of the distal contact points *DCP* of each of the central teeth to determine which segments of the trough equation will be used, as explained more fully in the description of the tooth placement routine (2200) below.

Finally, a distal contact point line *DCPL* is constructed for the central tooth through the *DCP*, at the intersection of circle *C₁* with the *MO*, and through the center of the identified circle segment of the *MO*, the expanded *MTE*, on which the *DCP* of the tooth lies. This line lies along a radius of the circle segment of
 35 the *MO* curve through the distal contact point of the central tooth. Similar lines *DTMP* are constructed for the center of the tooth *TMP*.

(845) For each of the remaining mandibular teeth on the same side of the arch, in distal sequence, a new mandibular trough offset *MO*, is calculated, by expanding the *MTE* with radii of curvature increased by the amount of the next tooth's *OFFSET* and with center of the circles *C₁* and *C₂* moved labially or
 40 outwardly from the *MTE* along the prior tooth's distal contact point line *DCPL* by the amount of the current tooth's *OFFSET*. This is the *MCP* for the next tooth. Circle *C₁* for the tooth is constructed with a

radius equal to the mesiodistal width of the tooth and with its center at their center point *MCP*. Circle *C₂* is constructed with a radius equal to *MDW/2* and with centers coincident with circles *C₁*.

For bicuspid and molars, the tooth midpoints *TMP* can be considered as their points *P_j*. Then, as with the central, the intersections of *MO* and circles *C₁* and *C₂* are calculated for these teeth. The distal contact points *DCT* of these teeth are at the intersections of *MO* for the tooth and the respective *C_j*s. The centers of the teeth *TMP* are at the intersections of *MO* for the tooth and the respective circles *C_j*. The *MO* sector segments which the circles intersect are identified. Selection of the segments is made by comparing the *X* and *Y* coordinates of intersections to *X* and *Y* coordinates of distal contact points *DCPs*. Finally, a distal contact point line *DCPL* is constructed from selected segment center to the plane *DCP*. The same is done for the centers of the teeth *TMP*.

(848) The substeps (842) are repeated for all of the remaining mandibular teeth on the same side of the arch. Then, (849) substeps (840)-(848) are repeated for the teeth on the opposite side of arch.

(900) Best Fit Mandibular Arch Equation Step:

The above step (800) leaves the crown long axes *CLA* of the mandibular teeth intersecting the *MCHP* reference plane, which is at the level of the mandibular trough *MT* at or just below the gingival center points *GCP* of the teeth, along the mandibular trough equation *MTE*. The discontinuous offset equation *MO*, however, contains the approximate tips of the teeth in the occlusal plane *MOC*, with the teeth irregularly offset as represented by the discontinuous *MO* lines in Fig. 4B. To place the tips of the teeth into an ideal arch, (900) a final equation for better placement of the buccal cusp tips and incisal edges of the mandibular teeth in a continuous arch is developed. The development of the best fit equation is illustrated in the detailed flowchart of Fig. 2M.

When viewed perpendicularly to the occlusal plane as in Figs. 4B and 7B, it can be seen that the buccal cusp tips and incisal tips of all of the individual teeth do not lie along either the mandibular trough equation or the same geometrical expansion of that equation. In fact, due to small anatomical variations, it is unlikely that the tips will fall on any smooth curve when the tooth *CLAs* intersect a smooth curve at the mandibular trough in the *MCHP* and the *LAIs* are preserved. To remedy this, the equation is statistically developed that best fits the cusp tips and incisal edges of the individual teeth; a Best Fit Buccal Cusp Equation *BFBCE*. In the formulation of the equation, the coordinates of the right and left tooth midpoints *TMP*, the *ICPs* or *ICs* in Fig. 7B, are preferably averaged. The equation *BFBCE* may be obtained (910) by use of polynomial or other bezier or least square statistical techniques to arrive at a best fit equation. These are available in any of a number of off-the-shelf software packages.

Such a *BFBCE* equation is plotted in Fig. 4B. Once the *BFBCE* is determined, it may be (915) converted to a circle segment equation in a manner such as with the spline to circle conversion routine (2100). This equation provides a basis for moving the teeth labially or lingually from the discontinuous offset equation *MO* to place the tips of the mandibular teeth in a smooth arch in the occlusal plane *CP*, as illustrated in Fig. 7C. To do this, in the next step the profile planes will be translated bodily in their own horizontal *X*-directions (which is an *X-Y* movement in the coordinates of the horizontal planes), moving their *MTTPs* off of the *MTE* in the *MCHP* (or *MT*).

(1000) Mandibular Best Fit Arch Placement Step:

After statistically deriving a best fit equation *BFBCE*, (1000) positions of the individual mandibular teeth are calculated to translate then facially, either labially or lingually, so that their tips fall on the best fit curve. This step is illustrated in detail in the flowchart of Fig. 2N.

To achieve this, (1005) the mesiodistal contact point of the mandibular central, the point *MCP*, as in Fig. 7B, is first placed on the intersection of the midline *ML* with the *BFBCE* in the same manner as it was placed on the *MO* in step (800). Then (1010) circles *C1* and *C2*, as defined above, for the tooth are constructed and their intersections with the *BFBCE* curve are found. As with the placement in step (800) above, the intersection of *C1* with *BFBCE* is the distal contact point *DCP* of the tooth, and the intersection of *C2* with the *BFBCE* curve, is the center point *TMP* (which aligns with *IC*) of the tooth. This, in effect, moves the tooth normal to the circle segment of the *BFBCE* associated with the *TMP*. Then, (1015) new circles *C1* and *C2* are constructed with centers at the distal center points *DCP* and (1020) substeps (1005) and (1015) are repeated for all teeth on the same side of the mandibular arch. Then, (1025) steps (1005) through (1020) are repeated for the teeth on the other side of the mandibular arch. The placement uses the tooth placement routine (2200), the description of which below explains in detail the placement of the mandibular teeth on the *BFBCE*.

This step bodily translates the teeth in a generally horizontal direction, and rotates the teeth of the mandible about their *CLAs* to place incisal edges and cusp tips, as determined in step (800), on the *BFBCE*. With the completion of this step the finished positions of the mandibular teeth are calculated and the mandibular occlusion is finalized. At this point the mandibular occlusion can be envisioned as an ideal setup cast in stone, to which the maxillary occlusion will be fitted and related.

The finish positions of the mandibular teeth are illustrated in Fig. 7C in which the *X-Y* coordinates are those of the horizontal arch planes. A vertical *Z* coordinate, perpendicular to the horizontal *X-Y* plane, is aligned with the *Y* axes of the individual tooth profile planes. The *X* coordinates of the profile planes are aligned with the labial-lingual directions *La-Li* in Fig. 7B.

(1100) Maxillary Tooth Placement Step:

The construction of occlusion requires (1100) the fitting of the maxillary teeth to the already positioned mandibular teeth. This is accomplished by deriving a modified best fit buccal cusp equation *BFBCE* for the maxillary teeth in the step illustrated in detail in the flowchart of Fig. 2O. Unlike with the mandibular teeth, with the maxillary teeth, the cusp tips of the posterior teeth and incisal edges of the anterior teeth are not set in a single arch. The maxillary teeth are rather set: (1) with the central groove-marginal ridge points of the maxillary bicusps and molars on the *BFBCE*, (2) with the maxillary anteriors spaced labially off of the *BFBCE* to allow for incisal overlap and a clearance between the lingual surfaces thereof and the labial surfaces of the mandibular teeth, and (3) with the cuspid tips in the arch generally between the first maxillary bicuspid and the lateral incisor. The arches on which the maxillary teeth are placed as illustrated in Fig. 4C, as explained above.

For the maxillary incisors, the modification of the *BFBCE* first involves an averaging the distances from point *P1* to point *P2* on the mandibular incisor incisal edge, and dividing by two, to locate the arch that will contain the labial surface of the tooth adjacent the incisal center point *ICP* of the tooth, which is generally the point *P2*. This produces a uniform distance from the best fit equation to the contact point of the facial surface on the labial side of the mandibular anterior teeth with the facial point on the lingual side

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of the maxillary anterior teeth. An additional distance, of typically one-quarter millimeter, is added to the averaged distance to provide a slight *Clearance* between the upper and lower anterior teeth. This is illustrated in Fig. 7D.

The maxillary anterior dentition is set for vertical position relative to the occlusal plane *MOC* according to occlusion criteria selected to provide a predetermined overlap. From the cuspid rise calculation of step (700), the vertical positions of the maxillary cuspids are known relative to the mandibular occlusal plane *MOC*. For maxillary laterals and centrals, the vertical positions provide the overlaps according to the prescribed criteria, putting their lingual facial contact points with their mandibular counterparts on the *MOC* plane. All teeth are inclined at the prescribed crown long axis *CLA* inclination values *LAI* from Table 1 in step (600).

In the (1100) placement of the teeth of the maxilla, or upper jaw 24, with respect to those of the mandibular, or lower jaw 22, (1105) three arch forms are mathematically defined. These are (1106) the maxillary anterior arch form *MAAF*, (1110) the central groove marginal ridge arch form *CGMRAF*, and (1115) the maxillary cuspid arch form *MCAF*, as illustrated in Fig. 4B. The *MAAF* is established to position the maxillary incisors with respect to the *BFBCE* so that their lingual faces contact or clear the labial faces of the mandibular incisors. The *CGMRAF* is established separate from the *MAAF* because the maxillary bicuspid and molars contact their mandibular counterparts with their central groove marginal ridge intersection points juxtaposed on the mandibular buccal cusps. The *MCAF* is established separate from the *MAAF* and the *CGMRAF* because the cuspids have a still different relation to their mandibular counterparts.

(1106) Location of the *MAAF* relative to the *BFBCE* requires a circle segment radius expansion of the *BFBCE* equation such that the lingual surfaces of the maxillary incisors, after being adjusted vertically to provide a predetermined overlap, will contact the labial face of the mandibular incisors at points spaced labially from the *BFBCE* with the predetermined *Clearance*. This expansion is calculated as the average distance between points P_1 and P_2 on the four maxillary incisors and adding the predetermined *Clearance* of typically 0.25 mm. This expansion, so calculated, is added to the *BFBCE* circle segment radii to define the maxillary anterior contact arch form *MAAF*. The *MAAF* is thus also expressed as a circle segment equation.

The calculation of the amount of circle segment radius expansion of the *BFBCE* needed to define the *MAAF* is made at the midpoint of the mesiodistal width of either maxillary central, *TMP*, in Fig. 4C. This would be the intersection with *BFBCE* of circle C_1 in Fig. 7C. The tooth is placed on the maxillary contact arch form equation *MAAF* such that the mesial contact point of the tooth is on intersection of the midline *ML* and the maxillary contact arch form *MAAF* (Fig. 4C). (1108) The *MAAF* is defined as follows with respect to upper laterals and centrals:

$$MAAF = BFBCE + \sum_{i=1}^t \frac{P_{1i} - P_{2i}}{2(Avg)} + Clearance$$

where:

t = number of teeth (4),

$Avg = 2$ (to find midpoint), and

Clearance = 0.25mm, typically.

P_1 and P_2 are points on the maxillary central as defined in step (600). As described above, the crown long axes *CLA* of these teeth are angulated relative to the occlusal plane at the crown long axis seed values stated in Table 1.

(1109) The tooth placement proceeds in accordance with the tooth placement routine (2200) described below. The placement positions the lingual faces of the central teeth on the *MAAF*, with the central mesial contact point *MCP*, on *ML*. The midpoint *TMP*, of the mesiodistal width of the next maxillary tooth is then placed on the maxillary contact arch equation *MAAF* such that the mesial contact point *MCP*, touches a line normal to the curve *MAAF* and through the distal contact point *DCP*, of the previous tooth. This procedure applies on one side of the occlusion up to the cuspid. The other maxillary side is constructed similarly.

The next substep in the construction of the maxillary occlusion is (1110) the definition of the location of the arch for horizontal placement of the posterior teeth. The teeth are again set at the *LAI* values of Table I from step (600). (1111) The intersections of the marginal ridge and the central groove, which, if not separately selected in step (600) may be taken as point *P₁* in Fig. 6C, are placed over the buccal cusp of the appropriate mandibular tooth whose cusps were previously positioned on the best fit buccal cusp equation *BFBCB*. Thus, the *CGMRAF* coincides with the *BCBFB* as shown in Fig. 4B.

For the maxillary cuspids, (1115) the cusp tips are placed on some smooth arch between the *MAAF* and the *CGMRAF*. Preferably, their tips are placed on the *BFBCB* expanded by the average of the distances therefrom to the incisal tip of the lateral and to the buccal cusp tips of the first maxillary bicuspid. This labial distance from this point to the buccal cusp tip of the first bicuspid may alternatively be used to place the distal contact point of the cuspid, with its mesial contact point in contact with the distal contact point of the lateral. The point to which the *BFBCB* must be expanded to locate the buccal cusp tip of the first bicuspid for the two above alternatives is $P_{X1}(U, 4) - P_{X2}(U, 4)$. The cuspids will thereby be spaced out from the *BFBCB* by the average of a distance equal to the horizontal or *X* distance from *P₁* to *P₂* on the first maxillary molar, as illustrated in Fig. 6C, and the *MAAF*.

Alternatively, the cuspids may be placed with their mesial contact points *MCP*, on the *MAAF* and with their distal contact points *DCP* in line with the mesial contact points or with the buccal cusp tips of the first maxillary bicuspid.

A third alternative in placing the cuspids is to use the same criteria for clearance with the mandibular teeth used for the definition of the *MAAF*. Following the determination of the *MCAF*, the cuspids placed adjacent the laterals with the tips thereof on the *MCAF*, followed by the successive placement of the posterior teeth with the marginal ridges thereof on the *CGMRAF* (*BFBCB*), all according to routine (2200).

In relating the profile and archform drawings and equations above, it should be noted that the *X* dimension of the profiles on which *P₁* and *P₂* are defined are vertical planes, and that the *X* direction in these planes corresponds to the labial direction in the horizontal planes of the archforms, as was explained for the mandibular teeth in connection with Fig. 7C. Thus, addition of an *X* component of a point on a tooth profile to an archform curve results in a labial expansion of the archform, or an increase in the radius of the corresponding circle segment of the archform circle series equation.

At this point, information from the prescription 27 from the orthodontist 14 is retrieved to determine (1120) which maxillary anterior vertical occlusion method has been selected. The methods may include, for example, (1121) Roth occlusion, (1122) Ricketts occlusion, or (1123) the preferred method, referred to by the inventors as Elan occlusion. These are discussed below.

Where (1121) Roth occlusion has been selected, the maxillary cuspids will extend a distance CR_m equal to the cuspid rise *CR* below the occlusal plane *MOC*, and for laterals and centrals, the teeth will extend a distance CR_m equal to 0.5 the cuspid rise beyond the occlusal plane, as illustrated in Fig. 7D. From step

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(725), the treatment is selected to apply either group function or cuspid rise function, and the respective cuspid rise quantities for maxillary cuspids are determined. From the lowest point on buccal (facial) cusp, a distance is measure vertically upward equal to 0.5 CR to find the intersection of occlusal plane MOC and central and lateral teeth. If two profiles were taken, the profile that includes marginal ridges is used. The intersections of MOC with each maxillary incisor are defined as follows:

Facial intersection with MOC = FIMOC,

Lingual intersection with MOC = LIMOC,

The distance from LIMOC to FIMOC, DLF, is computed as follows:

$$DLF = X_{FIMOC} - X_{LIMOC}$$

where LIMOC is the contact point with MAAF.

Where (1122) Ricketts occlusion is prescribed, the maxillary cuspids also extend below the MOC by a distance CR_m equal to the cuspid rise CR. The laterals are positioned such that the tips are the distance CR_m of 1.0mm above the cuspid tips, and the distance CR_m is such that the tips of the centrals are 0.5mm above the cuspid tips. From step (725), in which either group function or cuspid rise function were selected, the respective cuspid rise quantities are applied for the maxillary cuspids. Then, from lowest point on buccal (facial) cusp, a distance of 1.0 mm is measured upward on the laterals and a distance of 0.4 mm is measured upward on centrals to find the intersection of MOC with the central and lateral teeth. If two profiles were taken, a profile that includes the marginal ridges is used. A line is then constructed through the points on the buccal cuspis parallel to the MOC. The intersections with the teeth are defined as follows:

Facial intersection with MOC = FIMOC

Lingual intersection with MOC = LIMOC

$$\text{Distance DLF from LIMOC to FIMOC} = X_{FIMOC} - X_{LIMOC}$$

where LIMOC is contact point with MAAF.

Where (1123) Elan occlusion has been selected, the maxillary cuspids will extend a distance CR_m equal to 0.67 of the cuspid rise CR below the occlusal plane MOC, laterals extend a distance CR_m equal to 0.33 of the cuspid rise CR below the plane MOC, and the centrals extend a distance CR_m equal to 0.50 of the cuspid rise CR below the plane MOC. As with the above, from step (725), in which either group function or cuspid rise function were selected, the respective cuspid rise quantities are applied for the maxillary cuspids. Then, from the lowest point on buccal (facial) cusp, a distance of 0.33 of the cuspid rise CR is measured upward on the laterals, and a distance of 0.50 of the cuspid rise CR is measured upward on the centrals, and the intersection of the teeth with the plane MOC is found. If two profiles were taken, a profile that includes marginal ridges is used. The MOC plane and the intersections with the teeth are defined as follows, as illustrated on the cuspid in Fig. 7D:

Facial intersection with MOC = FIMOC.

Lingual intersection with MOC = LIMOC.

$$\text{Distance DLF from LIMOC to FIMOC} = X_{FIMOC} - X_{LIMOC}$$

LIMOC is contact point with MAAF.

The (1125) elected horizontal occlusion is selected. If (1126) the Roth maxillary anterior horizontal occlusion has been selected, no further changes are required. This results in the lingual surfaces of the teeth forming a smooth arc. If (1127) the Ricketts maxillary anterior horizontal occlusion has been selected, changes are made to cause the labial surfaces of the teeth to form a smooth arc. This requires finding the

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largest *DLF*, or *LIMOC-FIMOC* distance for the centrals, subtracting the other *LIMOC-FIMOC* distances of the incisors from this largest distance, adding the respective differences to each tooth to extend the *LIMOC* point lingually along line *LIMOC-FIMOC*, and establishing a new point at which the *LIMOC* is to intersect the *MOC*.

5 If (1128) the Elan horizontal occlusion is selected, which is the preferred and illustrated embodiment, the horizontal tooth placement proceeds as set forth below. Because, given the overlap of the maxillary incisors, the labial-lingual thicknesses of the anterior teeth are greater in the plane of occlusion than the distance P_1P_2 , used to calculate the *MAAF* and the *MCAF*, offsets must be calculated and the maxillary teeth placed again on the offset versions of these archforms.

10 First, in calculating the positions of the teeth to provide the horizontal occlusion, (1130) a distance is calculated from *LIMOC* to *ICP* for the maxillary centrals and the laterals. This distance is referred to as the maxillary anterior offset *MAO*, thus:

$$ICP = \frac{X_2 + X_3}{2} ; \frac{Y_2 + Y_3}{2}$$

$$MAO = LIMOC_x - ICP_x$$

(1135) The maxillary first bicuspid offset *MBO* is calculated:

$$MBO = P_{1x} - P_{1x'}$$

15 (1140) The maxillary tooth positions are then recalculated, one side at a time, with respect to the offset maxillary arch forms defined above that contain the buccal cusp tips and incisal edges of the maxillary teeth. This is achieved by sending the relevant parameters to the placement routine (2200) and calculating placement in the same manner as shown in Fig. 7B for the mandibular teeth. For the maxillary centrals, (1141) *MAAF* is adjusted such that the *MAAF* radii are increased by the amount of the *MAO*. This curve is now called maxillary contact archform offset *MAAFO* and is illustrated in Fig. 4C.

20 Calculation of the positions of the maxillary incisors on the *MAAFO*, preferably in accordance with the tooth placement routine (2200), closes the spaces between the teeth that results from expanding *MAAF* to *MAAFO*.

25 The intersection of *MAAFO* and the arch midline *ML* is the mesial contact point *MCP* of the tooth. A circle C_1 is constructed with a radius equal to the mesiodistal width *MDW* of the central incisor. Its center is at the intersection point of *MAAFO* and *ML*. The intersection of the circle C_1 with *MAAFO* is the distal contact point *DCP*. Then, circle C_2 is constructed with a radius equal to $MDW/2$, that is half the mesiodistal width *MDW*. Its center is coincidental with that of C_1 . The intersection of the circle C_2 with the *MAAFO* curve is the mid-point of tooth *TMP* and the incisal center point *ICP*.

30 The intersection of *MAAFO* and circles C_1 and C_2 are then constructed. The curve defined by *MAAFO* and the intersection of circle C_1 is the distal contact point *DCP*. The intersections of *MAAFO* and *MAAFO* circle segment lines are found. The *X* coordinates of the intersections are compared to the *X* coordinates of *DCP* to determine which segment's center will be used.

35 A distal contact point line *DCPL* is constructed from the selected segment center to the *DCP*. Similarly a center of tooth line *TMPL* is constructed from the sector center to the *TMP*. Thus, the tooth

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LIMOC is on *MAAF* and the tooth mesiodistal width line is on the *MAAFO* arch. The location of *FIMOC* is accordingly determined by adding *DFL* to the *MAFFO* circle segment radius through the *TMP*.

The *MAAFO*, like the *MO* for the mandibular teeth, is discontinuous, with the archform being offset differently for the different maxillary teeth. Accordingly, for the maxillary laterals, the prior *MAAFO* is replaced with the *MAAF* adjusted such that the *MAAF* radii are increased by amount of *MAO* for lateral. The tooth's *MCP* is the tooth's *MAO* distance from the *MAAF* along the prior tooth's distal contact point line *DCPL*. Circle *C₁* is constructed with a radius the mesiodistal width of the tooth and with a center at the tooth's *MCP*. The intersection of *C₁* with the *MAAFO* is the tooth's *DCP*. Circle *C₂* is constructed with a radius equal to half of the tooth's *MDW* and with a center coincident with that of circle *C₁*. The intersection of circle *C₂* with *MAAFO* is the tooth's *ICP*.

Then, the intersections of *MAAFO* and the *MAAFO* sector lines are found. The *X* and *Y* coordinates of intersections are compared to the *X* and *Y* coordinates of *DCP* to determine which segment's center will be used. A distal contact point line *DCP* is constructed from the selected segment center to the *DCP*. Similarly a center of tooth line *TMPL* is constructed from the sector to the *TMP*.

For the maxillary cuspids, the prior *MAAFO* is eliminated. A new arch form, the maxillary cuspid arch form *MCAF*, is computed to place the cuspid between the lateral and the first bicuspid. In one preferred approach, the *MCAF* is constructed offset from the *BFBCE* by the average of the *OFFSETS* of the first bicuspid and the lateral, as calculated in substep (1135) above. With exception of a new arch radius, the cuspid is placed as above.

For the maxillary bicusps and molars, the arch form *CGMRAF*, which is the *BFBCE*, is offset by *MBO*. *CGMRAF* is adjusted by adding *MBO* for the respective teeth. The cuspid tips on the *MCAF*, which was offset from the *BFBCE* to align with the buccal cusp tips of the first bicusps in (1115) above, are thus in line with the posterior buccal cusp tips. From the cuspid *DCP*, circles *C₁* and *C₂* are constructed and *DCPLs* are established. This sequence is repeated for remainder of the teeth, completing the relation of the maxillary and mandibular occlusions. The finish positions of the maxillary teeth are illustrated Fig. 4D.

At this point, the final positions of the maxillary teeth have been calculated, and thus, the finish positions of all of the teeth.

Appliance Design Procedure (96)

The appliance design procedure includes the steps of (1200) determining the location of the mandibular archwire plane relative to the calculated finish positions of the mandibular teeth, (1300) calculating the angle of each mandibular bracket slot relative to the mounting surface of the respective tooth, (1400) determining the location of the maxillary archwire plane relative to the calculated finish positions of the maxillary teeth, (1500) calculating the angle of each maxillary bracket slot relative to the mounting surface of the respective tooth, (1600) calculating the shape of the mandibular archwire and the slot in-out dimension of each mandibular bracket, (1700) calculating the shape of the maxillary archwire and the slot in-out dimension of each maxillary bracket, and (1800) calculating the contours of bracket placement jigs for each tooth.

(1200) Mandibular Archwire Plane Step:

The next step is (1200) to establish the position of the archwire plane for the mandibular teeth, which is illustrated in detail in the flowchart of Fig. 2F. The archwire plane can be located in an infinite number

of vertical positions since the brackets and archwire will be designed to accommodate any chosen location. Since the overlap of the maxillary teeth is known, for labial bracket placement, the mandibular archwire plane is set to provide bracket clearance for the maxillary teeth in the finished occlusion. For lingual bracket placement, this consideration is given to the maxillary archwire plane instead, in step (1300) below.

5 Since the maxillary teeth do not pose a bracket interference dilemma with labial bracket placement, the brackets can be positioned for ease of placement, cosmetic considerations and gingival health. This applies to the mandibular bracket positioning where lingual bracket placement is used. Typically, these brackets are located more centrally than the brackets of the other arch.

10 More particularly, as illustrated in the flowchart of Fig. 2P and Fig. 8, (1200) to establish the archwire plane, (1205) the selected vertical occlusion and respective vertical overlap from *MOC* for cuspids, laterals and centrals is recalled from (1110). Then, (1210) with the information from (705), the buccal cusp height *BCH* is recalled for each bicuspid and molar. Next, (1215) the maximum *BCH* or anterior vertical overlap is chosen as the maximum vertical overlap *MVO*. Then, (1220) a distance equal to the *MVO* is measured downward from the *MOC*. Finally, (1225) half of the bracket height (typically 3.0 mm) plus an additional 0.75 mm is added for occlusal clearance. This defines the mandibular archwire plane *MAWP*. This places brackets as occlusal as possible with an 0.75 mm clearance from the worst case from the maxillary occlusion.

(1300) Mandibular Slot Inclination Step:

20 Once the archwire planes have been defined with respect to the teeth, as illustrated in the flowchart of Fig. 2Q, (1300) the angle between the bracket mounting surface of the teeth and archwire plane is determined. This angle minus 90° is the facial torque or inclination angle to be formed into the brackets. This also defines the bracket slot placement height which is the distance from the top of the incisal edge to the archwire plane. This distance is calculated perpendicular to the archwire plane.

25 Slotless bracket bodies (vanilla brackets) have now been positioned appropriately. A smooth archwire is then designed such that it will pass through the bodies of the brackets. The archwire must not cut too deeply into the bracket or pass even partially outside the face of the brackets. Brackets are chosen having different heights according to need. Without modifying buccal tube assemblies, standard bracket distances from the tooth surface to the center of the slot may be used as a seed values. The archwire equation is then mathematically derived from cubic spline and tangential circle techniques as previously described and provided in the routines (2000) and (2100). Both archwires are developed similarly.

30 Bracket angle determination (1300), more particularly, is achieved by (1305) taking the intersection of the *MAWP* and labial (buccal) surface of each mandibular tooth in the case of labial appliances, and the intersection of the *MAWP* with the lingual surface of each tooth in the case of lingual appliances. Then, (1310) circles are constructed with centers at the intersections and with diameters that represent the occluso- gingival (vertical) dimensions of the bracket bonding pad (typically 3.0mm). Then, (1315) *X, Y* coordinates of the circle intersections with labial (buccal) tooth surface are taken, and, with the equations:

$$R^2 = (X_1 - h)^2 + (Y_1 - K)^2$$

$$Y_1 = mX_1 + b_1$$

$$Y_2 = mX_2 + b_2$$

40 (1320) The slopes between the points of intersection are calculated to produce the facial inclination angle *FIA*, where:

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h, k = coordinates of circle center

X_1, Y_1, b_1 = definition of first line segment

X_2, Y_2, b_2 = definition of second line segment

Then, as illustrated in Fig. 8A for labial appliances, $\pi/2$ radians are then subtracted to produce the slot inclination angle SIA :

$$FIA = \frac{Y_2 - Y_1}{X_2 - X_1}$$

$$SIA = FIA - \pi/2$$

(1400) Maxillary Archwire Plane Step:

The next step is (1400) locating the maxillary archwire plane as illustrated in the flowchart of Fig. 2R and diagram of Fig. 8. For the maxillary centrals, this involves (1405) finding the vertical distance from incisal edge to point P_c . (1410) The smallest value is selected and divided by two to produce the slot placement height for the maxillary centrals. (1415) For terminal maxillary bicuspids the vertical distance from buccal cusp to point P_c is found. (1420) Again, the smallest value is selected and divided by two. This produces the slot placement height SPH for the terminal maxillary bicuspids.

For maxillary centrals, (1425) the Y value of $FIMOC$ is subtracted from the Y value for the slot placement height SPH . This is the distance from MOC to the slot centerline. For terminal maxillary bicuspids, (1430) the Y value of MOC is subtracted from the Y value for the slot placement height SPH . This is the distance from MOC to the slot centerline. Then, (1435) the SPH for the terminal bicuspid from SPH for the maxillary centrals. This is elevation change DH of the maxillary archwire relative to the MOC from the centrals to the terminal maxillary bicuspids. (1440) The elevation of the maxillary archwire $MXAWP$ from the MOC , or archwire height AHT on each tooth, is calculated as follows:

$$AHT = K + DH + SPH - MOC,$$

+ Vertical overlap from (1110)

where K is the conversion factor from Table 3.

Tooth Type	Non-Extraction	Extraction (e.g. 2nd Bicuspid)
Maxillary Central	0.0	0.0
Maxillary Lateral	-0.19	-0.23
Maxillary Cuspid	-0.42	-0.62
Maxillary First Bicuspid	-0.68	-1.00
Maxillary Second Bicuspid	-1.00	NA
Maxillary First Molar	-1.32	-1.46

TABLE 3

(1500) Maxillary Slot Inclination Step:

Once the archwire plane is determined, as illustrated in the flowchart of Fig. 2S, (1500) the slot inclination angle SAI for each of the maxillary tooth brackets is determined in a manner similar to the slot

inclination determination step for the mandibular brackets (1300). This step (1505) begins by finding the intersection of the maxillary archwire plane *MAXWP* with the labial or buccal surface of each maxillary tooth. Then, (1510) circles are described, for each maxillary tooth, having centers at this intersection point and having diameters equal to the occluso-gingival, or vertical, dimensions of the bracket bonding pad, which is typically 4.0 mm. From these circles, (1515) *X,Y* coordinates of the intersections of the circles with the labial or buccal tooth surface are found, as follows:

$$R^2 = (X_1 - h)^2 + (Y_1 - k)^2$$

$$Y_1 = mX_1 + b_1$$

$$Y_2 = mX_2 + b_2$$

Where: *h,k* = coordinates of the circle center

X₁,Y₁ = possible coordinates on the circle

X₁,Y₁,b₁ = definition of a first line segment

X₂,Y₂,b₂ = definition of a second line segment

Then, as illustrated in Fig. 8A, (1520) $\pi/2$ radians are then subtracted to produce the slot inclination angle *SIA*:

$$FIA = \frac{Y_2 - Y_1}{X_2 - X_1}$$

$$SIA = FIA - \pi/2$$

(1600) Mandibular Archwire and Slot Depth Step:

The next step, as illustrated in the flowchart of Fig. 2T, is (1600) to determine the mandibular archwire and bracket in-out dimension. First, (1605) the circle segment of the *BFBCE* with which the *ICP* of the right central is associated is determined, as illustrated in Fig. 8B. Then, (1610) the incisal center point and circle segment center point plane *ICPCDCPP* is created normal to the arch planes. An incisal center point line *ICPL* is struck that will pass through the *ICP* and a particular circle segment center point *CSCP* associated with the tooth. Then (1615) the Pythagorean distance *PD* from *CSCP* to *ICP* is determined. Then, (1620) viewing the tooth in the *ICPCDCPP*, as illustrated in Fig. 8C, a line *NL* is struck normal to the *BFBCE* plane through the *ICP*, which is the intersection of *CLA* and *BFBCE*. Next, (1625) still viewing the tooth in this plane, the intersection point *XP* of *NL* and *MAWP* is determined.

Still viewing the tooth in the *ICPCDCPP*, (1630) the *X* distance *XD* to the labial surface of the tooth from the *XP* is determined, and (1635) *PD* is added to *XD* and the lower limit of the bracket slot *LLBS*. The *LLBS* is a distance associated with the particular bracket that will be placed on this tooth. It is the deepest slot allowable for that bracket. Then, the lower limit *LL* is calculated thus:

$$LL = PD + XD + LLBS$$

Similarly, (1640) *PD* is added to the *XD* and the upper limit of the bracket slot *ULBS*. The *ULBS* is also a distance associated with the particular bracket that will be placed on this tooth. It is the shallowest slot allowable for that bracket. Then, the upper limit *UL* is calculated thus:

$$UL = PD + XD + ULBS$$

(1645) Then, viewing the mandibular occlusion in a plan view and moving out along the *ICPL* from its *CSCP* by the *LL* distance, *X* and *Y* points, *AWLL_{XP}*, are determined relative to an origin at the

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intersection of *BFBCE* and the mandibular midline *ML*. Then, (1650) viewing the mandibular occlusion in a plan view and moving out along the *ICPL* from its *CSCP* by the *UL* distance, *X* and *Y* points, *AWUL_{X,Y}* are determined relative to the intersection of *BFBCE* and the mandibular midline *ML*. Then, (1655) the mid-point of *AWLL_{X,Y}* and *AWUL_{X,Y}* is found and steps (1605) through (1650) are then repeated for all mandibular teeth.

Then, (1660) the average mid-point and distance from right to left is calculated to force mandibular archwire symmetry:

$$S_X = MP_X + \frac{PR_X - PL_X}{2}$$

$$S_Y = MP_Y + \frac{PR_Y + PL_Y}{2}$$

Where: *S_{X,Y}* is the symmetricalized point.

MP is the mid-point of *BCBCE*.

PR is a point on the right side of the midline.

PL is a point on the left side of the midline.

The smoothest curve *SC* that will pass between all *AWLL_{X,Y}* and *AWUL_{X,Y}* points is then determined, as illustrated in Fig. 4E. This is accomplished by the following procedure:

- a) The mid-point of each *AWLL_{X,Y}* and *AWUL_{X,Y}* pair is found.
- b) Then, as described above, a cubic spline equation is passed through these points.
- c) The existence of any inflection points is determined.
- d) The curve with the least variation in radius changes along the curve is considered the smoothest curve. Preferably, it has no inflection points. If there are one or more inflection points, a logical alternative bracket solution will be derived based upon where the inflection occurred.

Then, (1665) the intersection point *XSCICPL* of the mandibular right central's *ICPL* is determined as well the smoothest curve as defined above in substep (1660). Next, (1670) the in-out *IO* of that particular tooth is determined as the distance along *ICPL* from *ICP* to *XSCICPL* minus that tooth's *XD*. Then, (1675) steps (1665) and (1670) are repeated until all in-out dimensions are calculated.

Finally, (1675) all *XSCICPL* points are passed into the cubic spline routine (2000) and to circle routine (2100) and (1680) all circle segment information gathered therefrom are converted to linear distance *LD* moves needed to bend the appropriate wire, as will be further explained in connection with the wire bending step (3200) below. The bracket slot cutting is described in connection with step (3000) below.

(1700) Maxillary Archwire and Slot Depth Step:

The next step, as illustrated in the flowchart of Fig. 2U, is (1700) to determine the maxillary archwire and bracket in-out dimension. As with the mandibular determination step (1600), (1705) the circle segment of the *BFBCE* with which the *ICP* of the right central is associated is determined. The step is similar to that for the mandibular slot in-out dimension calculation of Figs. 4E and 8C, except that the maxillary centrals and laterals are associated with the *MAAF* rather than the *BFBCE*, the maxillary cuspids are associated with *MCAF*, and teeth posterior to the cuspid are associated with the *BFBCE*.

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The calculation proceeds with (1710) the incisal center point and circle segment center point plane *ICPCDCPP* being created, with a line being struck that will pass through the incisal center point line *ICPL* which will pass through the *ICP* and a particular circle segment center point *CSCP* associated with the tooth. The plane passing through the *ICP* and the *CSCP* and normal to the mandibular trough *MT* is the *ICPCSCPP*. Then (1715) the Pythagorean distance *PD* from *CSCP* to *ICP* is determined. Then, (1720) viewing the tooth in the *ICPCSCPP*, a line *NL* is struck normal to the *BFBCE* through the intersection of *CLA* and *BFBCE*. Next, (1725) still viewing the tooth in this plane, the intersection point *XP* of *NL* and *MAWP* is determined.

Still viewing the tooth in the *ICPCSCPP*, (1730) the *X* distance *XD* to the labial surface of the tooth from the *XP* is determined, and (1735) *PD* is added to *XD* and the lower limit of the bracket slot *LLBS*. The *LLBS* is a distance associated with the particular bracket that will be placed on this tooth. It is the deepest slot allowable for that bracket. Then, the lower limit *LL* is calculated thus:

$$LL = PD + XD + LLBS$$

Similarly, (1740) *PD* is added to the *XD* and the upper limit of the bracket slot *ULBS*. The *ULBS* is also a distance associated with the particular bracket that will be placed on this tooth. It is the shallowest slot allowable for that bracket. Then, the upper limit *UL* is calculated thus:

$$UL = PD + XD + ULBS$$

(1745) Then, viewing the mandibular occlusion in a plan view and moving out along the *ICPL* from its *CSCP* by the *LL* distance, *X* and *Y* points, *AWLL_{X,Y}*, are determined relative to the intersection of *BFBCE* and the mandibular midline *ML*. Then, (1750) viewing the mandibular occlusion in a plan view and moving out along the *ICPL* from its *CSCP* by the *UL* distance, *X* and *Y* points, *AWUL_{X,Y}* are determined relative to the intersection of *BFBCE* and the mandibular midline *ML*. Then, (1755) The mid-point of *AWLL_{X,Y}* and *AWUL_{X,Y}* is found and steps (1705) through (1750) are then repeated for all mandibular teeth.

Then, (1760) the average mid-point and distance from right to left is calculated to force mandibular archwire symmetry:

$$S_x = MP_x \frac{PR_x - PL_x}{2}$$

$$S_y = MP_y \frac{PR_y + PL_y}{2}$$

Where:

S_{X,Y} = the symmetricalized point.

MP = the mid-point of *BCBCE*.

PR = a point on the right side of the midline.

PL = a point on the left side of the midline.

Then the smoothest curve *SC* that will pass between all *AWLL_{X,Y}* and *AWUL_{X,Y}* points is determined. This is accomplished by the following procedure:

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- a) The mid-point of each $AWLL_{x,r}$ and $AWUK_{x,r}$ pair is found.
- b) Then, as described above, a cubic spline equation is passed through these points.
- c) The existence of any inflection points is determined.
- d) If there are no inflection points, this is considered the smoothest curve. If there is an inflection point, a logical alternative bracket solution will be derived based upon where the inflection occurred. The relevant information necessary to determine a new pair of $AWLL_{x,r}$ and $AWUL_{x,r}$ and their midpoints is undertaken. It should be noted that there are varying $LLBS$ and $ULBS$ possibilities available for each tooth.

Then, (1765) the intersection point $XSCICPL$ of the mandibular right central's $ICPL$ is determined as well the smoothest curve as defined above in substep (1760). Next, (1770) the in-out of that particular tooth is determined as the distance along $ICPL$ from ICP to $XSCICPL$ minus that tooth's XD . Then, (1775) steps (1765) and (1770) are repeated until all in-out dimensions are calculated.

Finally, (1775) all $XSCICPL$ points are passed into the spline to circle program and (1780) all circle segment information gathered therefrom are converted to linear distance LD moves needed to bend the appropriate wire, as will be further explained in connection with the wire bending step (3200) below. The bracket slot cutting is described in the discussion of step (3000) below.

(1800) Placement Jig Design Step:

With the shapes of the individual teeth determined, their finish positions calculated, and the brackets designed and their places on the individual teeth determined, the information necessary for the design of bracket placement jigs to aid the orthodontist in positioning the brackets in their proper positions on the individual teeth is available. In the preferred embodiment of the invention, the design of the placement jigs is carried out in the software associated with the jig manufacturing step (3500) described below, following a loading of the appropriate files with the necessary data from the calculations described above into the manufacturing control computer 30c. An abbreviated presentation of the jig design substeps is set forth in the flowchart of Fig. 2V.

Referring to Fig. 2V, (1805) a file containing data of the individual tooth profiles, the archwire plane location including data relating each of the tooth profiles to the relevant archwire plane, the bracket profiles relevant to each tooth, and the bracket design data including the slot size, inclination and depth, are prepared. Then, (1810) the tools that will form the jig are determined, and (1815) clearances are established. Then, (1820) data needed for instructions to cut an internal profile into each jig is assembled to hold a bracket and to locate the bracket at the proper position on the tooth by precise fitting of the jig over the tooth profile along a labial-lingual plane through the tooth midpoint TMP .

The details of the jig design step, as it is performed along with the jig manufacturing step, is described in detail in connection with the description of the flowchart of Fig. 2Z under step (3500) below.

Subroutines

Three subroutines are used in calculating various archforms and calculating the positions of the teeth thereon. These are (2000) the cubic spline equation curve calculation subroutine, (2100) the spline equation to circle segment equation conversion subroutine, and (2200) the tooth placement subroutine. These are illustrated in the flowchart of Fig. 2W.

(2000) Cubic Spline Equation Fitting Subroutine:

In the cubic spline interpolation, symmetrical data points are interpolated and a cubic spline equation is derived. As illustrated in Fig. 5A, a symmetrical mandibular trough or cubic spline equation *SMT* is shown for one side of the lower jaw. In Fig. 5A, the point $M_p M_r$ represents the intersection of the curve and the midline *ML*. The points $SI_x SI_r$ for $I = 1$ to 6 represent the symmetricized points X_{sm} referred to above.

The cubic spline method uses a cubic (3rd degree) polynomial to interpolate between each pair of data points. A different polynomial is used for each interval, and each one is constrained to pass through the original data points with the same slope as the data. At these points, slopes are computed by finding the slope of the parabola that passes through each data point and its two nearest neighbors.

The iterations necessary to compute the cubic polynomial are as follows:

- 1) For each data point, the *X* and *Y* coordinates are made equal to zero and all other data points evaluated relative to this new original.
- 2) The slopes of the cubic spline are computed by first computing the coefficients of the above described parabola, then a first point of a slope array is filled followed by the remaining points through the final slope array point.
- 3) The spline coefficients are computed.
- 4) The polynomial is evaluated.

These steps are described in Science and Engineering Programs, Apple II Edition, Edited by John Heilborn, and published by Asborne / McGraw - Hill. Copyright, 1981, McGraw - Hill, Inc., and incorporated herein by reference.

Once the polynomial has been evaluated, it is possible to acquire additional data points. A *Y* value can be determined for any given *X* value, with the constraint that additional data points be within the upper and lower limits of the original *X* values. The following iterations are performed before circle conversion:

- 1) Determination of *X* and *Y* points on each side of the original data points. This is done by taking *X* points that are one thousandth (.001) to each side of original *X* data points. Then *X* values two thousandths (.002) less than the last data point are taken. Then *Y* points are determined for each arrayed *X* point by evaluation of the polynomial equation discussed above. Then the *Y* points of the array are calculated.
- 2) The slope array is then filled with slopes corresponding to data points on either side of the original data points.
- 3) The slope of the curve at each of the original data points is calculated. This involves retrieving *X* and *Y* points on either side of original data points, and calculating the slope at the original data points using the Point Slope method according to:

$$SLOPE = \frac{Y_2 - Y_1}{X_2 - X_1}$$

Where:

SLOPE = the slope of the curve at that point.

XI = the *X* point .001 to left of original data point.

YI = the *Y* point associated with *XI*.

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$X2$ = the X point .001 to right of original data point.

$Y2$ = the Y point associated with $X2$.

The slope is calculated using the arrayed point that is .002 less than the last data point and the last data point, and the slope is calculated using the point slope method as all array slopes are calculated.

5 (2100) Circle Segment Conversion Subroutine:

The circle segment conversion typically fits two circle segments into one spline segment. A spline segment is defined as the interpolated cubic spline equation which describes the shape of the curve between two original data points. A circle segment is defined as the arc associated with a beginning point, or end point, and the slope of tangency at that point. Two configurations of circle segments are possible when
10 converting a spline segment into two circle segments, one where the first circle is larger than the second (Fig. 5B) and the other where the first circle is smaller than the second circle Fig. 5C, the variables in which are identified below. The iterations necessary to convert a spline segment into two circle segments are illustrated in Fig. 5D in which:

$P1, P1_t$ = the beginning point of spline segment

15 $P2, P2_t$ = end point of spline segment

$MT1$ = tangent slope of spline at point $P1, P1_t$

$MN1$ = normal slope of $MT1$

$MT2$ = tangent slope at point $P2, P2_t$

$MN2$ = normal slope of $MT2$

20 $P3, P3_t$ = intersection of a line through point $P1, P1_t$ with a slope of $MT1$ and a line through point $P2, P2_t$ with a slope of $MT2$

CL = a Cord Line, a line connecting points $P1, P1_t$ and $P2, P2_t$

CNL = a Cord Normal Line, a line normal to CL through $P3, P3_t$

h_s, k_s = the center of the smaller of the two circle segments

25 The iterations to convert a spline segment into two circle segments are, as follows:

- 1) Determine $MN1$ and $MN2$. They are the negative inverse of $MN1$ and $MT2$, respectively.
- 2) Determine the intersection point $P3, P3_t$.
- 3) Determine the slope of the CL .
- 4) Determine the slope of CNL .
- 30 5) Determine the distance from $P1, P1_t$ to $P3, P3_t$. This is defined as test one.
- 6) Determine the distance from $P2, P2_t$ to $P3, P3_t$. This is defined as test two.
- 7) Test to determine which length is smaller. If the test one result is shorter than the test result, the smaller circle is associated with $P1, P1_t$, otherwise, the smaller circle is associated with $P2, P2_t$.
- 8) Rename the variable associating to the size of the circle. See Fig. 5B in which:

35 $P1, P2_t$ = the beginning point of spline segment

$P2, P2_t$ = the end point of spline segment

MNS = the normal slope of small circle segment, equivalent to $MN1$ or $MN2$ depending on the relative results of test one and test two

MNL = normal slope of large circle segment

40 h_s, k_s = the center of the smaller of the two circle segments

h_l, k_l = the center of the larger of the two circle segments

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$P6_p, P6_r =$ a distance, defined by the radius of the small circle, to a point along MNL from the spline segment point associated with it

$MNF =$ is the slope of the final line

9) Determine the intersection of the line described by slope of CNL and passing through $P3_p, P3_r$ and the line described by MNS through the spline segment point associated with it. The intersection point of these two lines is the center of the smaller circle hs, ks .

10) Determine the Pythagorean distance from the small circle center hs, ks to the spline segment points associated with it. This distance is the radius of the small circle rs .

11) Move along the line described by MNL and passing through the spline segment point associated with it by the radius of the smaller circle rs . This point is $P6_p, P6_r$.

12) Strike a line from $P6_p, P6_r$ to hs, ks .

13) The negative inverse of the slope of the line from $P6_p, P6_r$ and hs, ks is mnf .

14) Determine the midpoint of the line from $P6_p, P6_r$ to hs, ks .

15) Determine the intersection of the line described by a slope of mnf and passing the point described in step 14 and the line described by MNL and through the spline segment point associated with it. The intersection point of these two lines is the center of the larger circle hl, kl .

16) Determine the Pythagorean distance from the large circle center hs, ks to the spline segment points associated with it. This distance is the radius of the larger circle rl .

17) The intersection of the two circles is defined as the intersection of the line going through the large circle center hl, kl and the small circle center hs, ks and either of the circles. At this point the tangency of the two circles are equivalent.

18) Accommodate an arc length calculation dependent upon which spline point is closer to $P3_p, P3_r$:

If the test one result is greater than that of test two, then:

$$Theta1 = ATN(m) - ATN(MSI)$$

$$Theta2 = ATN(MLI) - ATN(m)$$

otherwise:

$$Theta1 = ATN(msl) - ATN(m)$$

$$Theta2 = ATN(m) - ATN(mll)$$

where:

$$m = \frac{k1 - ks}{h1 - hs}$$

$Theta1 =$ the arc angle of the smaller circle

$Theta2 =$ the arc angle of the larger circle.

19) Calculate arc length for each segment.

$$s1 = rs (Theta1)$$

$$s2 = rl (Theta2)$$

where:

$s1 =$ arc length of smaller segment

$s2 =$ arc length of larger segment

20) Calculate the running arc length.

21) Continue distally until all spline segments are converted.

Figs. 5E-5J illustrate the building of the mandibular trough data points into circle segments.

(2200) Tooth Placement on Curve Subroutine:

The individual tooth placement upon an equation is required in many steps of the tooth finish position calculation procedure (94). The preferred method is described here in connection with the first occurrence in the procedure for the placement of the mandibular teeth.

There are four alternative equations upon which teeth can be placed: the mandibular trough *MT* equation, the maxillary anterior arch form *MAAF* equation, the maxillary cuspid arch form *MCAF* equation, and the central groove marginal ridge arch form *MGMRAF* equation. All occlusion equations will have been converted to circle segments before teeth are placed upon them. A typical tooth placement is illustrated in Fig. 5N, in which:

DCP = Distal Contact Point

ICP = Incisal Center Point

MCP = Mesial Contact Point

MCPL = is the Mesial Contact Point Line.

The *DCP* is the point at which the tooth contacts the proceeding tooth. The *ICP* is the center of the tooth being placed. The *MCP* is the point at which the tooth contacts the preceding tooth. The *MCPL* is defined as the line through the *DCP* of the tooth being placed and the center of the circle segment associated with the *DCP*. The *MCPL* is the line upon which the *DCP* of the proceeding tooth will be found.

The iterations to place the teeth onto the circle segments are:

- 1) Determine the offset distance for the mandibular central tooth on the side of the jaw under consideration.
- 2) Expand all circle segments about their centers by the offset amount.
- 3) Determine the intersection of the first circle segment and the midline. This is the mesial contact point *MCP* of the central, as illustrated in Fig. 5K.
- 4) Place the first circle C_1 , whose radius is the mesio-distal width of the tooth, at *MCP*, as illustrated in Fig. 5K.
- 5) Determine which circle segment in the distal direction circle C_1 intersects and identify the intersection point. This is accomplished by performing an iteration which begins by transferring the coordinate system to the beginning point of the circle segment, as illustrated in Fig. 5L, in which:

X_{BEO}, Y_{BEO} = beginning coordinates of the circle segment

X_{END}, Y_{END} = End points of the circle segment

X_{INT}, Y_{INT} = coordinates of circle intersection

X and *Y* axes are oriented at X_{BEO}, Y_{BEO} .

The two following circle equations are then solved simultaneously:

$$R_1^2 = (x - h1)^2 + (y - k1)^2$$

$$R_2^2 = (x - h2)^2 + (y - k2)^2$$

Where:

$h1, k1$ = the center coordinates of the first circle

$h2, k2$ = the center coordinates of the second circle

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R_1 = the radius of the first circle C_1
 R_2 = the radius of a second circle C_2
 X, Y = coordinates of possible intersection points

The following solutions are possible: (1) two real solutions which are labeled XI_{DT}, YI_{DT} and $X2_{DT}, Y2_{DT}$, respectively. (2) imaginary solutions, which are discarded, whereupon the next circle segment is evaluated. If intersections are real, the circle segment is rotated, as illustrated in Fig. 2M, such that X_{DCT}, Y_{DCT} is placed on the X axis. Then, X_{DCT}, Y_{DCT} is subtracted from the rotated X intersection point XI_{DT} or $X2_{DT}$, and rotated X_{DCT} is subtracted from the rotated X intersection point XI_{DT} or $X2_{DT}$. If the signs of the results of the two subtractions are opposite, the rotated intersection point is tested for a value less than zero. If it is not less than zero, the other rotated intersection point is tested to determine if it is valid. The testing continues until a segment is found such that the subtractions produce opposite sign results and the associated rotated Y intersection point is less than zero. This is the distal contact point *DCP* of the tooth, as illustrated in Fig. 5N.

- 6) Construct a line passing through the *DCP* and the center of the circle segment that intersects C_1 .
- 7) Place circle C_2 , whose radius is one half the mesio-distal width *MDW* of the tooth, at the *MCP*.
- 8) Determine which circle segment in the distal direction intersects circle C_2 and identify the intersection point. This is the incisal center point *ICP* of the tooth, as illustrated in Fig. 5N.
- 9) Eliminate all expanded circle segments.
- 10) Determine the offset distance for the mandibular lateral.
- 11) Expand all circle segments about their centers by the offset amount.
- 12) Determine the intersection point of the expanded circle segment *ECS* associated with the *DCP MCP Line*. The intersection point is the mesial contact point *MCP* of the lateral, as illustrated in Fig. 5O.
- 13) Place circle C_2 , with radius the mesio-distal width *MDW* of the lateral, at the current *MCP* point.
- 14) Determine which circle segment in the distal direction circle C_2 intersects and identify the intersection point, which is the *DCP* of the lateral.
- 15) Construct a line passing through the *DCP* and the center of the circle segment that intersects C_1 .
- 16) Place circle C_2 , whose radius is one half the mesio-distal width *MDW* of the tooth, at the *MCP*.
- 17) Determine which circle segment in the distal direction intersects circle C_2 and identify the intersection point. This is the incisal center point *ICP* of the tooth, as illustrated in Fig. 5P.
- 18) Continue distally until all teeth are placed.
- 19) Perform the same iterations for the co-lateral side of the arch.

(97) Appliance Manufacturing Procedure

The appliance manufacturing procedure (97) includes the steps of (3000) manufacture of the custom brackets, (3200) manufacture of the custom archwires and (3500) manufacture of custom placement jigs for placement of the custom brackets on the patient's teeth. These steps are described in detail below for the embodiment in which all of the manufacturing is carried out at the appliance design facility 13.

(3000) Bracket Manufacturing Step:

The bracket manufacturing step (3000) produces the custom brackets, preferably by selecting bracket blanks and cutting a torque slot in the bracket for the archwire 64. This utilizes the modified CNC mill 40 illustrated in Fig. 2D. The bracket slot cutting step is illustrated in the detailed flowchart of Fig. 2X.

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Referring to Fig. 2X, the bracket manufacturing step (3000) begins with the computer 30c (3005) loading the data for each bracket from the patient data file 36.

For each tooth and bracket, as a default or initial selection, (3010) low profile brackets are assumed. Then, the slot angle *PAI* and the slot in-out dimension *IO* are read. Also, (3020) the radius of the archwire at the tooth midpoint is determined.

Then, (3025) a main CNC program is created and (3030) the program loops to generate the code for the cutting of each bracket, beginning with the calculation of the variables for the bracket, (3040) assigning the variables for each bracket to (3045)-(3050) set the cutting of the slot at the appropriate angle by rotating the bracket support 73 and setting the cutter 77c to a cooperating height *Z* and horizontal *X* position. If the position of the slot lies outside of the area of the bracket, a bracket of the appropriate higher profile is called for by the program, and loaded, either automatically or by an operator. The code is then generated (3055) to control the path of the cutter in the *Y* direction to cut the archwire radius in the slot bottom. (3060) then, the NC code is combined with the calculated variable values for the tooth and bracket and a subroutine is generated for the bracket, with (3065) the P-codes subroutines written the file. (3068) The program loops until codes for all of the brackets are complete.

Then, (3070) the CNC code is preferably downloaded to an NC controller and the brackets are formed by the cutting of the slots in the series of bracket blanks, and (3080) a report is written.

(3200) Archwire Manufacturing Step:

The archwire manufacturing step (3200) produces the archwire 64, as illustrated in Fig. 2E, preferably that is symmetrical about its archwire midline *AML*, having the appropriate terminal leg span *TLS*, formed of a series of circle segments.

As illustrated in the flowchart of Fig. 2Y, the archwire manufacturing step (3200) executes a program with the manufacturing control computer 30c to generate a CNC code to operate the wire forming machine 40. The program begins by (3215) opening one or more files from the calculated patient data 36 and reads therefrom the wire alloy and the wire cross-section prescribed, and an array of data that contains a series of *j* sets of data including the radius and sector length of each circle segment of which the archwire curve is formed, and the calculated total cumulative archwire length. To the archwire equation, (3220) a radii and sector lengths are added to produce a one half inch of straight segment at each end of the wire to form parallel terminal leg extensions. Then, calculating the cumulative slopes and sector lengths of the wire along the equation, (3225) the terminal leg span *TLS* is calculated.

Based upon the wire type selected, (3230) one of several data files or tables are read. For rectangle wire, for example, four files would include: (1) 0.022" thickness stainless steel (SS), (2) 0.025" thickness SS, (3) 0.022" thickness titanium molybdenum alloy (TMA), and (4) 0.025" thickness TMA. Other files are provided for round wires of various diameters and types.

Then, using the cubic spline subroutine (2000), (3235) the slopes of the cubic spline equation describing wire behavior are calculated by: (1) computing the coefficients of a parabola, (2) filling the first point of a slope array, (3) filling the intermediate points of the slope array, and (4) filling the last point of the slope array. Then, (3240) the cubic spline coefficients are calculated. Then, (3245) the vertical displacement of the bending lever arm *LA* (Fig. 2E) between the contact points of the roller 70b with the wire 69 and the contact point of the rollers 68 with the wire 69 is determined for each circle segment of the archwire equation, and data added to the array.

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Then, (3255) temporary variables are defined for the sector length, lever arm displacement, radius and terminal leg span across the straight segments of the archwire, (3260) the controller card 65 of the computer 30c is initialized, (3265) the controller base address is set, and (3270) default parameters are set. Then, (3275) a sequential series of sector lengths and lever arm displacements are sent respectively (1) through the circuits 66a and 67a to the drive of the feed rolls 68, and (2) through the circuits 66b and 67b to the anvil assembly 70.

When all circle segments have been formed, (3280) the lever arm displacement is zeroed and (3285) the wire leg location is read by the sensor 71. This reading converted to a numerical value in the computer 30b and any difference in the actual measured terminal leg span and the desired terminal leg span TL_S is calculated. If (3290) the difference is out of tolerance, a correction is made and another wire is formed. (3500) Jig Manufacturing Step:

The jig manufacturing step (3500) produces bracket placement jigs custom designed for each tooth to aid in the placement of the custom designed brackets in the proper positions on the teeth so that the custom designed archwire will, when installed in the custom designed and custom placed brackets, move the teeth to their calculated finish positions.

The information necessary for the design of the custom placement jigs is contained in the patient data file of from the calculations made in the appliance design procedure (96) and in the tooth profile data file of digitized information read in step (500), in the illustrated embodiment of the invention. The design of the custom jigs involves, primarily, an assembly of the information already generated, and, in the preferred embodiment, takes place in the course of generating the code for control of the NC controlled manufacturing equipment 41 that produces the jigs.

In the preferred and illustrated embodiment, the jig manufacturing equipment 41 is a standard CNC mill equipped with a small carbide endmill tool of, for example, 0.020 inches in diameter (Fig. 1F). The jigs themselves 82 are made from circular ABS plastic wafers 83 of approximately one inch in diameter and approximately 0.040 inches in thickness, though considerable variation in size is acceptable.

The jig manufacturing step (3500), as illustrated in the detailed flowchart of Fig. 2Z, begins with the execution of a program or routine in the manufacturing computer 30b and the input of parameters identifying the patient or case. Upon beginning of the execution of the program, (3515) the file of patient data 36 generated in the tooth position calculation and analysis procedure (95) and the appliance design procedure (96) is opened and information is read for each tooth, as illustrated in the diagram of Fig. 9I, in relation to a tooth profile PF . The variables read are (a) the intersection of the archwire plane and the labial (or lingual, if prescribed) surface of the tooth TS , which is in the form of a pair of X, Y coordinates $TS_{x,y}$ in the tooth profile vertical-labial/lingual plane, (b) the slot in-out dimension $Elan$ or IO , (c) the type of bracket, which provides access to the appropriate place in a lookup table of bracket dimensions, such as bracket base thickness $BRel$ and bracket pad height BPH , and (d) the torque slot width, 0.018 or 0.022 from the prescription.

Then, (3520) the bracket data file is opened and the bracket base thickness read, as illustrated in Fig. 9J. Then, a file name is assigned, (3530) a CNC file is created, and (3535) a CNC "main" program is written to it, as set forth, for example, in the flowchart of Fig. 2Z-1.

Then, (3540) a sequential file is identified that contains the beginning and ending object number for each tooth profile, and (3545) a CAD program file containing the tooth profiles PF_i is loaded. The profiles

PF, as illustrated in Fig. 3C, are made up of a series of closely spaced points in the profile plane, each represented by *X,Y* coordinates, connected by straight line segments to define the profile curve *PF*. The endmill tool diameter *Endmill* is also entered, which must be less than the archwire diameter or archwire slot width (0.018 or 0.022). Constants are declared, including the diameter of the jig blank 83, the cut clearance on the outside of the jig, the number of loops, set at 23, and the counter initial settings.

Then, (3560) the CNC P-code is generated for each tooth, by looping through substeps (3560) through (3639) until the code for each of the jigs 82 is generated. The loop begins by (3560) incrementing the tooth and P-code counters by 1. The loop begins with the lower left bicuspid, as brackets are usually not used on the molars, and proceeds left to right. Thus, (3565), when the incrementing of the counter advances the count to the lower right molar, (3565) the counter is advanced to skip to the upper left bicuspid.

Then, (3570) the parameters for the particular tooth are set up as illustrated in the flowchart detail of Fig. 2Z-2. This is followed by creating the profile and bracket clearance compensation tool paths *IITP* and *BCTP*, respectively, as illustrated in the flowchart detail of Fig. 2Z-3. This involves (3590) the creation of an initial inside tool path line *IITP* made up of a series of straight line segments, one parallel to each of the line segments of the tooth profile curve, spaced a distance equal to the tool radius on the inside of the profile curve, as illustrated in Fig. 9K, (3595) the creation of an initial bracket base compensation tool path line *IBCTP* made up of a series of straight line segments, one parallel to each of the line segments of the tooth profile curve, spaced a distance equal to the bracket base dimension minus the tool radius outside of the profile curve, as illustrated in Fig. 9L, and (3600) creation of the final bracket base compensation tool path (*d*) to cut from the inside tool path line to the base compensation line at the top of the bracket base pad to cut off the jig at the bottom of the pad, as illustrated in Fig. 9M ("top" and "bottom" being used as an example for the lower teeth, and being opposite for the upper teeth).

Next, (3605) the archwire slot tool path *ASTP* is created as illustrated in the flowchart detail of Fig. 2Z-4, which can be understood from the sequence set forth in the flowchart with reference to the diagrams of Figs. 9N, 9O and 9P. Then, as set forth in the flowchart detail of Fig. 2Z-5, (3610) a reference tool path *RefP* is created on an image of a jig blank 83, as illustrated in Fig. 9Q, and with reference to it, (3615) the outside jig boundary cutout *CTP* is added as illustrated in Fig. 2R, and (3620) the actual tool path *TP* is then generated as illustrated in Fig. 9S.

Then, (3625) the CNC machine code is generated, as illustrated in the detailed flowchart of Fig. 2Z-6, and written to the output file. Then, (3630) the variables are reset, (3635) the final results are displayed, and (3640) the program loops back to substep (3560) until all of the bracket jig code have been generated. Then, (3645) the completed CNC file is sent to the controller of the CNC mill and a pallet of wafers 83a (Fig. 1F) is cut into a set of bracket placement jigs 82. An example of one of the jigs is illustrated in Figs. 9T through 9W.

What is described above includes the preferred embodiments of the invention. Those skilled in the art will appreciate that additions to and modifications of the system and method of the invention, and the detailed manifestations thereof, may be made without departing from the principles of the inventive concepts set forth herein. Accordingly, the following is claimed:

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Claims:

1. A method of fabricating a custom orthodontic appliance to position teeth of a patient to preferred finish positions in the mouth of the patient, the method comprising the steps of:

measuring anatomical shapes from the mouth of the patient, and producing thereby digitized anatomical shape data;

5 deriving an archform from the digitized data with a specially programmed digital computer;

deriving with the computer tooth finish positions from the digitized data and the derived archform;

establishing appliance connection points, one on each of a plurality of the teeth;

10 designing, with the computer from the digitized data, the established appliance connection points and the derived tooth finish positions, an appliance configuration such that a custom appliance fabricated in accordance therewith and connected at the appliance connection points to the teeth, will exert substantially no tooth moving forces on the teeth when in the derived tooth finish positions, and will otherwise urge the teeth toward the derived finish positions;

15 producing machine code in accordance with the designed appliance configuration; and automatically fabricating a custom orthodontic appliance with a NC machine in response to the machine code to conform to the designed appliance configuration.

2. The method of claim 1 wherein the teeth include mandibular teeth and maxillary teeth and wherein:

the dental anatomical shape measuring step includes the steps of the measuring the lower jaw of a patient and producing thereby digitized data of lower jaw shape, and measuring
5 mandibular and maxillary teeth of the patient and producing thereby digitized data of individual mandibular and maxillary tooth shape;

the archform deriving step includes the step of deriving with the computer a mandibular skeletal archform from the digitized lower jaw shape data; and

10 the tooth finish position deriving step includes the step of deriving tooth finish positions from the tooth shape data and the derived mandibular skeletal archform to arrange the teeth with respect to the mandibular skeletal archform.

3. The method of claim 2 wherein each tooth has a crown, a root and a long axis extending generally vertically through the center of the crown, intersecting a gingival center point where the crown meets the root, and wherein:

5 the lower jaw measuring step includes the step of digitizing data points defining a mandibular trough in which mandibular tooth roots are to be confined;

the mandibular skeletal archform deriving step includes the step of fitting a smooth continuous mandibular trough equation to the digitized mandibular trough data points and producing a digitized representation of the mandibular trough equation;

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10 the mandibular tooth finish position deriving step includes the deriving positions which center each mandibular tooth by placing the long axis thereof approximately on the mandibular trough equation near the gingival center point of the tooth, and which place the tips of the mandibular teeth on a smooth continuous curve derived by adjusting the mandibular trough equation; and

15 the appliance configuration designing step includes defining the appliance configuration by a series of digital values derived from the smooth continuous curve.

4. The method of claim 1 wherein:

the measuring step includes the step of digitizing data of the shape of the lower jaw of the patient by digitizing boundary points corresponding to boundaries of the patient's cortical bone;

5 the archform deriving step includes the step of deriving from the digitized data a skeletal archform mathematically representing the shape of the patient's cortical bone by a smooth continuous equation derived from the digitized boundary points.

5. The method of claim 4 wherein:

the smooth continuous equation is a cubic spline equation through points related to the digitized boundary points.

6. The method of claim 1 wherein the archform deriving step comprises the step of:

5 defining a curve based on the digitized anatomical shape data and smoothing the curve by a best fit statistical method to produce smooth continuous archform equation, the finish position deriving step and the appliance configuration designing step being based at least in part on the archform equation.

7. The method of claim 1 further comprising the steps of:

digitally representing the derived archform by an archform equation in the computer;

representing the archform equation by a series of successively tangent circle segments;

5 the appliance configuration designing step includes the step of designing an arcuate appliance at least in part in accordance with a series of digital values representing circle segment lengths and radii derived from the circle segments of the archform equation;

10 the appliance fabricating step includes the step of converting the segment lengths and radii to a series of NC commands to produce the machine code, and, in response to the code, sequentially forming the appliance to a radius corresponding to each segment length thereof in response to the machine code to conform to the designed appliance configuration.

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8. The method of claim 1 wherein:

the tooth measuring step includes the step of digitizing the distances between mesial and distal contact points for each tooth to define mesial-distal widths for each tooth;

the tooth finish position deriving step includes the step of deriving tooth finish positions to place adjacent mesial and distal contact points of adjacent teeth in mutual contact to form a tooth placement arch conforming in shape to the derived archform and approximately equal in length to the sum of the mesial-distal widths of the teeth placed thereon; and

the appliance configuration designing step includes the step of designing the appliance configuration in part from the mesial-distal widths and tooth placement arch.

9. The method of claim 1 wherein:

the measuring step includes the step of digitizing, for each tooth, tooth profile data in the form of a series of digitized data points representing the shape of the surface of the tooth at least along a profile thereof extending generally vertically and labial-lingually;

the connection point establishing step includes the step of locating an appliance connection point on the surface of each of the plurality of teeth along a profile thereof; and

the appliance configuration designing step includes the step of designing, from the series of digitized data points representing the shape of the surface of the teeth, the established connection points and the derived tooth positions.

10. The method of claim 1 wherein the archform deriving step includes the step of

comparing corresponding contralateral points on opposite sides of the archform and, on the basis of the comparison, and calculating a modified archform that is laterally symmetrical about its center; and

designing the appliance configuration based at least in part on the modified archform.

11. The method of claim 1 wherein the measuring step includes the step of digitizing data of points on labial and lingual surfaces of each of a plurality of the teeth of the patient, and the method further comprises:

deriving from the digitized labial and lingual surface data a digital representation of the orientation of a crown long axis of each tooth with respect to the points;

calculating finish positions of the teeth from the digitized data and the digital representations of the crown long axes of the teeth, the calculated finish positions including preferred crown long axis orientations.

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12. The method of claim 1 further comprising the steps of:

treating a plurality of patients while calculating the preferred crown long axis orientations and producing a record of the calculated preferred crown long axis orientations;

5 recording personal data of each of the treated patients, correlating the personal data with the calculated preferred crown long axis orientations and classifying the patients in population groups on the basis of the correlation; and

producing a statistical record of preferred crown long axis orientations for patients of the population groups.

13. The method of any one of claims 1-11 wherein:

the measuring step includes the step of measuring tooth shape data;

5 the appliance designing step includes the step of designing appliance placement jig configurations from the tooth shape data, each having a jig surface that will conform to the surface of a respective tooth for facilitating the location of the connection point thereon and the connection of the appliance thereto;

the machine code producing step includes the step of producing the machine code at least in part in accordance with the designed appliance placement jig configurations; and

10 the appliance fabricating step includes the step of automatically fabricating appliance placement jigs with the NC machine in response to the machine code to conform to the designed placement jig configurations.

14. The method of claim 13 wherein the appliance placement jig configuration designing step comprises the steps of:

5 calculating, from the digitized tooth shape data and defined connection points, jig geometry defining a jig locating surface that conforms to a unique portion of the external surface of the crown of a tooth, and defining an appliance engaging surface having the same location relative to the jig locating surface as the unique portion of the external surface has to the connection point on the tooth, so that, the NC machine, when operated in response to the control signal, will form a jig that, when fit on the tooth, will position and orient an appliance engaged thereby at the connection point of the tooth for connection thereto.

15. The method of claim 14 wherein:

the connection point defining step includes the step of calculating the connection points from the digitized tooth shape data; and

5 the jig geometry calculating step includes the step of defining the appliance engaging surface such that the location relative to the jig locating surface is the same as that of the unique portion of the external surface to the calculated connection point on the tooth.

- 71 -

16. The method of claim 14 wherein:

the appliance includes a plurality of brackets, one for connection at each connection point to a tooth, each bracket having an archwire receiving slot therein;

5 the appliance configuration design includes bracket shape data including a digital representation of the position and inclination of the slot in the bracket; and

the jig geometry calculating step includes the step of defining the appliance engaging surface to include a part thereof that will align with the slot of the bracket when the bracket is engaged thereby.

17. The method of claim 16 wherein:

the appliance configuration designing step includes the step of calculating bracket design to accommodate arcuate archwire shape.

18. The method of claim 16 wherein:

the appliance configuration designing step includes the step selecting, from a plurality of bracket blanks, an optimum blank for the manufacture of the bracket in accordance with slot digital representation.

19. A method of any one of claims 1-11 wherein:

5 the measuring step includes the step of measuring the shapes of individual upper and lower teeth and the shape of the lower jaw of the patient and producing thereby digitized upper and lower tooth data and lower jaw shape data, the tooth shape data including data of the incisal tips of the lower anterior teeth and buccal cusp tips of lower posterior teeth and central ridge or marginal ridge locations of upper posterior teeth;

the finish position deriving step includes the steps of:

10 deriving a tooth-bearing lower jaw configuration based on assembly of the lower teeth along the lower arch configuration with adjacent teeth in contact with each other and the lower arch configuration;

vertically adjusting each lower tooth such that the incisal tips of the lower anterior teeth and buccal cusp tips of the lower posterior teeth are in substantially the same occlusal plane and are inclined at controlled angles of inclination;

15 adjusting the tooth-bearing lower arch configuration to provide a finished tooth bearing lower jaw configuration by labially-lingually positioning the lower teeth to place the incisal and buccal cusp tips thereof in a smooth arch in the occlusal plane with adjacent teeth in contact with each other; and

deriving a tooth-bearing finished upper tooth configuration in which:

20 the posterior teeth have their central grooves or marginal ridges lying horizontally on the finished tooth bearing lower jaw configuration and vertically on the occlusal plane;

- 72 -

the anterior teeth have their incisal tips positioned below the occlusal plane to achieve predetermined overlaps and are horizontally labially offset from the finished tooth bearing lower jaw configuration so as to establish a predetermined clearance between the lower anterior teeth lingual faces and the labial faces of the lower anterior teeth;

25

the appliance configuration designing step includes the step of calculating a bracket configuration, including bracket slot angle and bracket slot depth, for individual upper and lower tooth brackets, and calculating upper and lower archwire shapes, based upon the calculated finished tooth positions, predetermined upper and lower archwire planes, the tooth shapes, and the positions of the brackets on the teeth;

30

the appliance fabricating step includes the steps of:

fabricating the upper and lower archwires to conform to the calculated archwire shapes; and

fabricating the brackets to conform to the calculated bracket configurations.

20. The method of any one of claims 1-11 further comprising the steps of:

providing criteria describing the distances of the individual teeth from the pivot axis of the lower jaw;

the finish position deriving step includes the steps of:

5

calculating from the criteria and the tooth shape data a component of cuspid rise; and vertically adjusting the upper and lower cuspids such that their cusp tips are respectively below and above the occlusal plane a distance that has a predetermined relationship to the calculated cuspid rise.

21. The method of claim 20 wherein the tooth-bearing finished upper tooth configuration deriving step includes deriving the configuration in which:

the upper anterior teeth have incisal tips positioned below the occlusal plane so as to achieve predetermined overlaps that have a predetermined relationship to the calculated cuspid rise.

5

22. The method of claim 20 wherein the cuspid rise component calculating step includes the steps of:

identifying occluding pairs of respective upper and lower posterior teeth of the patient, and determining for each pair from the digitized tooth shape data a vertical distance from the highest extent of the lower tooth of the pair to the lowest extent of the upper tooth of the pair when the jaws are in a closed position;

5

adjusting each determined vertical distance by a factor proportionally related to a distance of each pair from the pivot axis, and selecting the largest adjusted vertical distance

- 73 -

10 calculating, from the digitized data, finish positions of the mandibular teeth of the patient
at which highest points thereon are at vertical positions on an approximately flat occlusal surface;
and

calculating finish positions of the upper and lower cuspids of the patient extend
respectively below and above the occlusal surface.

23. The method of any one of claims 1-11 further comprising the steps of:

providing an orthodontic appliance designing and manufacturing system including:

a data input sub-system for digitizing input data of measured anatomical shapes and
generating input signals carrying the digitized input data,

5 a data processing sub-system for processing the digitized input signals and generating,
in response thereto, output signals carrying the machine control code, and

an NC appliance hardware manufacturing sub-system, including the NC machine, for
fabricating, in response to the output signals, a custom orthodontic appliance for the treatment
of the patient by moving the teeth of the patient to the preferred finish positions;

10 generating, with the data processing sub-system, from the derived archform, output signals
carrying numerical machine control code for operating the NC appliance hardware manufacturing
sub-system to fabricate the custom orthodontic appliance; and

15 fabricating, with the NC appliance hardware manufacturing sub-system, in response to
the output signal and in accordance with the numerical machine control codes, the custom
orthodontic appliance of the custom configuration.

24. The method of claim 23 wherein:

the custom orthodontic appliance includes an archwire having an arcuate shape that is
mathematically related to the mandibular trough skeletal archform;

5 the NC appliance hardware manufacturing sub-system includes a wire bending apparatus
responsive to numerical machine control codes carried by the output signal;

the output signal includes a series of codes for operating the wire bending apparatus to
feed a wire and to bend the fed wire into the custom archwire configuration for connection of
the archwire to the teeth of a jaw at a respective connection points.

25. The method of claim 24 wherein:

the digitized input data contains information from which the connection point of the
appliance and slope of the surface at the connection point can be derived;

5 the custom orthodontic appliance includes a plurality of brackets, one for each tooth
connection point, each having a base securable to the respective connection point, and each
having an archwire slot connectable to the archwire;

- 74 -

the NC appliance hardware manufacturing sub-system includes a bracket fabricating apparatus responsive to numerical machine control codes carried by the output signal;

10 the output signal includes a series of codes for operating the bracket fabricating apparatus to fabricate each bracket with the archwire slot positioned with respect to the base to support and orient a point on the archwire with respect to the connection point of the respective tooth to transfer force therebetween to urge the tooth toward its finish position.

26. The method of claim 25 wherein:

the digitized input data contains information of a contour on the surface of the tooth;

5 the custom orthodontic appliance includes a bracket placement jig for each bracket having a surface for uniquely positioning the jig with respect to the surface of the tooth and for positioning the bracket thereon at the connection point thereof;

the NC appliance hardware manufacturing sub-system includes a bracket placement jig fabricating apparatus responsive to numerical machine control codes carried by the output signal;

the output signal includes a series of codes for operating the bracket placement jig fabricating apparatus to fabricate the bracket placement jig.

27. The method of claim 25 wherein the appliance fabricating step includes the steps of:

providing a plurality of bracket blanks; and

5 forming a bracket from the bracket blank by forming an archwire slot in each of the bracket blank such that each slot will lie in an archwire plane when the bracket is mounted on the connection point of a tooth with the tooth in its derived finish position.

28. The method of claim 27 wherein:

the bracket slot cutting step includes the step of forming the slot to a depth defined by the intersection of the appliance archform equation with the bracket, when the bracket is mounted on the connection point of a tooth with the tooth in its derived finish position; and

5 the bracket slot cutting step includes the step of forming the slot to a slot bottom curvature of the radius of the intersecting circle segment of the appliance archform equation.

29. The method of any one of claims 1-11 wherein the connection position establishing step includes, to provide optimal spacing thereof from the gums of a patient and clearance with teeth of the opposite jaw of the patient, the steps of:

5 digitizing data of shapes of the teeth of the patient and of geometry of parts of an appliance to be connected thereto;

calculating from the digitized data finish positions of the teeth of the patient and the relationships of between points on surfaces of teeth of the opposite jaws;

- 75 -

calculating from the digitized data locations on the surfaces of the teeth of one jaw of the patient at which the appliance is to be connected to provide optimal spacing thereof from the gums of a patient and clearance with teeth of the opposite jaw of the patient; and
10 designing the appliance configuration in accordance with the calculated locations for connection of the appliance to the teeth of the patient.

30. A method of any one of claims 1-11 wherein:
the custom orthodontic appliance includes an archwire;
the appliance configuration designing step includes the step of deriving digital archwire shape data based at least in part on the the derived archform;
5 the machine code producing step includes the step of generating a wire shape control signal in response to the digital archwire shape data, such that, when communicated to an archwire former, the former will produce a custom orthodontic archwire based on the anatomical shapes from the individual patient's mouth; and
forming a length of orthodontic archwire material into a controlled shape in response to
10 the wire shape control signal to produce the custom archwire.

31. The method of claim 30 wherein the machine code producing step includes the steps of:
providing archwire material property data of the archwire material; and
generating the wire bending control signal in response to the material property data of the
5 archwire material.

32. The method of claim 30 further comprising the steps of:
measuring an archwire span between two points on the produced custom orthodontic archwire;
calculating a design archwire span from the derived archwire shape data;
5 comparing the measured archwire span with the design archwire span and signaling a result of the comparison; and
generating the wire bending control signal in response to the signaled result of the comparison.

33. A custom orthodontic appliance fabricating apparatus comprising:
means for measuring anatomical shapes from the mouth of the patient, and producing thereby digitized anatomical shape data;
a digital computer including program means for:
5 deriving an archform from the digitized data with a specially programmed digital computer;

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10 deriving tooth finish positions from the digitized data and the derived archform;
designing, from the digitized data, established appliance connection points and the
derived tooth finish positions, an appliance configuration such that a custom appliance
fabricated in accordance therewith and connected at the appliance connection points to the
teeth, will exert substantially no tooth moving forces on the teeth when in the derived
tooth finish positions, and will otherwise urge the teeth toward the derived finish
positions; and
15 producing machine code in accordance with the designed appliance configuration; and
an machine for automatically fabricating a custom orthodontic appliance in response to
the machine code to conform to the designed appliance configuration.

34. The apparatus of claim 33 wherein the fabricating machine comprises:
an archwire former including means for forming a length of orthodontic archwire material
into a controlled shape in response to a wire shape control signal communicated thereto; and
the program means including means for generating a wire shape control signal in response
5 to the digital archwire shape data, such that, when the signal is communicated to the archwire
former, the former will produce a custom orthodontic archwire conforming to the anatomical
shape of the individual patient's mouth.

35. The apparatus of claim 34 wherein:
the derived digital archwire shape data includes wire length data correlated to a length
component of the derived digital archwire shape data and wire curvature data correlated to a
curvature component of the derived digital archwire shape data that is a function of the length
5 component;
the wire shape control signal includes a wire feed control signal carrying the wire length
data and a wire bending control signal carrying the wire curvature data;
the program means includes means for generating the wire feed control signal and means
for generating a wire bending control signal and communicating the control signals to the
10 archwire former; and
the archwire former includes means for longitudinally feeding the orthodontic archwire
material in response to the wire feed control signal and means for transversely bending the
archwire material fed by the wire feeding means in response to the wire bending control signal
and in synchronism with the feeding of the archwire material.

36. The apparatus of claim 34 wherein:
the digital archwire shape data is a digital representation of a connected series of wire
segments, each having a length component and a curvature component; and

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5 the archwire former includes means for longitudinally feeding a series of lengths of the orthodontic archwire material corresponding to the respective wire length components in accordance with the wire length data and means for bending each fed length of archwire material to a curvature corresponding to the respective wire curvature component in accordance with the wire curvature data.

37. The apparatus of claim 36 wherein:

5 each wire segment is in the form of a circle segment with the length component thereof representing a tangential length of archwire material and with the curvature component thereof representing a constant radius of curvature of the material over the tangential length of the segment; and

the feeding means includes means for longitudinally feeding a series of tangential lengths of the orthodontic archwire material and the bending means includes means for bending each fed length of archwire segment to a constant radius in accordance with the wire curvature data.

38. The apparatus of claim 37 wherein:

5 the feeding means is operative to sequentially feed a series of lengths of the archwire material equal to the length components of the circle segments, in response to the wire feed signal, along a longitudinal path;

the bending means includes a bending element moveable in response to the wire bending signal transverse to the path to impart a transverse bending deflection to the segment and a transverse position sensor for producing a feedback signal responsive to the deflection; and

the computer includes means for modifying the wire bending control signal in response to the feedback signal to provide closed loop control of the bending element.

39. The apparatus of claim 34 wherein:

5 the program means includes means in communication with the wire shape control signal generating means for receiving material property data of the archwire material and for modifying the wire bending control signal in accordance with the property data to compensate for elastic properties of the material.

40. The apparatus of claim 34 further comprising:

means for measuring an archwire span between points on first and last segments of the series of the produced custom orthodontic archwire;

5 the program means including means for calculating a design archwire span from the derived archwire shape data;

means for comparing the measured archwire span with the design archwire span and for storing the results of the comparison; and

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the program means being operative to generate the wire shape control signal in response to a stored result of the comparison.

41. The apparatus of any one of claims 33-40 wherein the fabricating machine comprises::

a bracket forming apparatus including:

a holder having means thereon for mounting a bracket blank thereon for fabrication;

5 means for forming at least one surface of a bracket blank mounted on the holder in response to a machine control signal communicated thereto in response to the control signal including means for shaping the bracket blank mounted on the holder to produce a bracket having a slot of a calculated geometric relationship to the mounting surface of the bracket base thereof.

42. The apparatus of claim 41 wherein:

each slot includes generally parallel upper and lower sides defining a slot inclination and includes a slot base at an end thereof nearest the bracket base defining a slot position;

5 each calculated geometric relationship of a slot to the mounting surface of a bracket includes the slot inclination and a slot position relative to the mounting surface;

the generated machine control signal carries machine control instructions for causing the forming means to shape the bracket blank to produce a bracket having a slot of the calculated slot inclination and slot position with respect to the mounting surface;

10 the slot of each bracket is adapted to receive an archwire having a custom curvature adjacent the tooth on which the bracket is to be secured;

each calculated geometric relationship of a slot to the mounting surface of a bracket includes a slot bottom curvature conforming to the custom curvature of the archwire adjacent thereto; and

15 the generated machine control signal carries machine control instructions for causing the forming means to shape the bracket blank to produce a bracket having a slot of the calculated slot bottom curvature.

43. The apparatus of claim 41 wherein:

the forming means includes means for cutting a slot in the support in response to the control signal.

44. The apparatus of claim 41 wherein:

the holder and the forming means are mounted on a stand; and

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the apparatus further comprises means for angularly orienting the holder with respect to the stand and to the forming means, and means for translating the cutting means with respect to the stand and to the holder, in response to the control signal.

45. The apparatus of claim 33 wherein:

the fabricating machine comprises: a jig former including means for forming a jig for positioning a custom orthodontic appliance on a tooth of a patient, including means for shaping the contours of a surface of blank of jig forming material in response to a control signal communicated thereto;

the measuring means includes means for providing a digitized record of the shapes of the teeth of a patient and of the locations relative to the tooth shape record of appliance connection points on surfaces of the teeth;

the program means includes means for calculating, from the digitized tooth shape and connection point record, jig geometry defining a jig locating surface that conforms to a unique portion of the external surface of the crown of a tooth, and defining an appliance engaging surface having the same location relative to the jig locating surface as the unique portion of the external surface has to the connection point on the tooth; and

the generating means includes means for generating a machine control signal carrying machine control instructions for producing a jig in accordance with the calculated jig geometry.

46. The apparatus of claim 45 wherein:

the appliance includes a plurality of brackets, one for connection at each connection point to a tooth;

the apparatus further comprises means for providing digitized bracket shape data of an external surface of each bracket to be connected to a connection point; and

wherein the jig geometry calculating means includes means for defining the appliance engaging surface of the jig to conform, in response to the digitized bracket shape data, to the established appliance geometry.

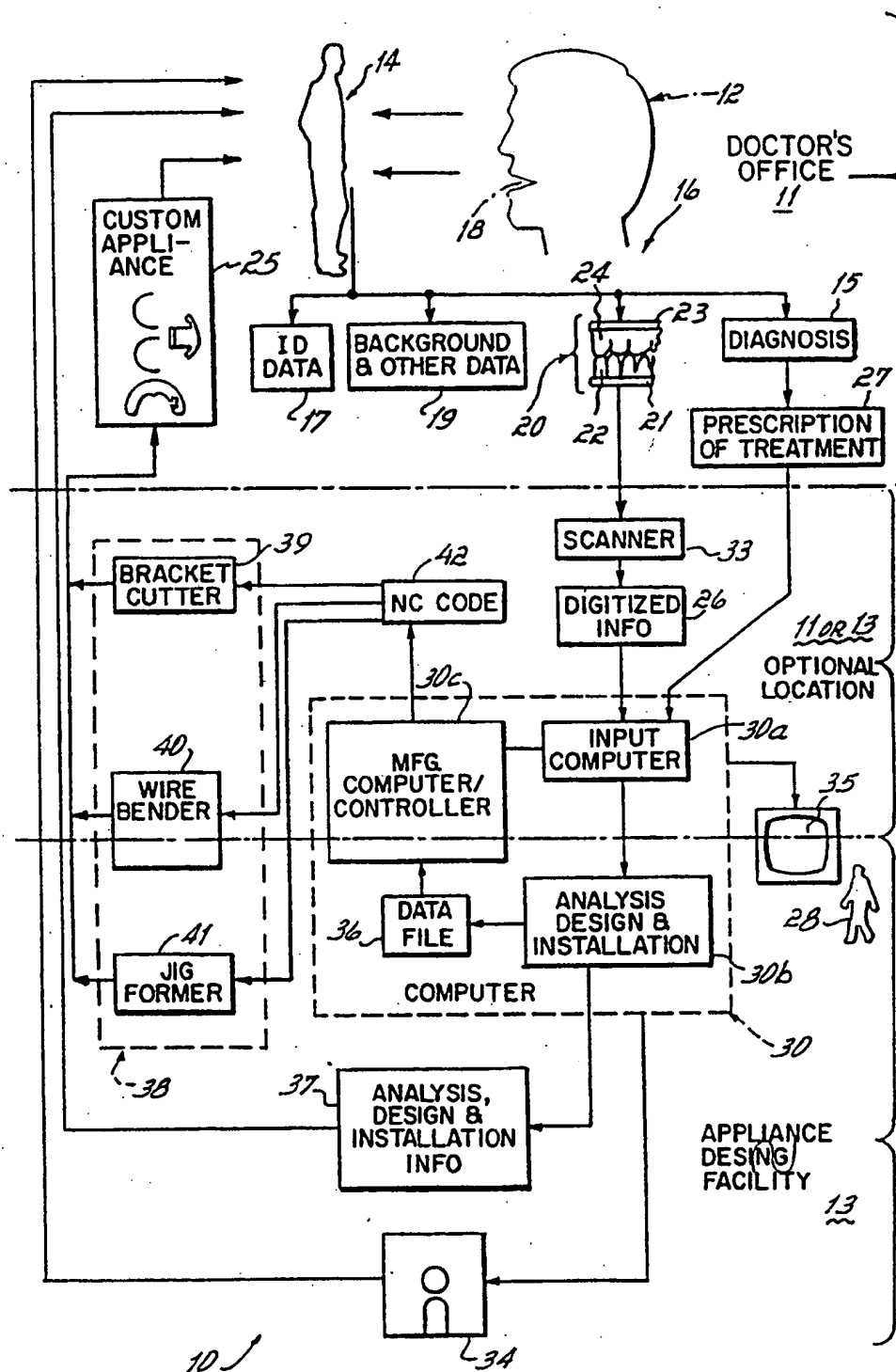


FIG. 1

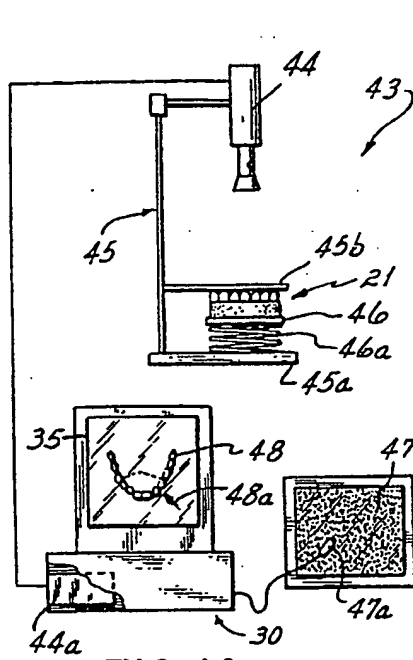


FIG. IA

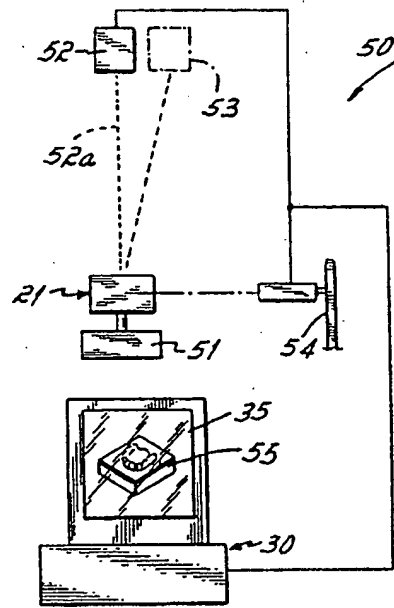


FIG. IB

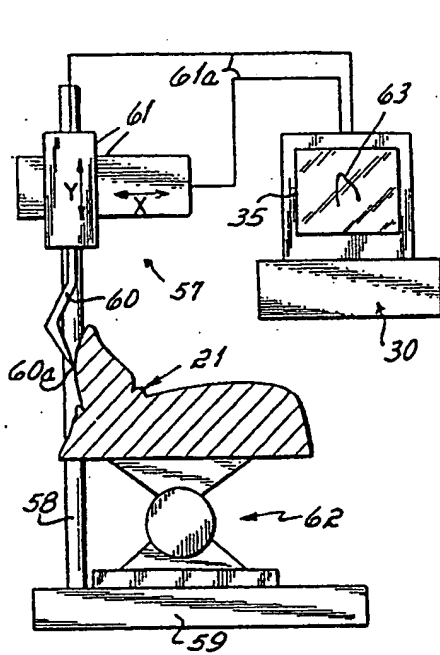


FIG. IC

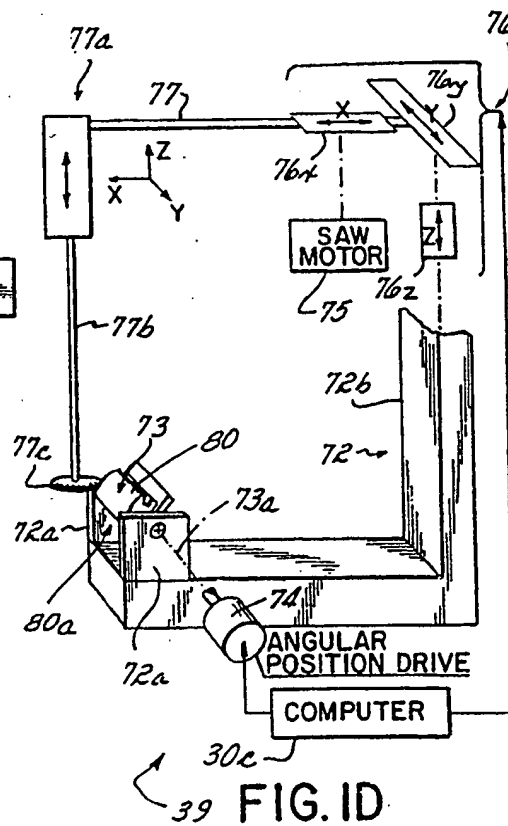


FIG. ID

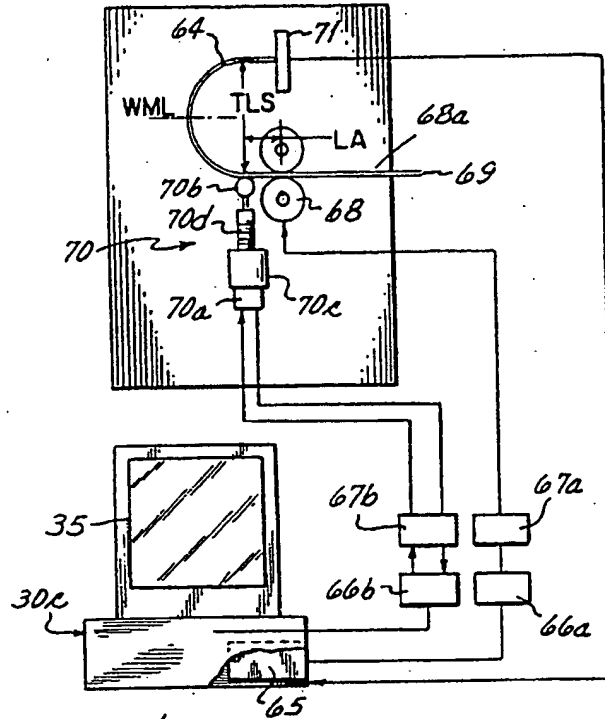


FIG. IE

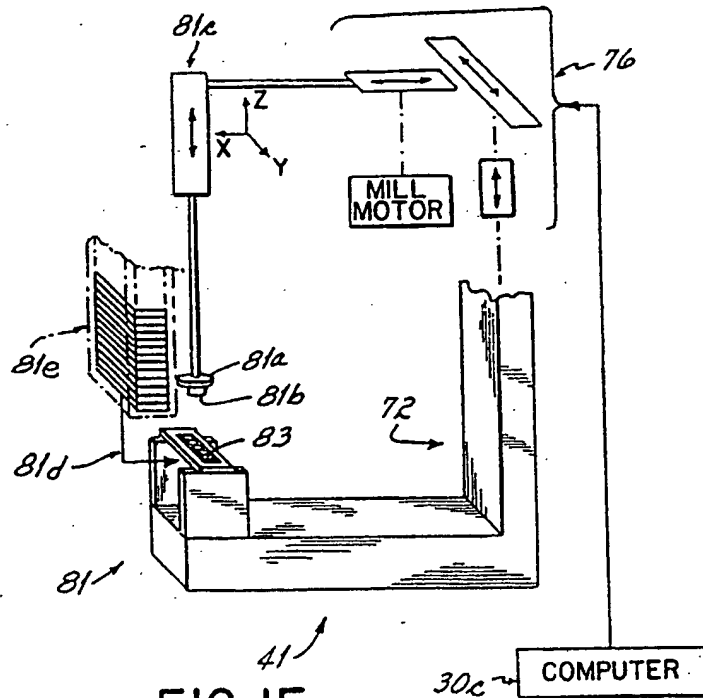


FIG. IF

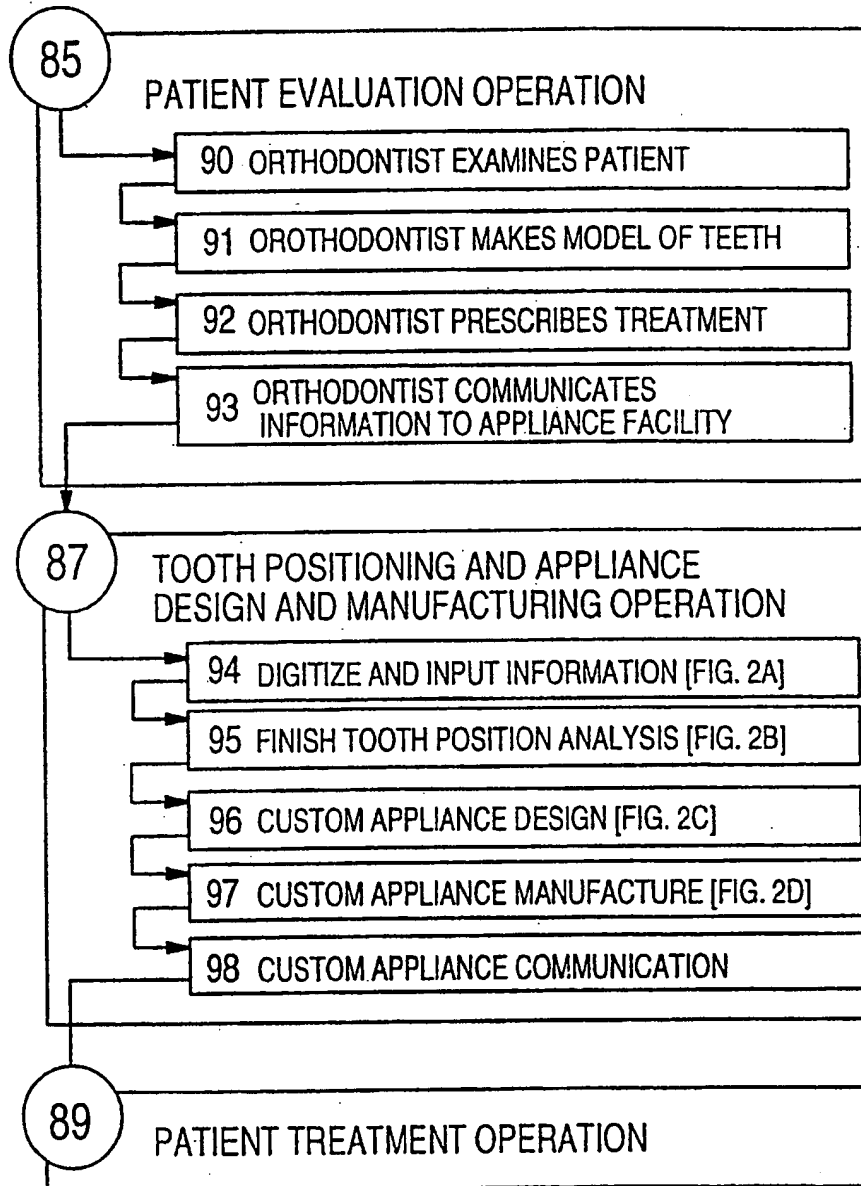


FIG. 2

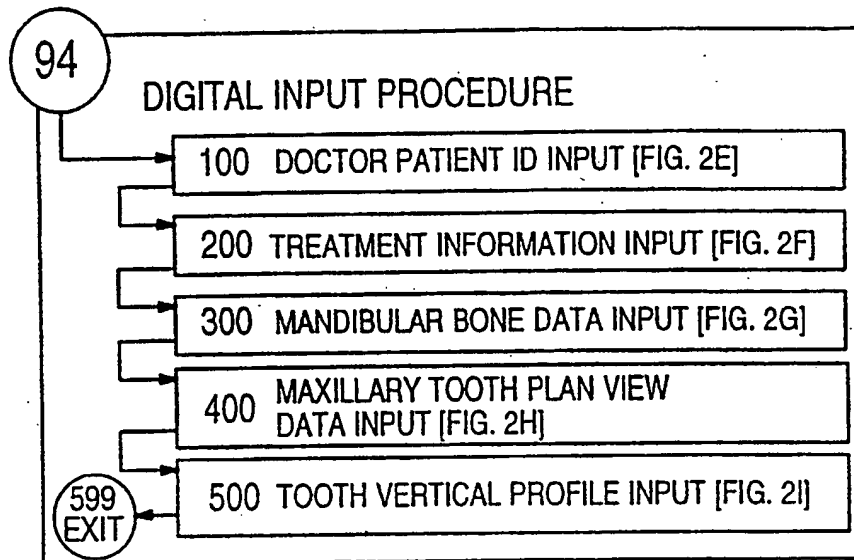


FIG. 2A

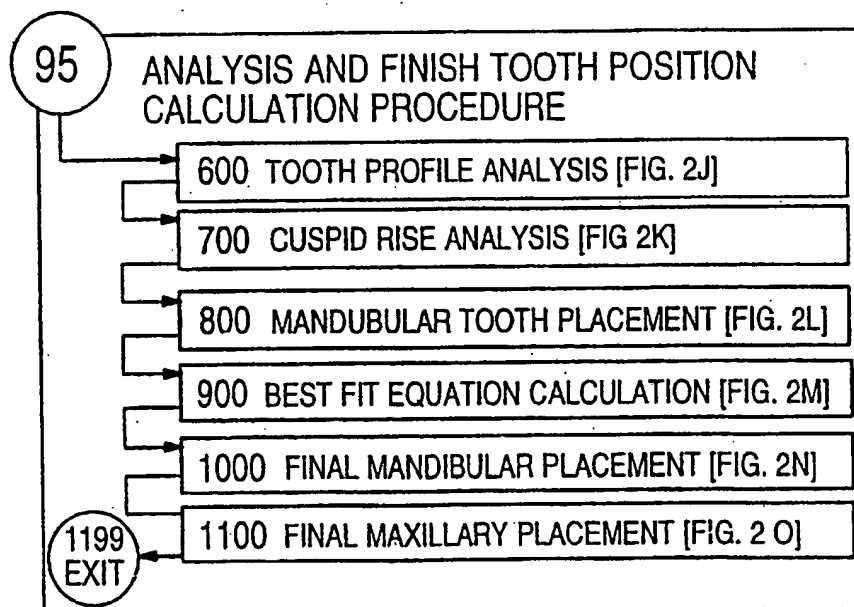


FIG. 2B

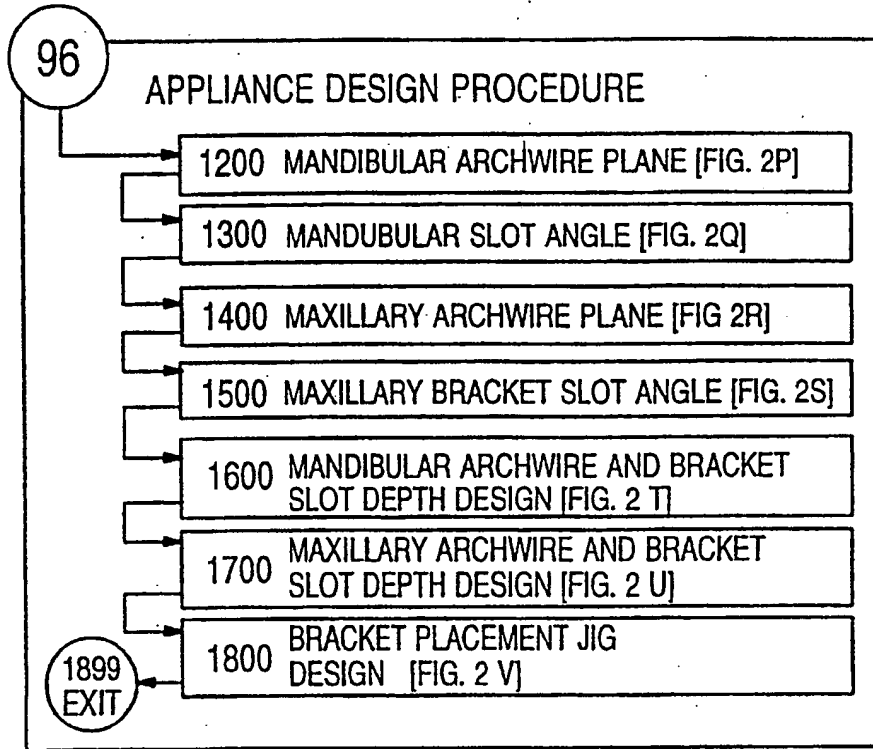


FIG. 2C

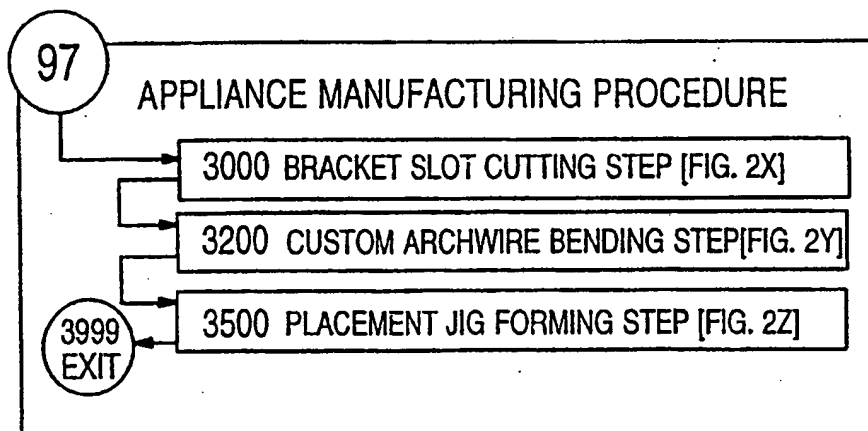


FIG. 2D

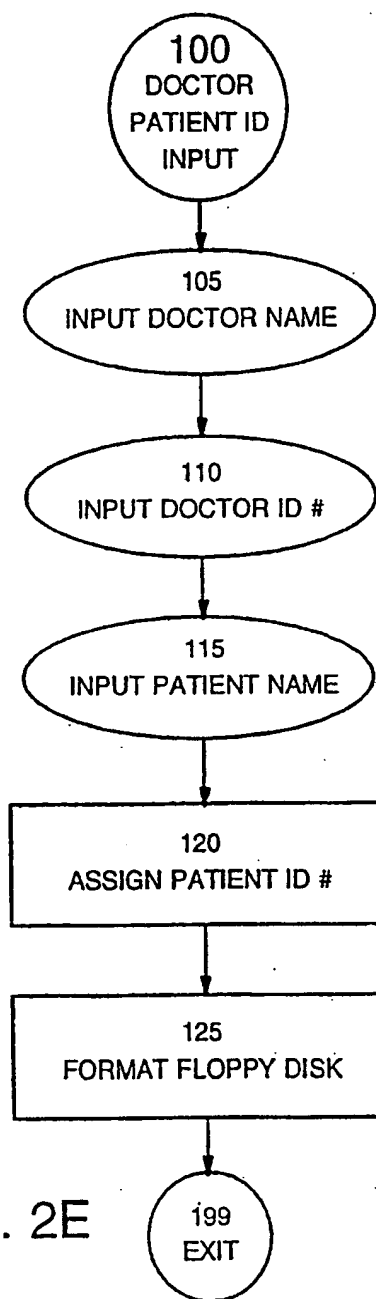
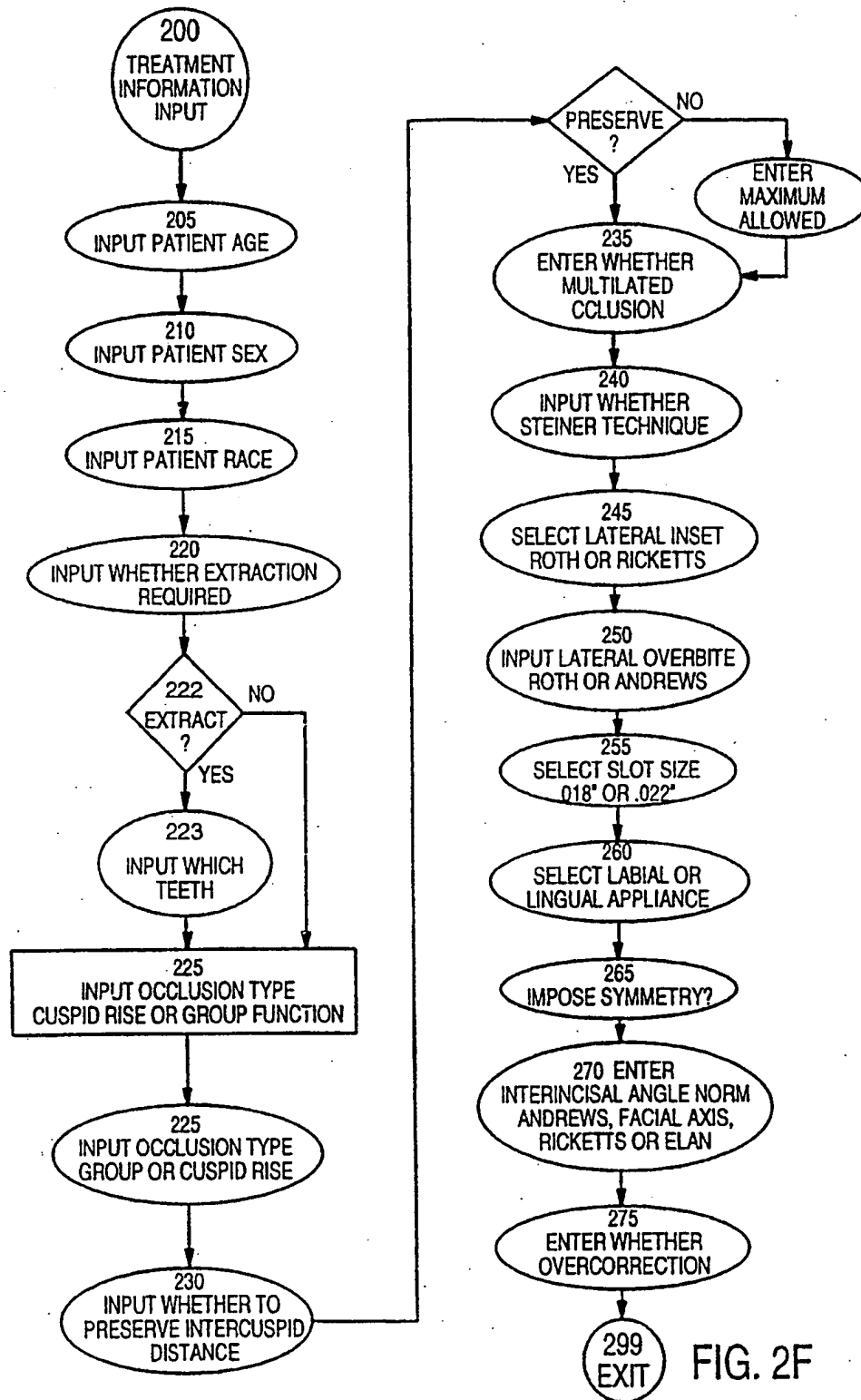


FIG. 2E



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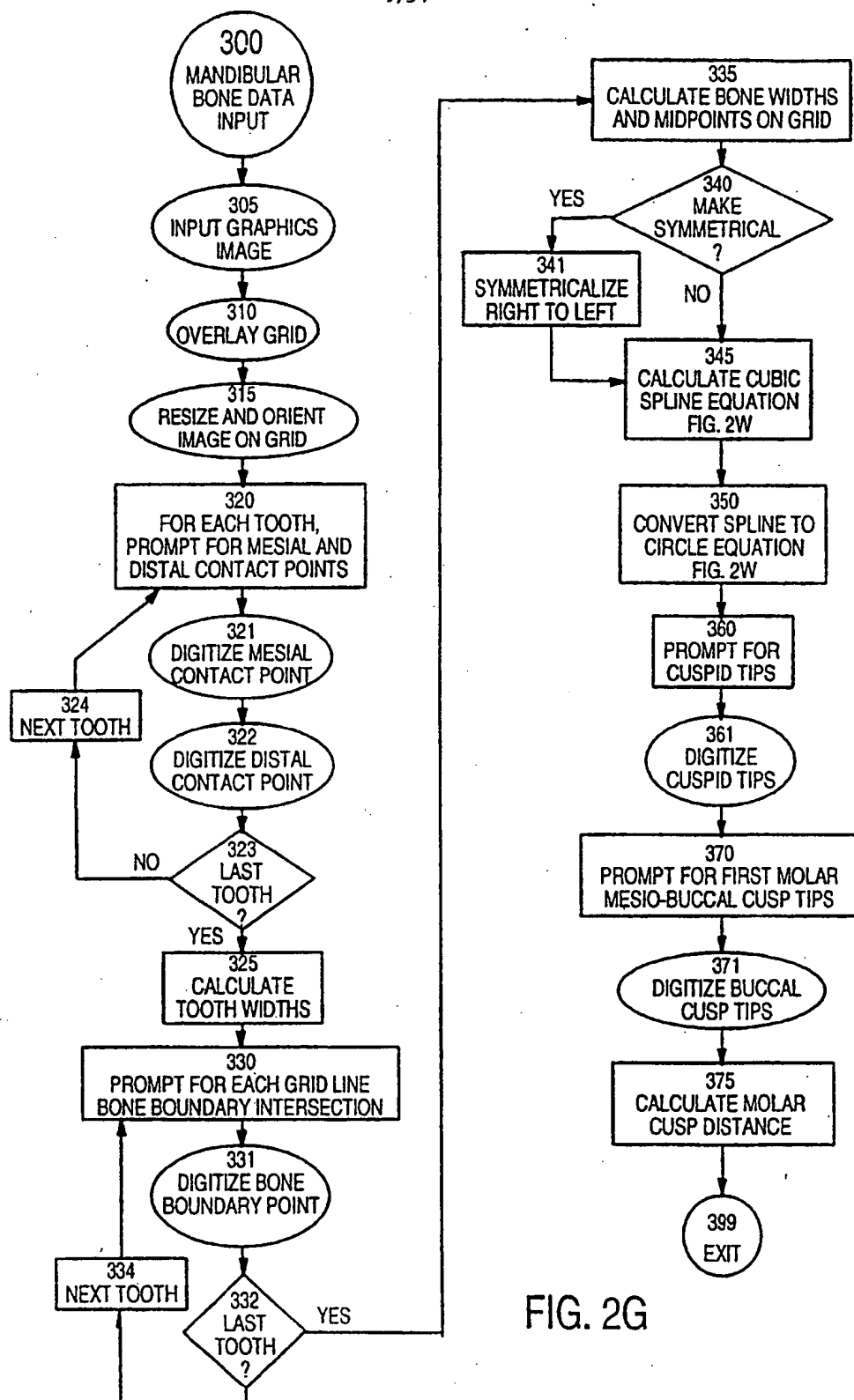
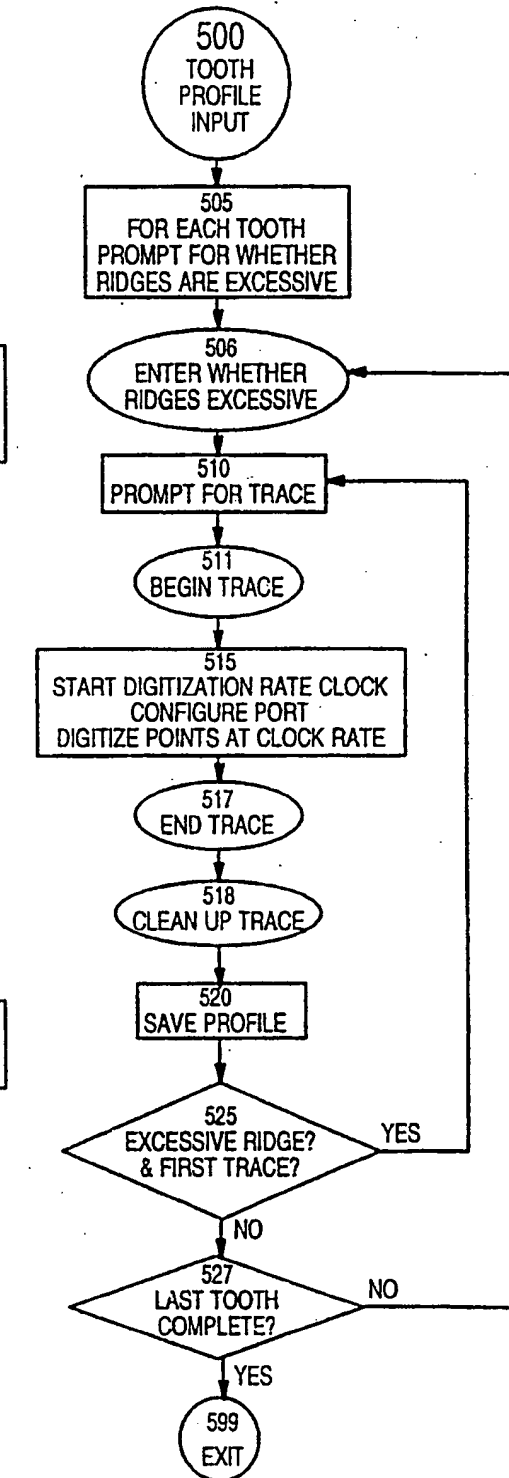
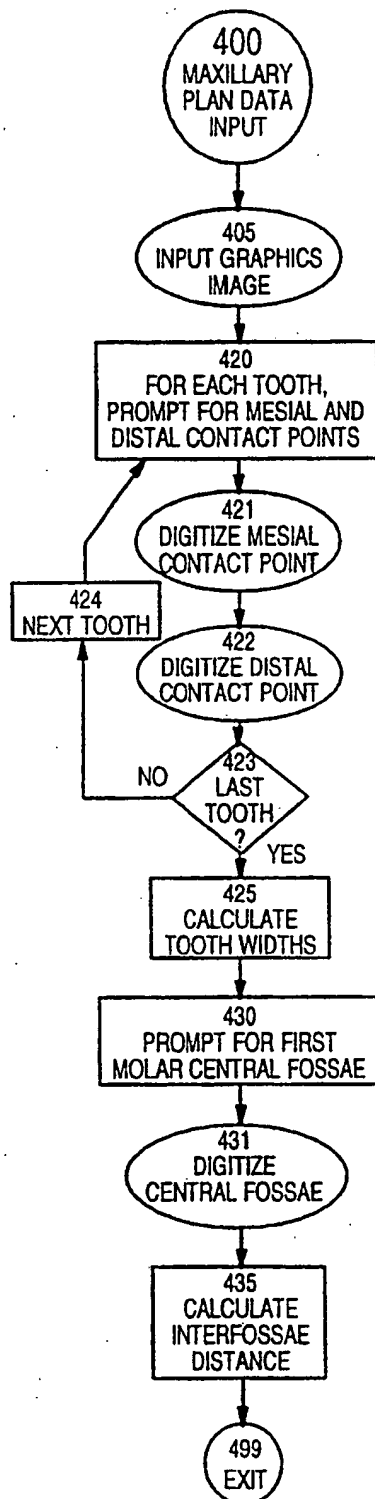


FIG. 2G

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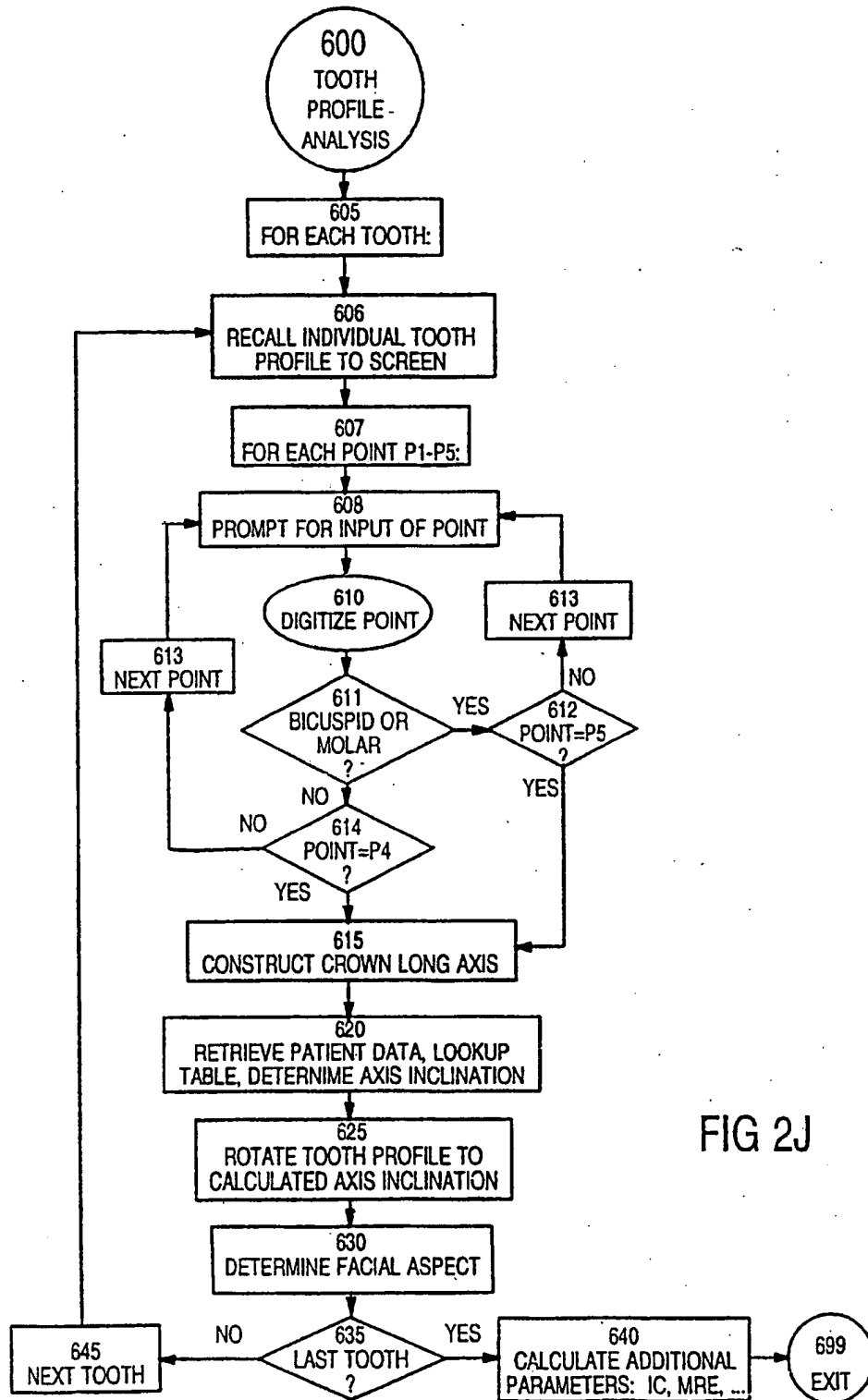


FIG 2J

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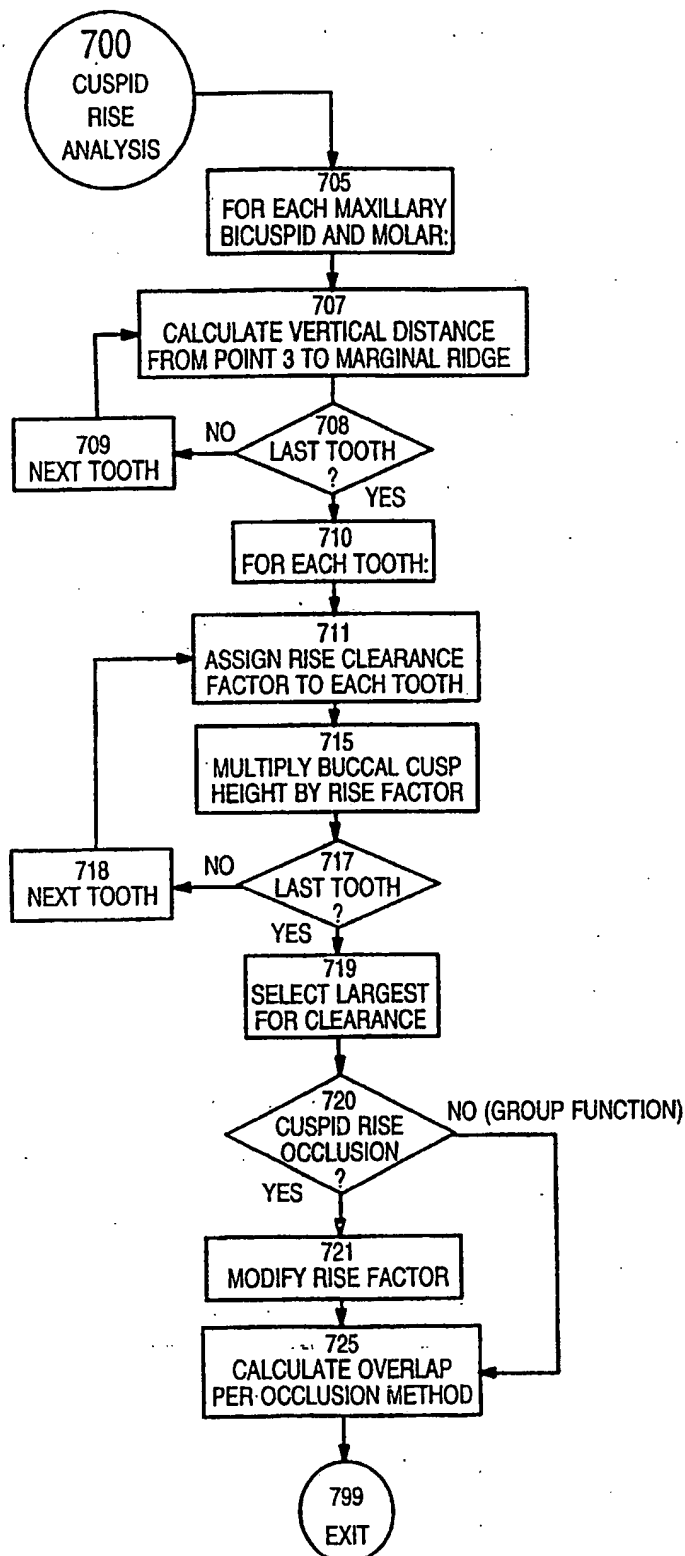


FIG. 2K

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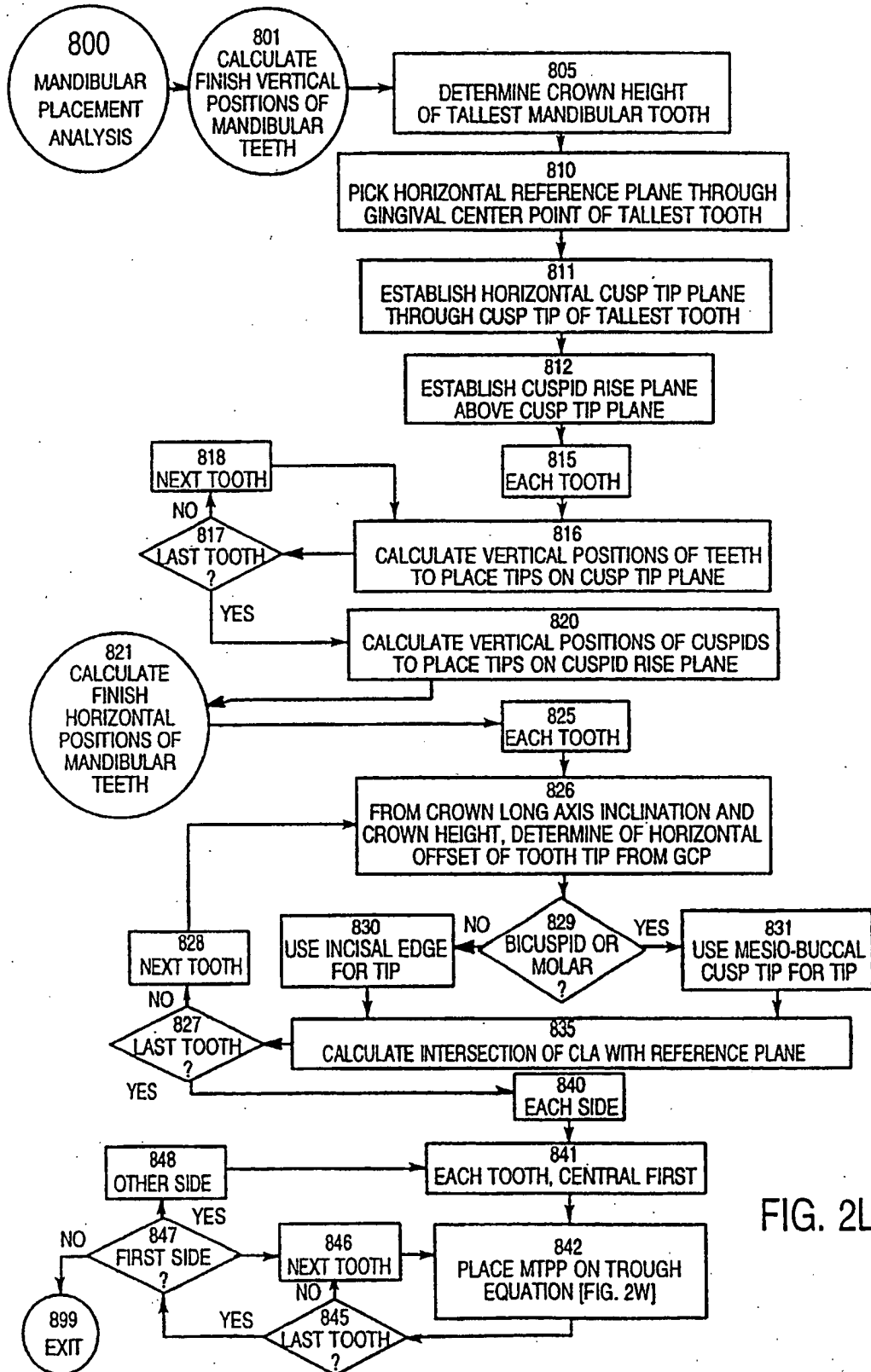


FIG. 2L

FIG. 2M

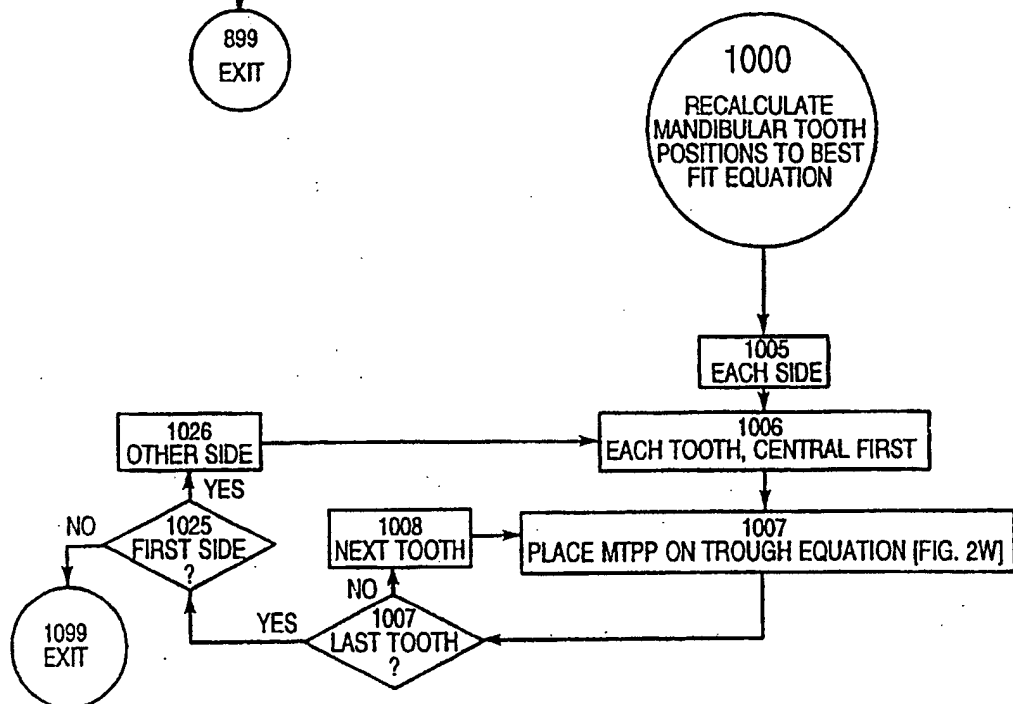
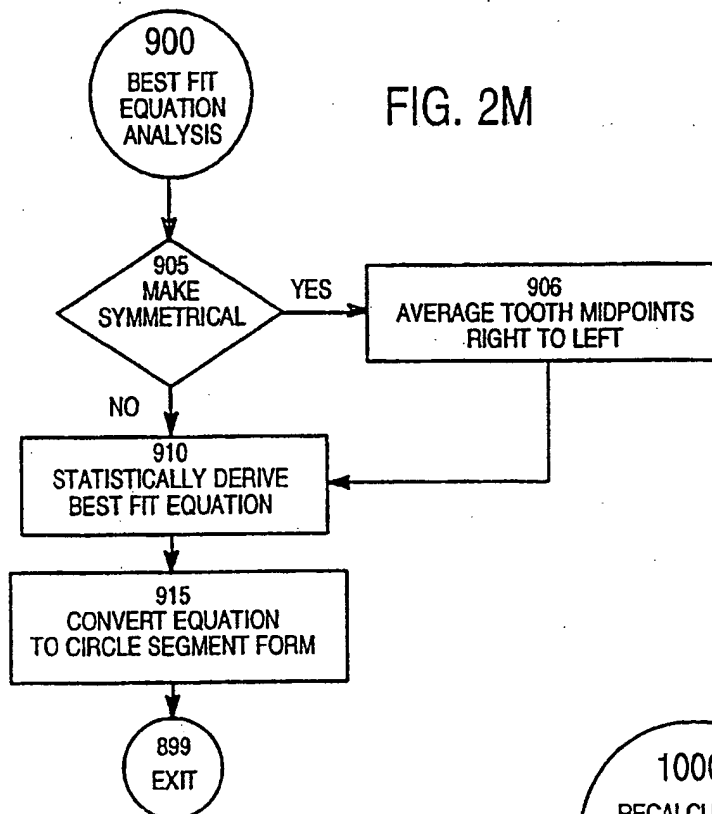


FIG. 2N

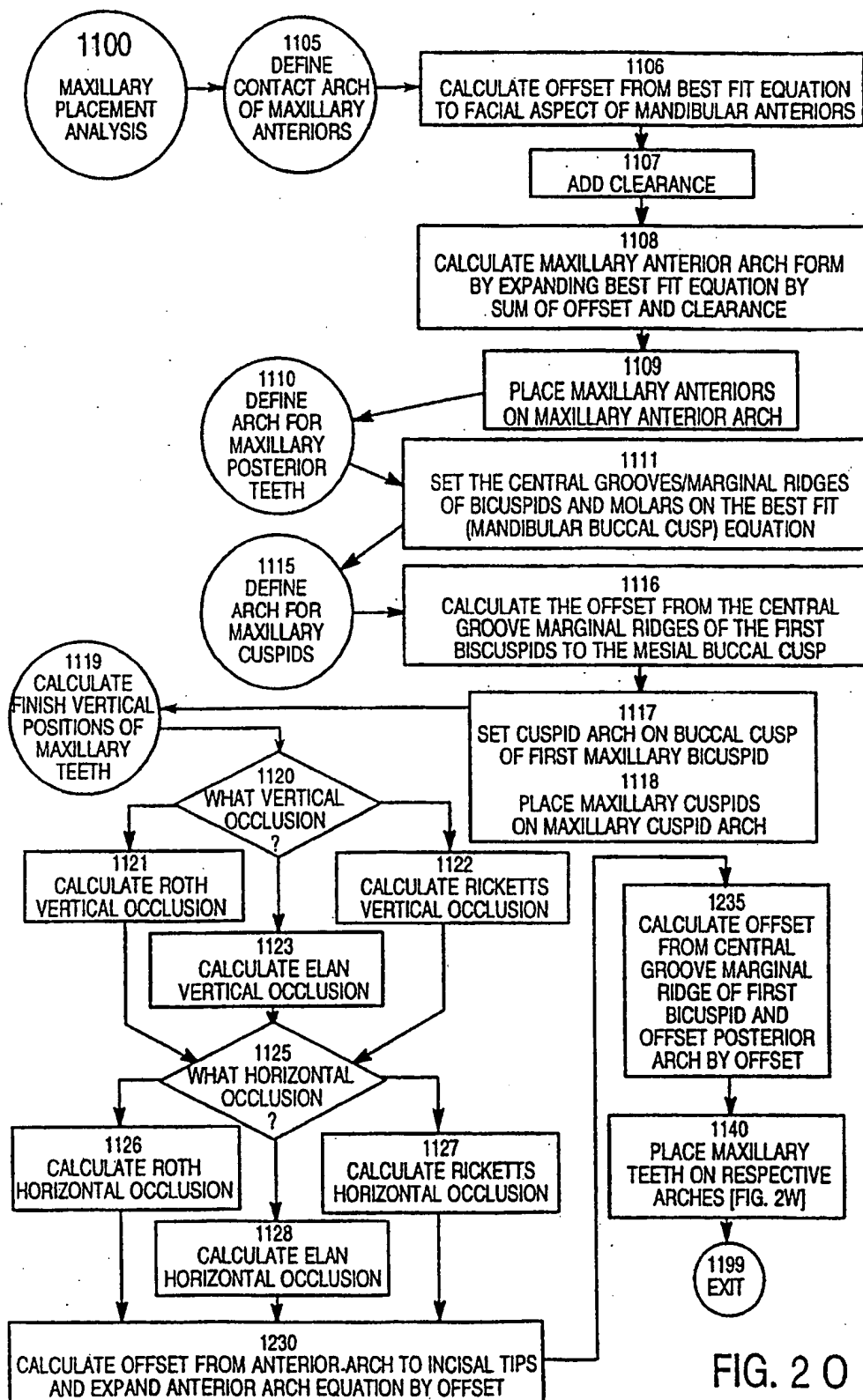


FIG. 2 O

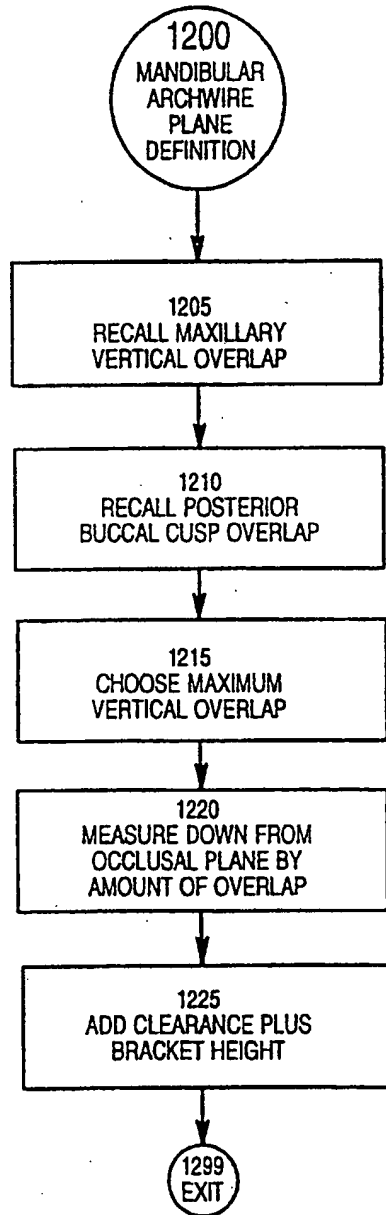


FIG. 2P

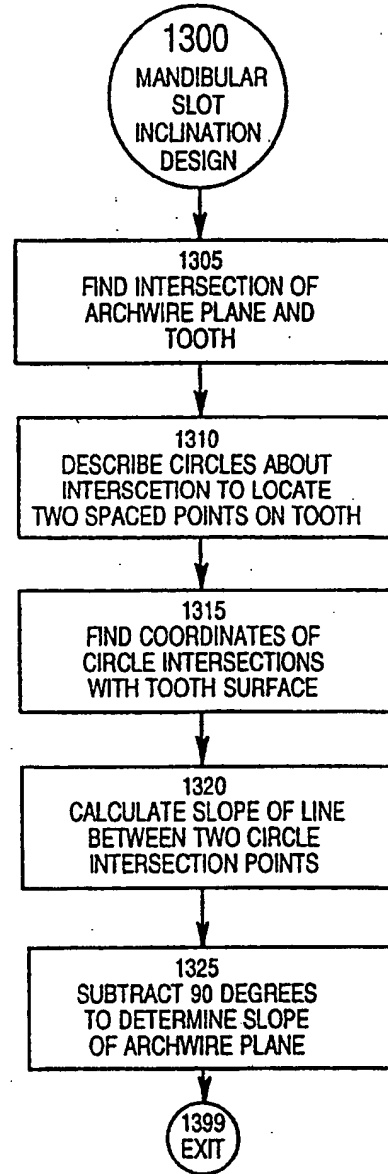


FIG. 2Q

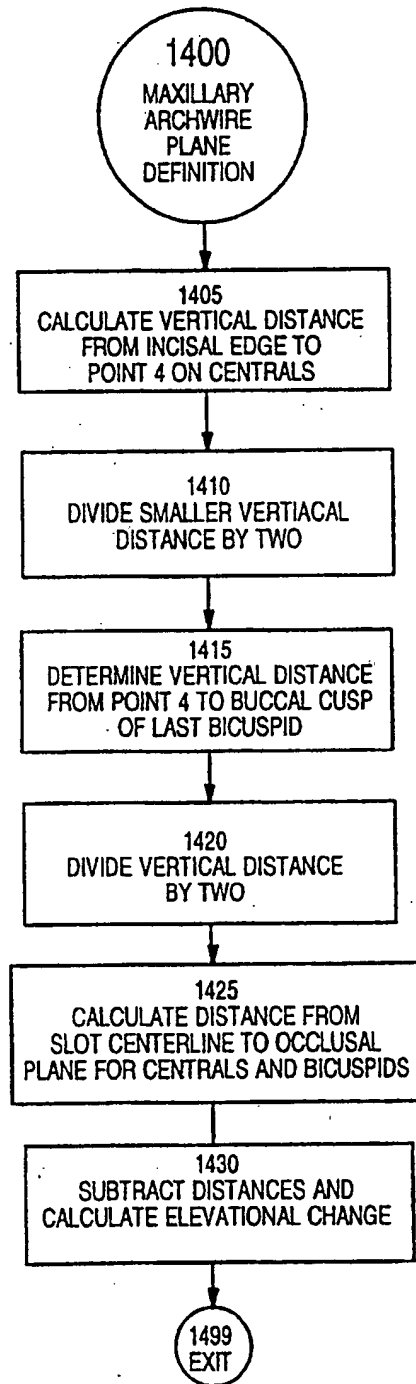


FIG. 2R

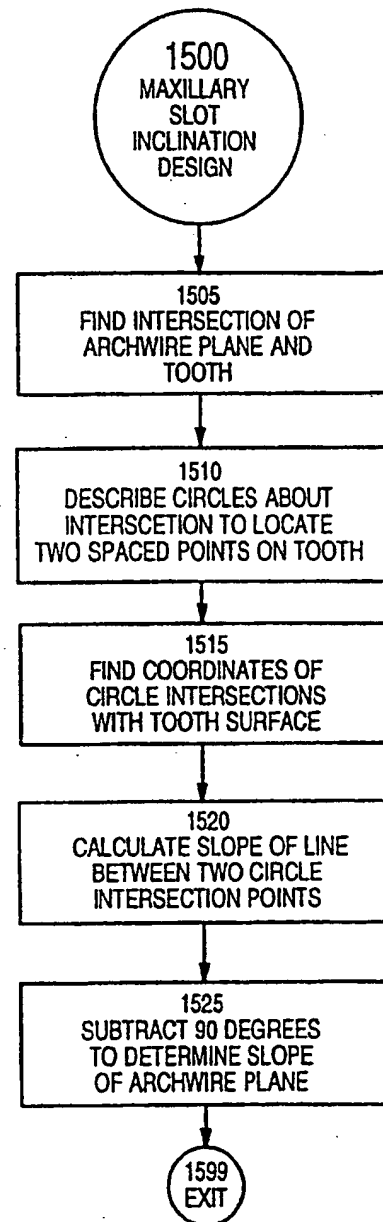


FIG. 2S

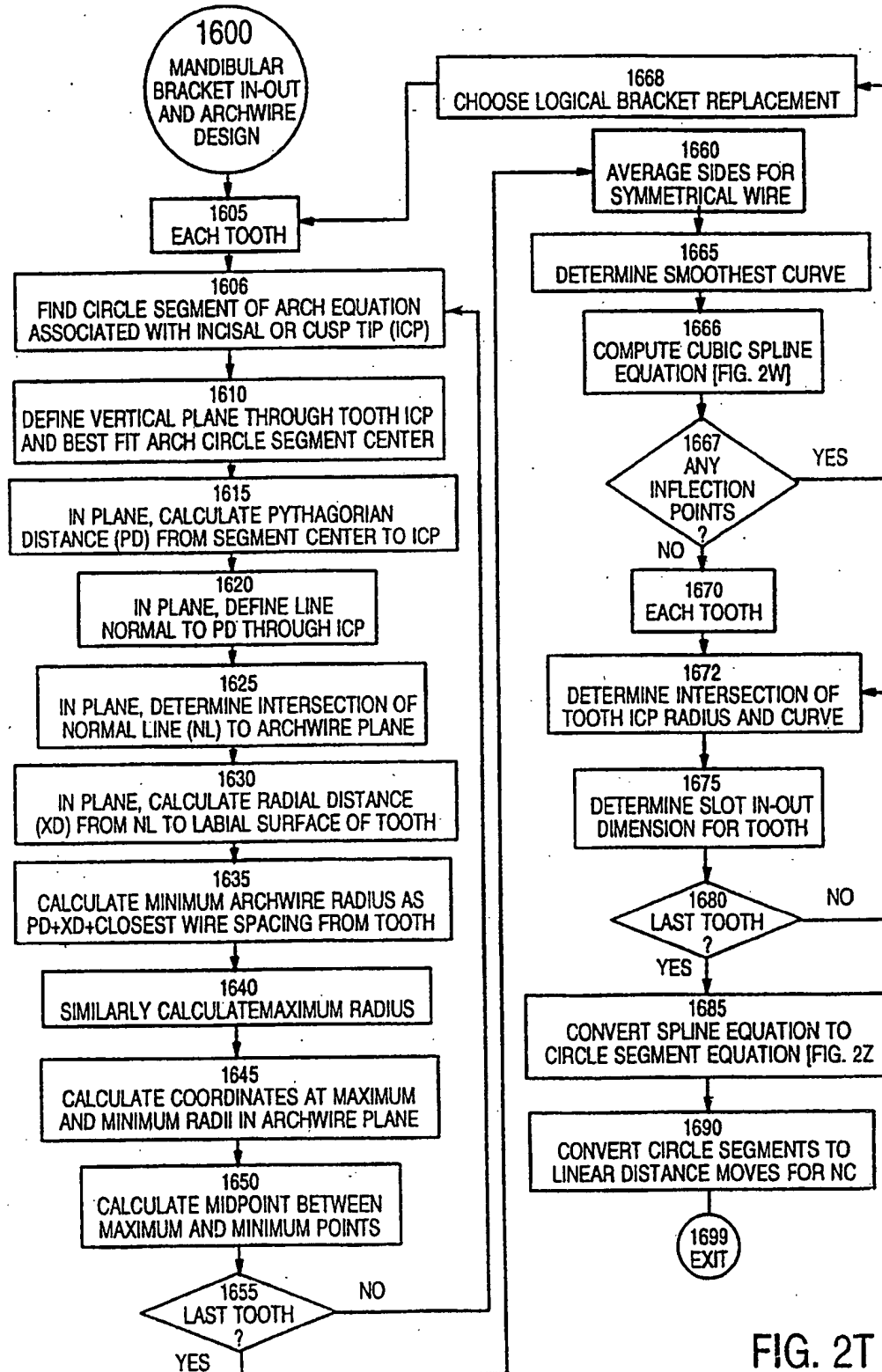


FIG. 2T

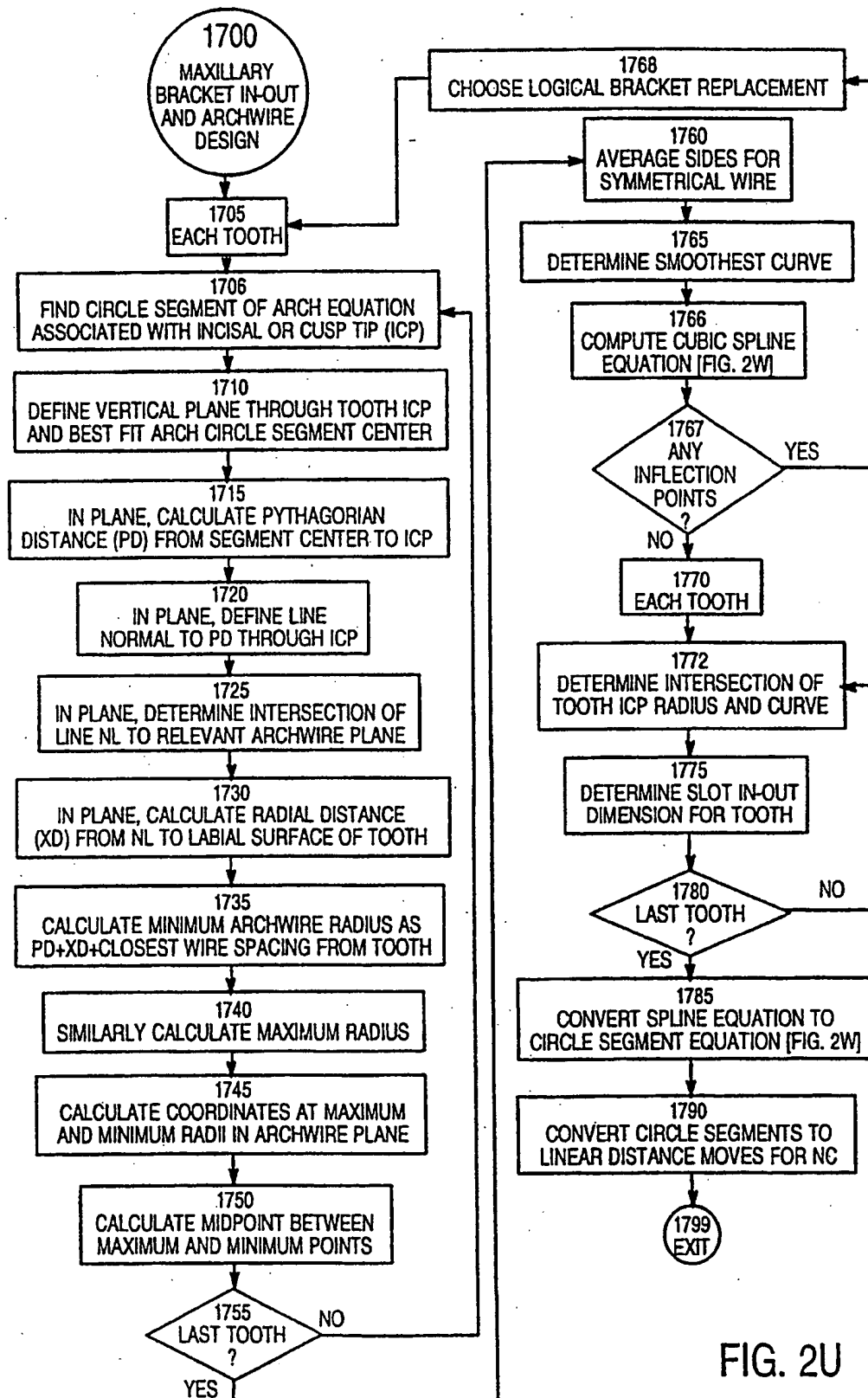


FIG. 2U

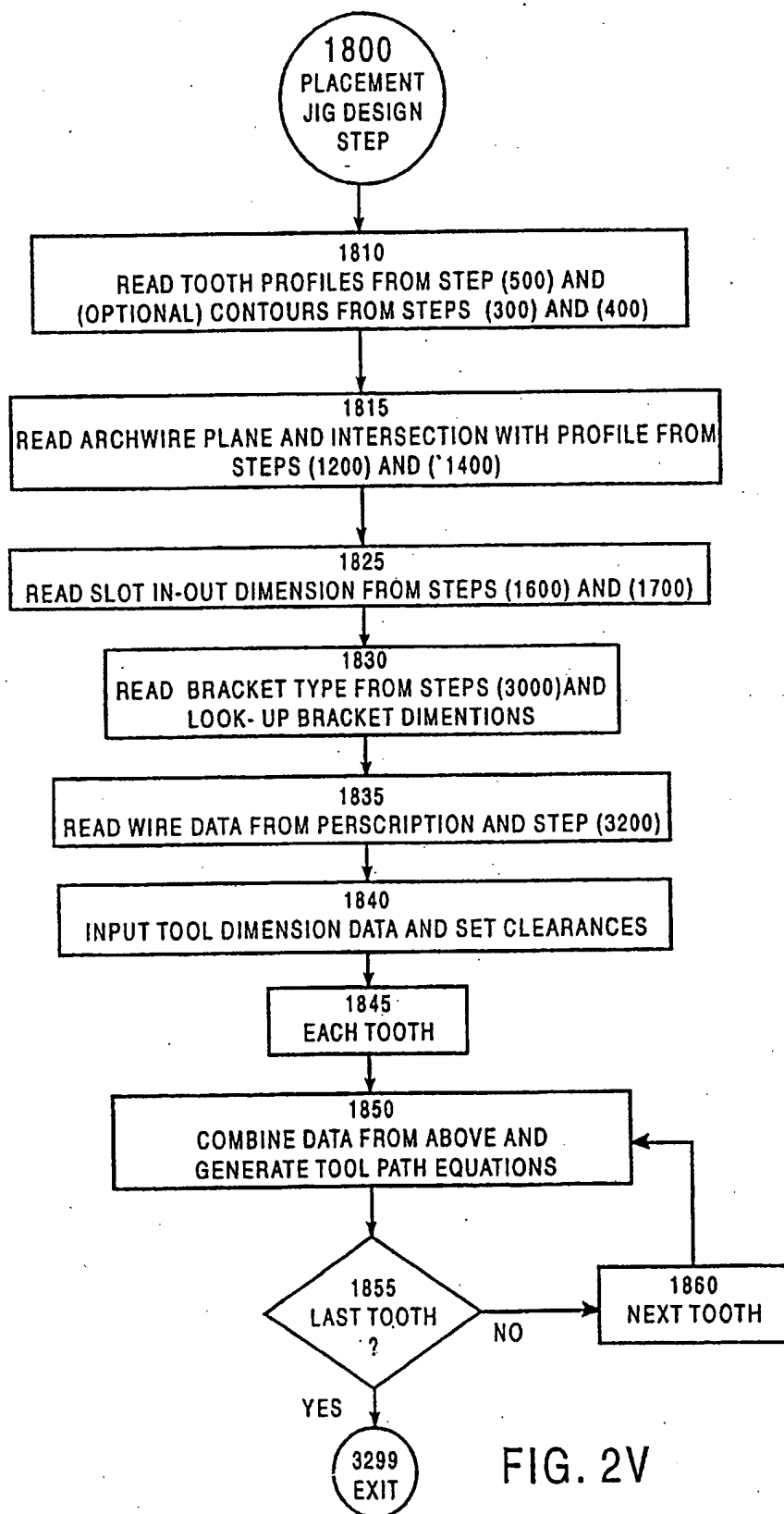


FIG. 2V

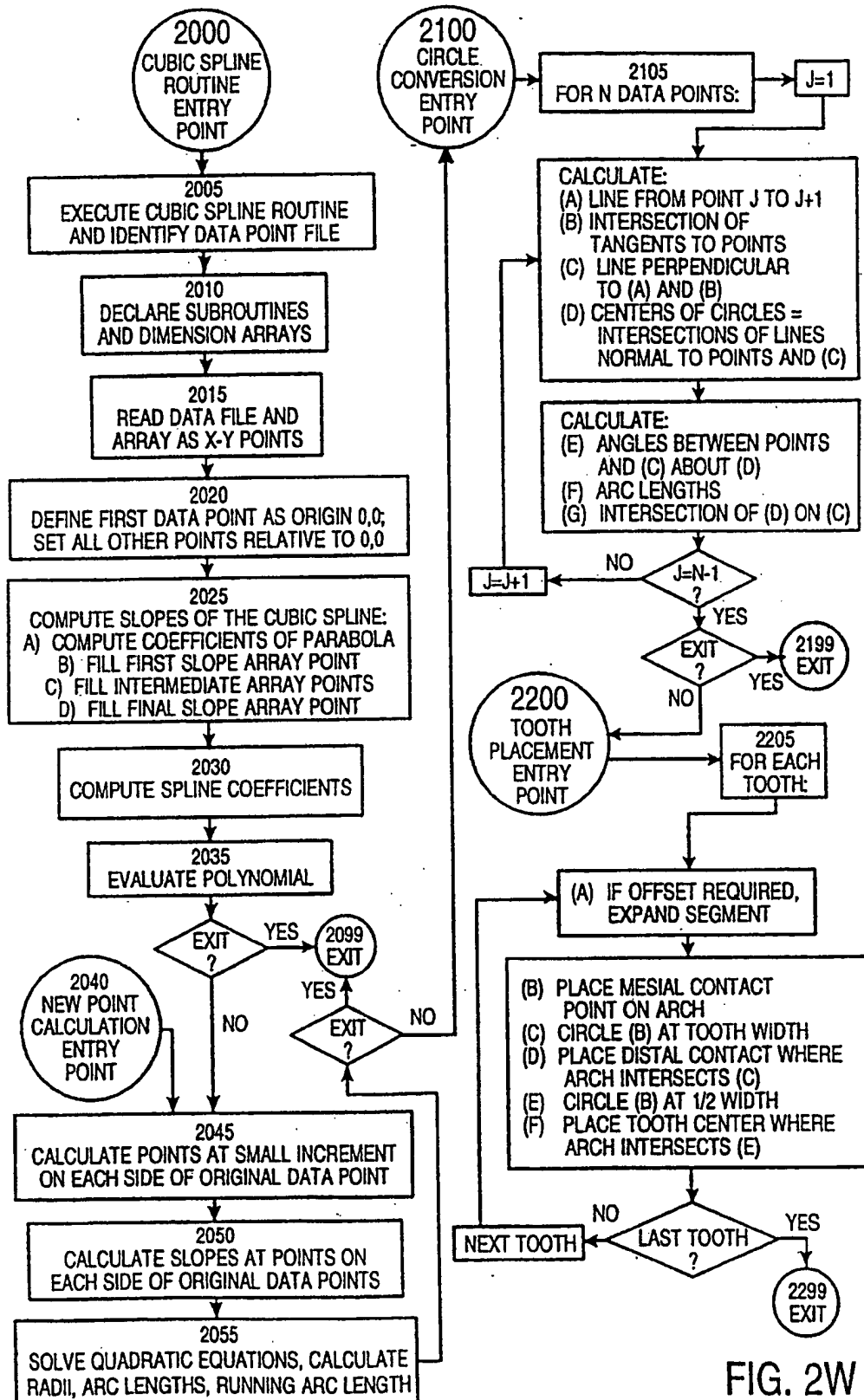


FIG. 2W

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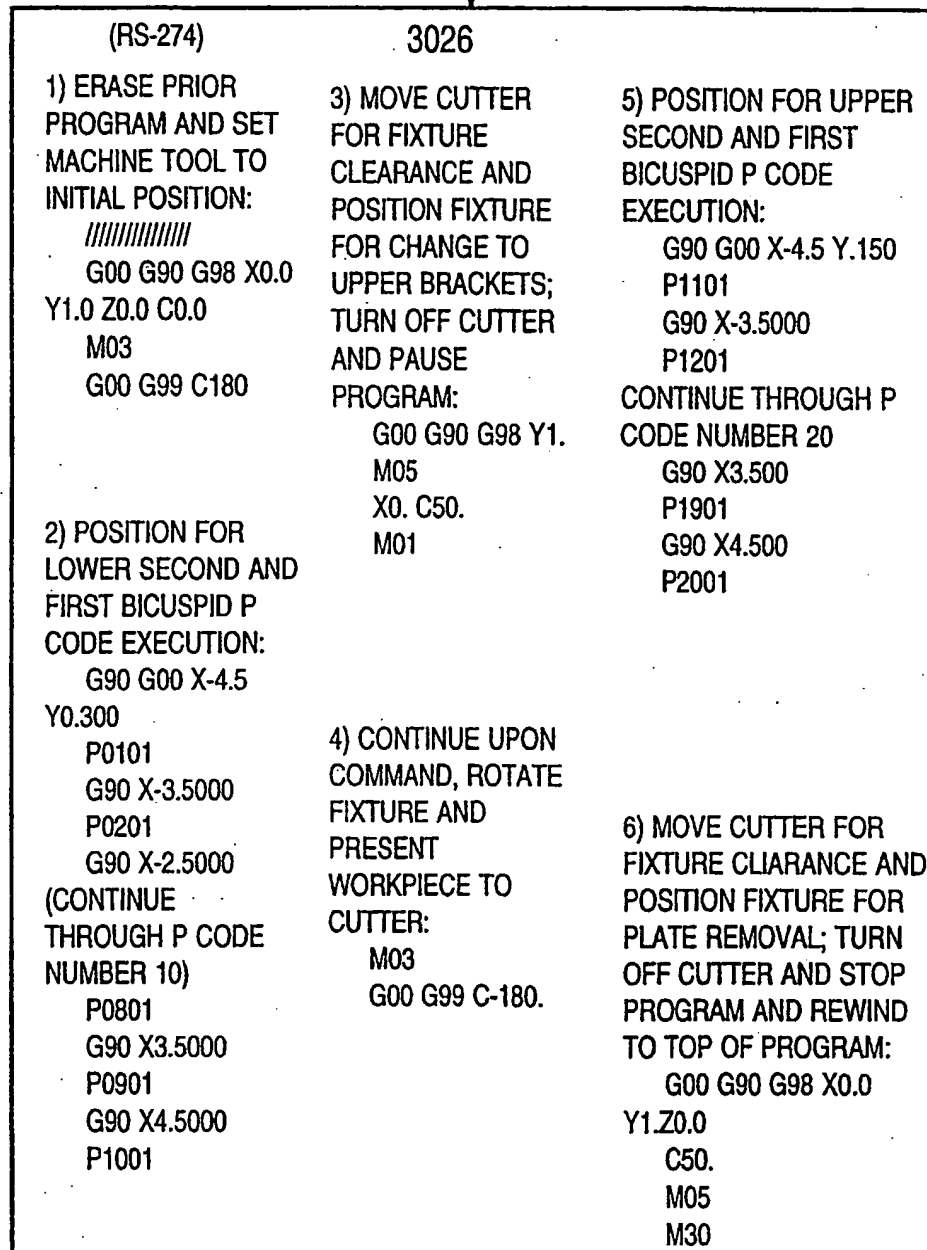


FIG. 2X-1



SUBSTITUTE SHEET (RULE 26)

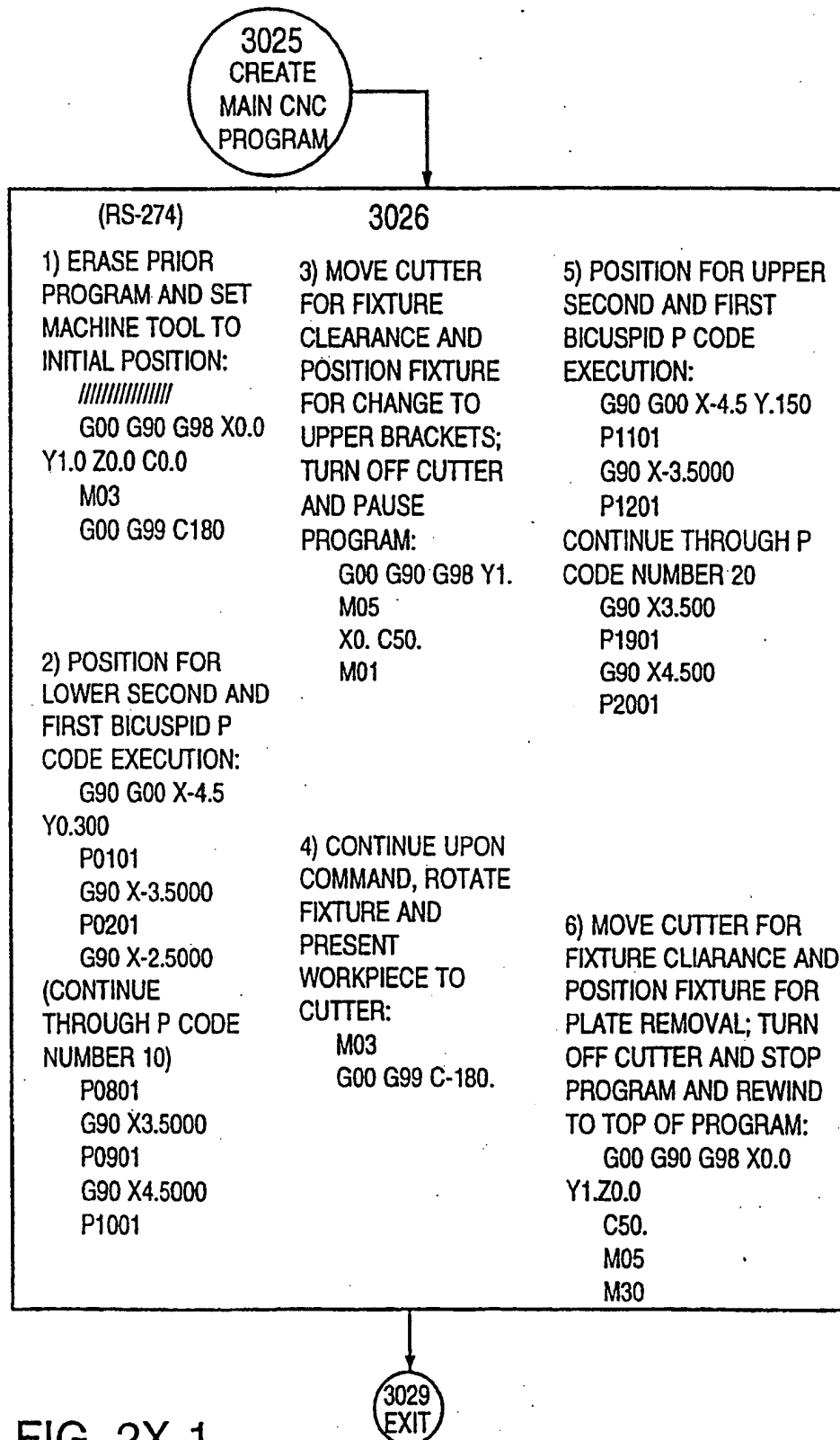


FIG. 2X-1

FIG. 2X-2

3030

CALCULATE VARIABLES FOR EACH BRACKET:

IF $\text{TmpTta} < 0$ THEN:
 $\text{IYPT} = (-1) * (\text{BW} / (\text{BO} - \text{TWR}))$;
 $\text{BL3} = \text{IYPT} / \cos(\text{ThtaRad}) + \text{eLAN} / \tan(\text{ThtaRad})$;
 $\text{bL5} = \text{fc} / \sin(\text{ThtaRad})$;
 $\text{mL5} = \tan(\text{ThtaRad} - \text{PI}/2)$;
 $\text{ML4} = \text{ML5}$; $\text{Beta} = \text{ThtaRad} + \text{atan}(\text{bo} / \text{fc} + \text{bc})$;
 $\text{D1} = ((\text{fc} + \text{bc})^2)^{1/2}$;
 $\text{P7x} = (\text{bL5} - \text{bL3}) / \text{ML3} - \text{ML5}$; $\text{P7y} = \text{ML3} * \text{P7x} + \text{bL3}$;
 $\text{P8x} = (\text{D1} * \sin(\text{Beta}) + \text{twr} - \text{bL5}) / \text{ML4}$;
 $\text{P8y} = \text{D1} * \sin(\text{Beta}) - \text{twr}$;
 $\text{Delx} = \text{P8x} - \text{P7x}$; $\text{Dely} = \text{P8y} - \text{P7y}$;
 $\text{LA} = (\text{Delx}^2 + \text{Dely}^2)^{1/2}$;
 $\text{x} = (\text{LA} * (\cos(\text{ThtaRad}))^2 / (1 + (\cos(\text{ThtaRad}))^2))$;

WHERE:

P7x AND P7y = X AND Y
 COORDINATES OF INTER-
 SECTION OF LINE 5 AND LINE 3;
 P8x AND P8y = X AND Y
 COORDINATES OF INTER-
 SECTION OF LINE 5 AND LINE
 PARALLEL TO X AXIS AND
 THROUGH TIE WING IN ROTATED
 POSITION;
 LA =PYTHAGOREAN DISTANCE
 FROM POINT 8 TO POINT 7;
 P9x AND P9y = BOTTOM OF SLOT
 IN X AND Y DIRECTIONS FROM
 CENTER OF FIXTURE ROTATION.

3032 IF $\text{TmpTta} > 0$, THEN:

$\text{IYPT} = \text{bw} + \text{bo} + \text{twr}$;
 $\text{bL3} = \text{IYPT} / \cos(\text{ThtaRad})$;
 $\text{bL5} = \text{fc} / \sin(\text{ThtaRad}) + \text{eLAN} / \tan(\text{ThtaRad})$;
 $\text{ML3} = \tan(\text{ThtaRad} - \text{PI}/2)$;
 $\text{ML4} = \text{ML5}$;
 $\text{Beta} = \text{ThtaRad} + \text{atan}(\text{bo} / \text{fc} + \text{bc})$;
 $\text{D1} = ((\text{fc} + \text{bc})^2 + (\text{b0})^2)^{1/2}$;
 $\text{D2} = ((\text{fc} + \text{bc})^2 + (\text{IYPT})^2)^{1/2}$;
 $\text{p7x} = (\text{bL5} - \text{bL3}) / (\text{ML3} - \text{ML5}) / \text{ML4}$;
 $\text{P7y} = \text{ML3} * \text{p7x} + \text{bL3}$;
 $\text{p8x} = (\text{D1} * \sin(\text{Beta}) + \text{twr} - \text{bL5}) / \text{ML4}$;
 $\text{P8y} = \text{D1} * \sin(\text{Beta})$;
 $\text{Delx} = \text{P8x} - \text{P7x}$;
 $\text{Dely} = \text{P8y} - \text{P7y}$;
 $\text{LA} = (\text{Delx}^2 + \text{Dely}^2)^{1/2} / (1 + (\cos(\text{ThtaRad}))^2)$;
 $\text{P9x} = \text{P7x} + \text{x} * \sin(\text{ThtaRad})$;
 $\text{P9y} = \text{P7y} - \text{x} * \cos(\text{ThtaRad})$;
 IF $\text{Theta} < 0$ THEN
 IF LOWER TEETH, THEN
 $\{\text{TtaStrt} = \text{Theta}; \text{TtaEnd} = (-1) * \text{Theta};\}$
 ELSE $\{\text{TtaStrt} = (-1) * \text{Theta}; \text{TtaEnd} = \text{Theta};\}$
 ELSE
 IF LOWER TEETH THEN
 $\{\text{TtaStrt} = \text{Theta}; \text{TtaEnd} = (-1) * \text{Theta};\}$
 ELSE $\{\text{TtaStrt} = (-1) * \text{Theta};$
 $\text{TtaEnd} = \text{Theta};\}$
 $\text{D2} = \text{PYTHAGOREAN DISTANCE FROM}$
 $(0,0)$ TO $(\text{fc} + \text{bc}, \text{IYPT})$;
 TEMPORARY $\text{Theta} (\text{TmpTta}) = 0$
 TIE WING RADIUS $(\text{twr}) = 0.010$

3033 SUBTRACT ONE HALF WIRE
 HEIGHT FROM IN-OUT DIMENSION;
 $\text{Elan} = \text{Elan} - 0.012$

WHERE: ML3 =SLOPE OF line 3;
 bL3 =Y INTERCEPT OF line 3;
 ML5 =SLOPE OF LINE 5;
 bL5 =Y INTERCEPT OF LINE 5;
 ML4 =SLOPE OF LINE 4;
 BETA =ANGLE BETWEEN X AXIS
 AND CENTER OF TIE WING
 (BELOW X AXIS).

3034 EXTRACT DESIGN DATA
 FOR SECOND BICUSPIDS:

$\text{BCLoLo} = \text{L5BCLL}$ $\text{BCUpHi} = \text{U5BCUH}$
 $\text{BCLoHi} = \text{L5BCLH}$ $\text{BOUpLo} = \text{U5BOUL}$
 $\text{BOLoLo} = \text{L5BOLL}$ $\text{BOUpHi} = \text{U5OUB}$
 $\text{BOLoHi} = \text{L5BOLH}$ $\text{BWLowlr} = \text{L5BW}$
 $\text{BCUpLo} = \text{U5BCUL}$ $\text{BWUppr} = \text{U5BW}$

WHERE:

FOR LOWER SECOND BICUSPIDS:
 L5BCLL =BRACKET CONSTANT BELOW X AXIS;
 L5BCLH =BRACKET CONSTANT ABOVE X AXIS;
 L5BOLL =BRACKET OFFSET BELOW X AXIS;
 L5BOLH =BRACKET OFFSET ABOVE X AXIS;
 L5BW =BRACKET WIDTH;
 FOR UPPER SECOND BICUSPIDS:
 U5BCUL =BRACKET CONSTANT BELOW X AXIS;
 U5BCUH =BRACKET CONSTANT ABOVE X AXIS;
 U5BOLL =BRACKET OFFSET BELOW X AXIS;
 U5BOLH =BRACKET OFFSET ABOVE X AXIS
 U5BW =BRACKET WIDTH

3035 SET ALL
 BRACKETS EXCEPT
 BICUSPIDS TO
 LOWER PROFILE.

3039
EXIT

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3040 ASSIGN VARIABLES FOR EACH TOOTH:
 IF TOOTH IS LOWER SECOND BICUSPID: WHERE:
 $bw = L \% BW$ MinBic=MINIMUM BICUSPID
 $Elan = LL2biT$ IN-OUT FOR HIGHER
 $Theta = LL2biA$ PROFILE BRACKETS
 $ar = LR5$ bw =BRACKET WIDTH
 $fc = FCLo$ $Elan$ =IN-OUT
 IF $Elan \leq MinBic$ THEN LOW PROFILE BRACKET & $Theta$ =TORQUE (SLOT
 $LL15=0$ INCLINATION TO PLANE)
 IF $Theta \leq 0$ THEN $\{bc = BCBiLo; bo = -1 * BOBiLo\}$ ar =ARCH RADIUS
 ELSE $\{bc = BCBiHi; bo = BOBiHi\}$ $LR5$ =LOWER RADIUS FOR
 ELSE IF $Theta \leq 0$ THEN LOW PROFILE BRACKET SECOND BICUSPID
 & $\{BC = L5BCLL; bo = -1 * L5BOLL\}$ fc =FIXTURE CONSTANT
 ELSE HIGH PROFILE BRACKET & bo =BRACKET OFFSET
 $\{bc = L5BCLH; bo = L5BOLH\}$ bc =BRACKET CONSTANT

3045 TEST FOR NON-ZERO ANGLE: WHERE:
 IF $Theta \neq 0$ THEN: $ThaRad$ =THETA
 ASSIGN UPPER OR LOWER SIGN TO ANGLE: CONVERTED TO
 LOWER TEETH: $TmpTA = (-1) * Theta$ RADIANS
 UPPER TEETH: $TmpTta = Theta$ $P9x$ AND
 $ThaRad = RAD(TmpTta)$ $P9y$ =DISTANCE OF
 ELSE: $TtaStrt = Theta$ BOTTOM OF SLOT IN
 $TtaEnd = Theta$ X AND Y DIRECTIONS
 $P9x = fc + Elan$ FROM CENTER OF
 $P9y = (0.5) * ABS(bo + twr + 0.5 * bw)$ FIXTURE ROTATION
 IF LOWER TEETH: $P9y = (-1) * P9y$ I

3050 IF $TmpTta > 0$: WHERE: $IYPT$ =DISTANCE FROM X AXIS
 $P9x = P7x - x * \sin(ThaRad)$ TO BRACKET WALL;
 $P9y = P7y + x * \cos(ThaRad)$ bo =BRACKET OFFSET;
 IF $Theta < 0$ THEN: fc =FIXTURE CONSTANT;
 IF $COUNTER \leq +12$ THEN bc =BRACKET CONSTANT;
 $\{TtaStrt = Theta; TtaEnd = (-1) * Theta\}$ twr =TIE WING RADIUS;
 ELSE $\{TtaStrt = (-1) * Theta;$ bw =BRACKET WIDTH;
 $TtaEnd = Theta\}$ $D1$ =PYTHAGOREAN DISTANCE
 FROM (0,0) TO $(fc+bc,bo)$

3055 PERFORM CALCULATIONS FOR TORQUE SLOT ON ARCHWIRE RADIUS: WHERE:
 $z = P9y$ $z = P9y$ (HEIGHT OF CUTTER
 $cr = cd/2$ NEED TO CUT TORQUE
 IF $bic \leq 0$ THEN: cd = CUTTER DIAMETER;
 $NCi = 0.35$ NCi AND NCj = START TO
 $NCj = 0.0$ CENTER POINTS FOR ARCH
 $ys = P9x + cr$ RADIUS CUTTER PATH IN i
 ELSE: AND j DIRECTIONS;
 $NCi = tr * \sin(arr)$ ys AND $xs = y$ AND x START
 $ncj = tr * \cos(arr)$ POINTS FOR ARCH RADIUS
 $ys = P9x - tr * (1 - \cos(arr)) + cr$ CUTTER PATH;
 $xs = s - NCi$ $xe = x$ ENDPOINT FOR ARCH
 $XE = S + NCi$ RADIUS CUTTER PATH

3059
EXITFIG.
2X-3

26/54

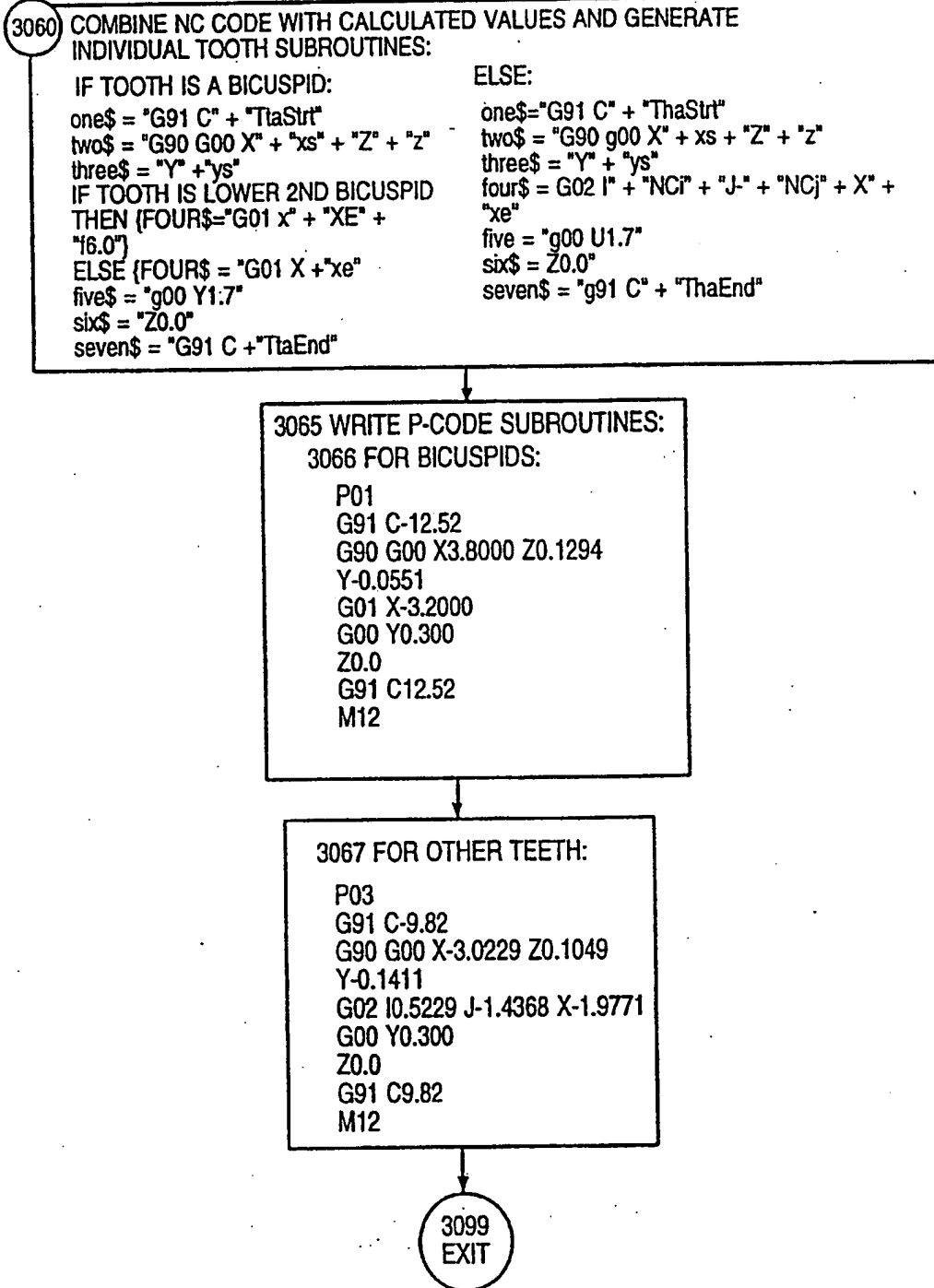


FIG. 2X-4

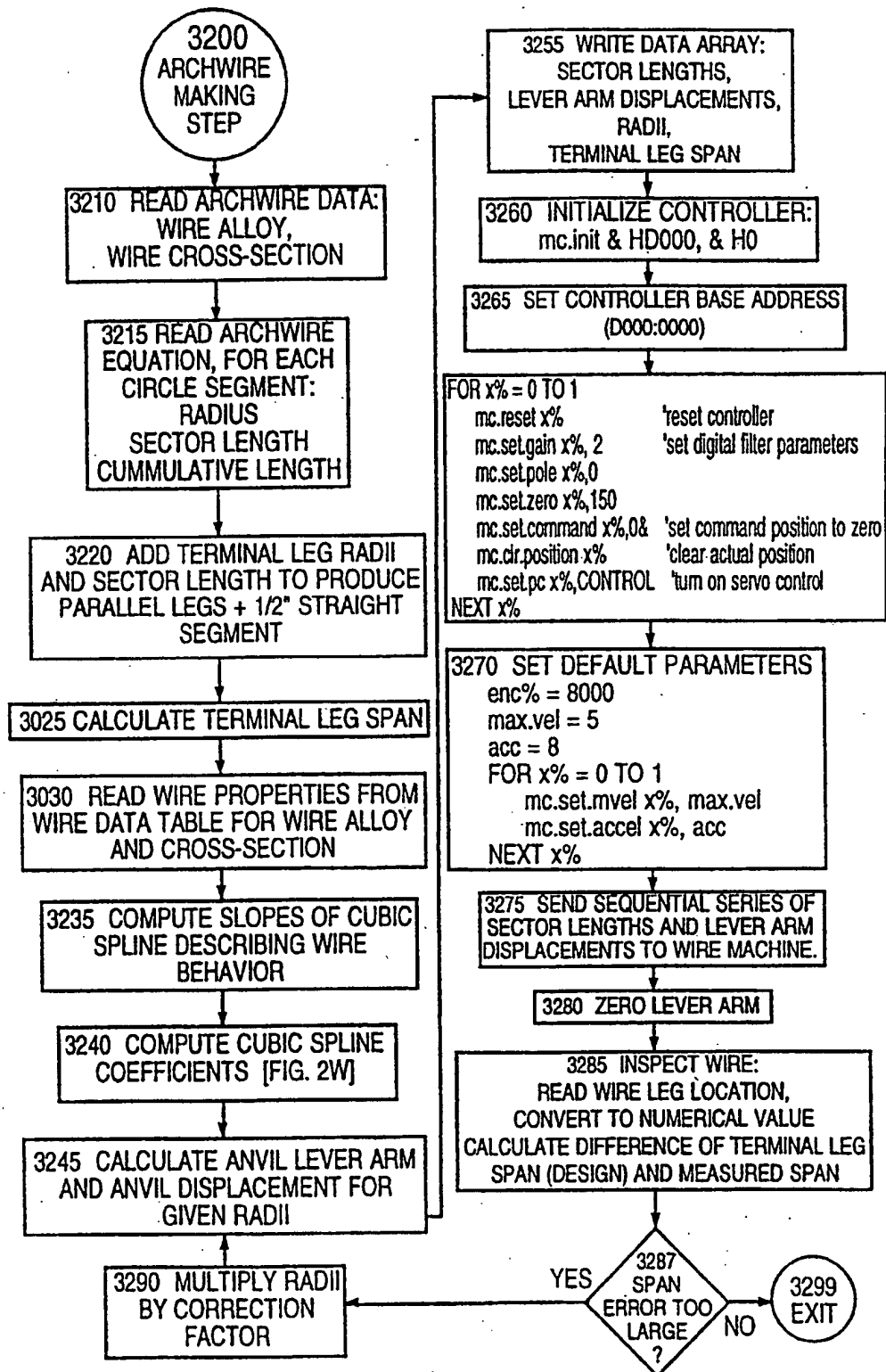


FIG. 2Y

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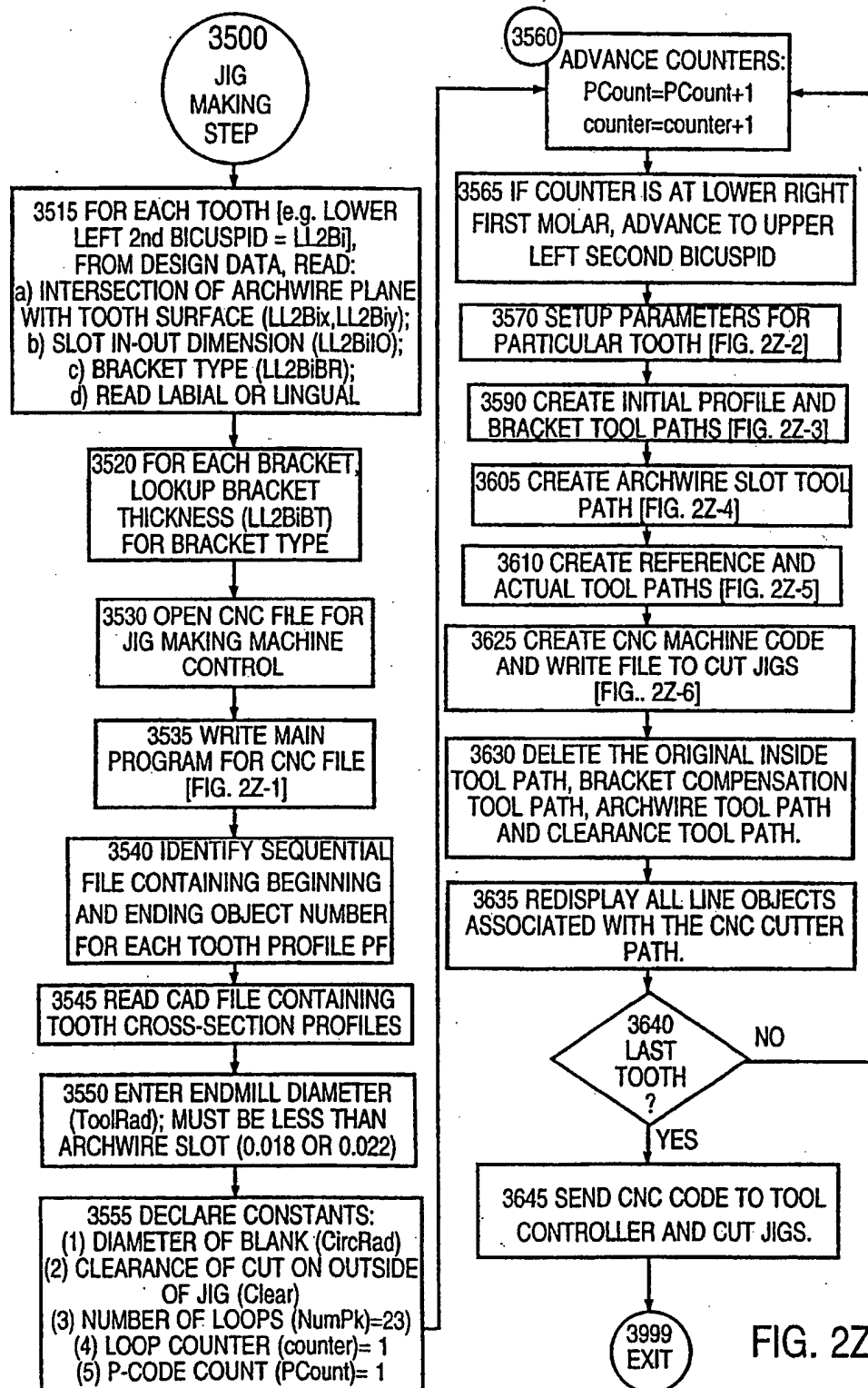


FIG. 2Z

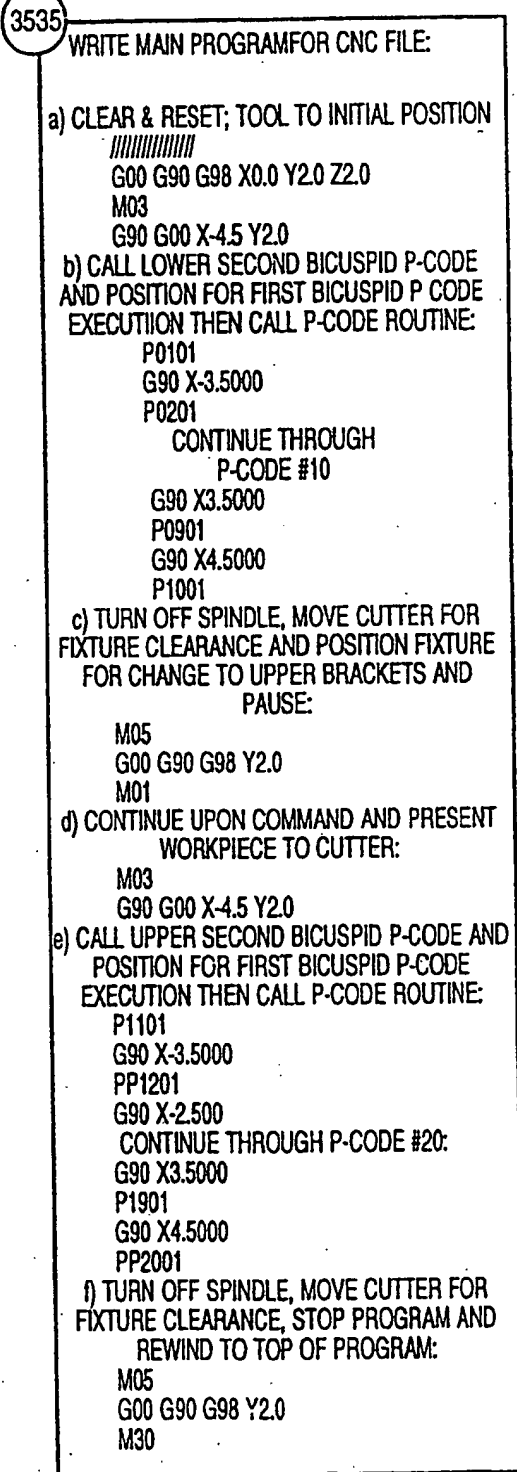


FIG. 2Z-1

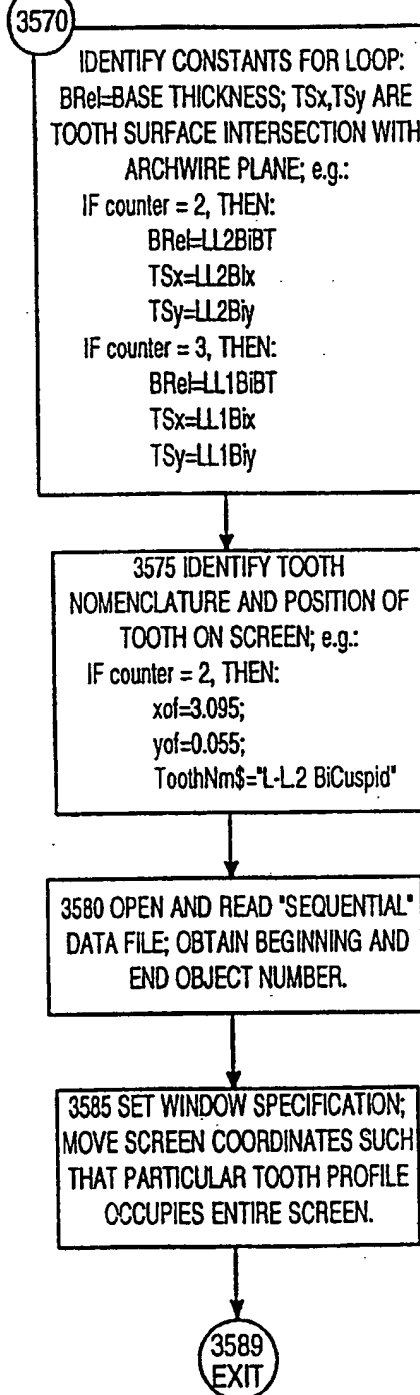
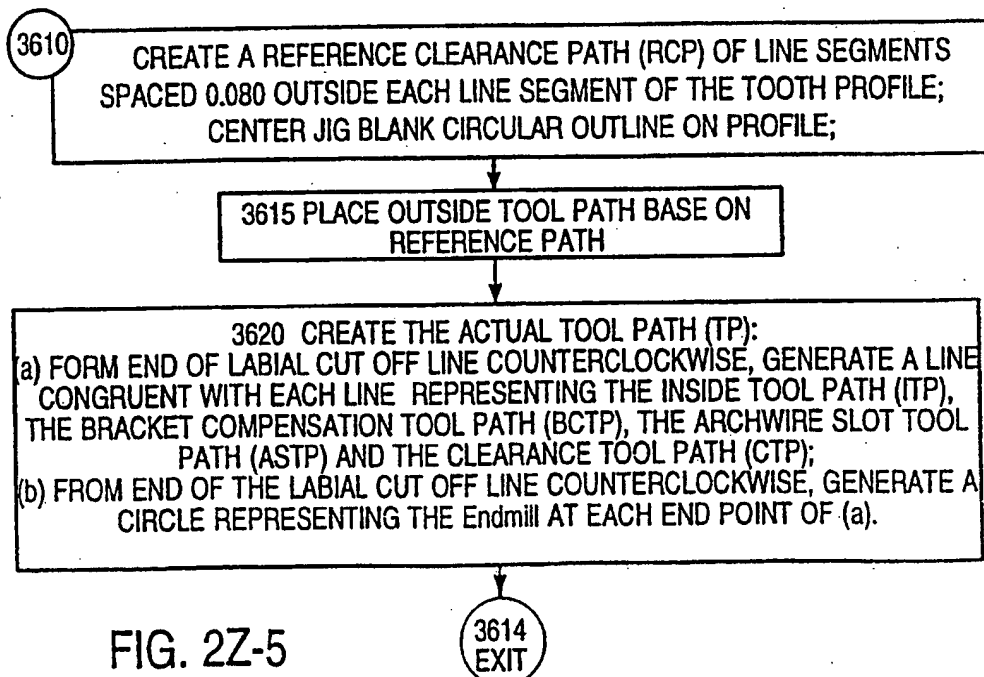
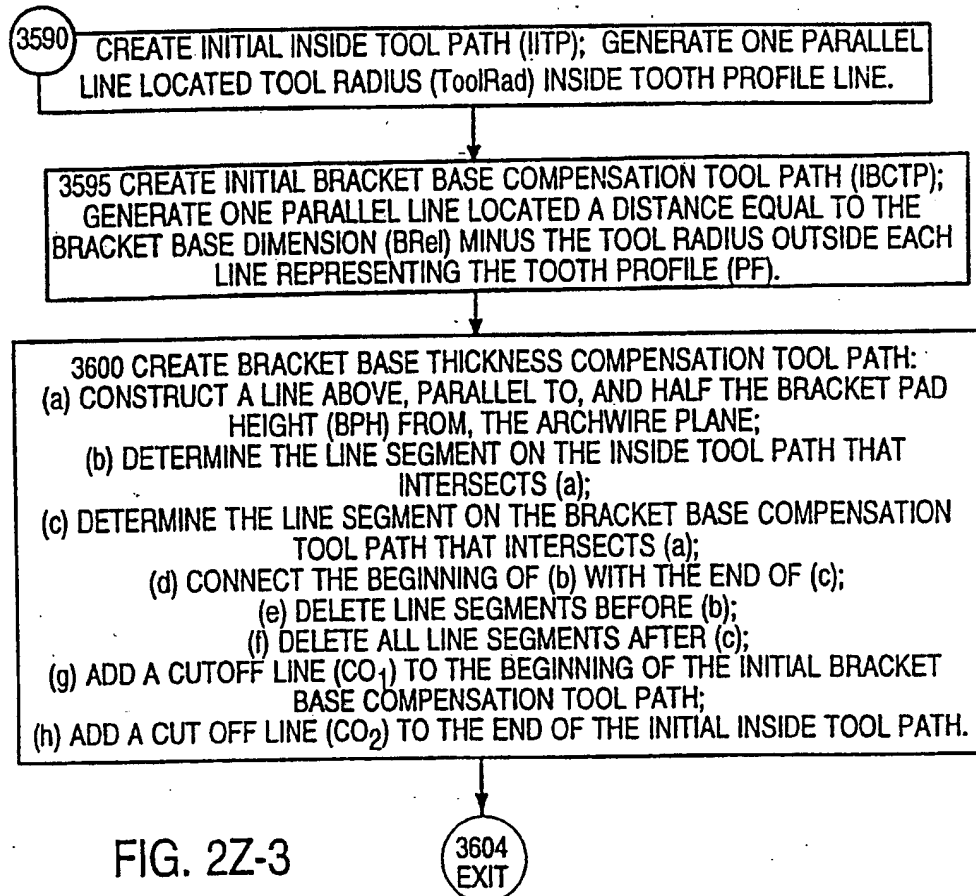


FIG. 2Z-2



3605

CREATE AN ARCHWIRE SLOT TOOL PATH (ASTP):

- (a) DETERMINE THE DISTANCE FROM THE SURFACE OF THE TOOTH IN THE x DIRECTION THAT WILL ALLOW A PLASTIC SHIM TO FIT INTO THE TORQUE SLOT:

THE DIMENSIONS OF THE SHIM ARE:

(torque slot width) x 0.085 x 0.100;

$LnEnd = TSx + Elan - 0.012 + 0.085 \cdot ToolRad$

WHERE: $LnEnd = x$ LOCATION

$Elan = \text{BRACKET In-out (IO)}$

- (b) CONSTRUCT A LINE ABOVE AND PARALLEL TO THE ARCHWIRE PLANE SUCH THAT THE ENDMILL WILL GENERATE A LINE CONGRUENT WITH THE BRACKET TORQUE SLOT WALL; THE HEIGHT ABOVE THE ARCHWIRE PLANE IS:

$(\text{torque slot width})/2 - ToolRad$;

- (c) DETERMINE THE LINE SEGMENT ON THE BRACKET BASE COMPENSATION TOOL PATH THAT INTERSECTS (a);

(d) DELETE (b);

- (e) CONSTRUCT A LINE BELOW AND PARALLEL TO THE ARCHWIRE PLANE SUCH THAT THE ENDMILL WILL GENERATE A LINE CONGRUENT WITH THE BRACKET TORQUE SLOT WALL:

THE HEIGHT ABOVE THE ARCHWIRE PLANE IS:

$(\text{torque slot width})/2 - ToolRad$.

- (f) DETERMINE THE LINE SEGMENT ON THE BRACKET BASE COMPENSATION PATH THAT INTERSECTS (a):

THIS IS POINT 8: $P8x, P8y$;

(g) DELETE (e);

- (h) CONSTRUCT A LINE FROM POINT 1 ($P1x, P1y$) TO POINT 2 ($P1x, LnEnd - 0.001$);

- (i) CONSTRUCT A LINE FROM POINT 2 ($P1x, LnEnd - 0.001$) TO POINT 3 ($P1x + 2.5ToolRad, LnEnd - 0.001$);

- (j) CONSTRUCT A LINE FROM POINT 3 ($P1x + 2.5ToolRad, LnEnd - 0.001$) TO POINT 4 ($P1x + 2.5ToolRad, LnEnd$);

- (k) CONSTRUCT A LINE FROM POINT 3 ($P1x + 2.5ToolRad, LnEnd - 0.001$) TO POINT 4 ($P1x + 2.5ToolRad, LnEnd$);

- (l) CONSTRUCT A LINE FROM POINT 5 ($P2x - 2.5ToolRad, LnEnd$) TO POINT 6 ($P2x - 2.5ToolRad, LnEnd - 0.001$);

- (m) CONSTRUCT A LINE FROM POINT 6 ($P2x - 2.5ToolRad, LnEnd - 0.001$) TO POINT 7 ($P2x, LnEnd - 0.001$);

- (n) CONSTRUCT A LINE FROM POINT 7 ($P2x, LnEnd - 0.001$) TO POINT 8 ($P1x, P8y$)

3609
GO TO 3610
[FIG. 2Z-4]

FIG. 2Z-4

3625

3625 CREATE A CNC MACHINE CODE AND WRITE IT TO FILE:

- (a) WRITE PCount GENERATED P-CODE ROUTINE NOMENCLATURE TO FILE:

```

IF PCount<=9, THEN: { PCount$=str(PCOUNT);
                     strext(count$,PCount$,0,1);
                     strcat(one$,"P0",count$); }
ELSE:                { d$=str(PCount);
                     strext(count$,d$,0,2);
                     strcat(one$,"P",count$); }

```

WRITE(h1,one\$);

- (b) WRITE RAPID TO 0.020 ABOVE WORKPIECE TO FILE: "G00 G90 Z.020";

- (c) DETERMINE END OF INITIAL LINE AND NAME AS P1x AND P1y;

- (d) DETERMINE STARTING POSITION RELATIVE TO JIG BLANK CENTER:

```

GStrtx=P1x-Toolx;
GStrty=P1y-Toolx;
strcat(two$,"G00 G91 X",str(GStrtx),"Y",str(GStrty));
WRITE(h1,two$);

```

- (e) CREATING PECKING MOTION TO CLEAR WORKPIECE ENTRANCE:

```

WRITE(h1,"G01 G90 Z-.055 F1.0");
WRITE(h1,"G00 A.020");
WRITE(h1,"G01 Z-.055 P1.0");

```

- (f) CREATE EACH INCREMENTAL MOVE

AND WRITE TO FILE:

```

i=CutStrt + 1;
WHILE i<= CutEnd do
  { inqobj(i,10,Begx,Begy,Endx,Endy);
    P2x=Endx;
    P2y=Endy;
    addobj(40,P2x,P2y,ToolRad);
    x=P2x-P1x;
    y=P2y-P1y;

```

IF i=CutStrt + 1 THEN

```

  { five$="";
    strcat(five$,"G01 G91
    X",str(x),"Y",str(y),"F1.5");
    WRITE(h1,five$); }

```

ELSE

```

  { five$="";
    strcat(five$,"X",str(x),"Y",str(y));
    write(h1,five$); }
  P1x=P2x;
  P1y=P2y;
  i=i+1;
}

```

- (g) DETERMINE AND CREATE LAST MOVE TO CLOSE LOOP:

```

inqobj(CutStrt,10,Begx,Begy,Endx,Endy);
addobj(10,Endx-.01,Endy,Endx+.01,Endy);
addobj(10,Endx,Endy-.01,Endx,Endy+.01);
P2x=Endx;
P2y=Endy;
x=P2x-P1x;
y=P2y-P1y;
six$="";
strcat(six$,"X",str(x),"Y",str(y));
WRITE(h1,six$);

```

- (h) TURN ON ABSOLUTE TO MOVE .500 ABOVE WORKPIECE AND P-CODE:

```

WRITE(h1,"G00 G90 Z.5");
WRITE(h1,"M12");

```

3629
EXIT

FIG. 2Z-6

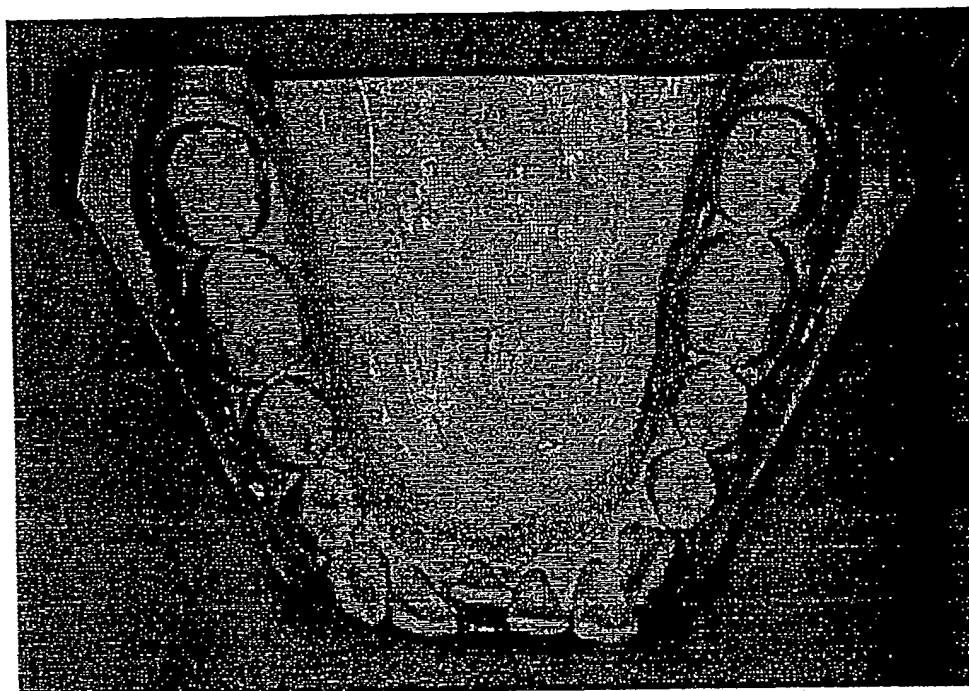
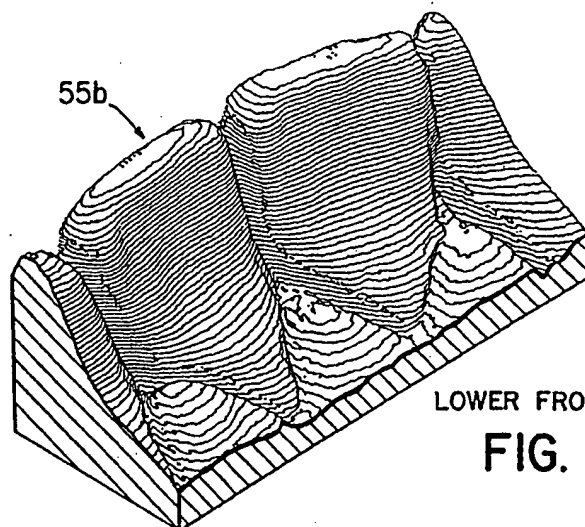
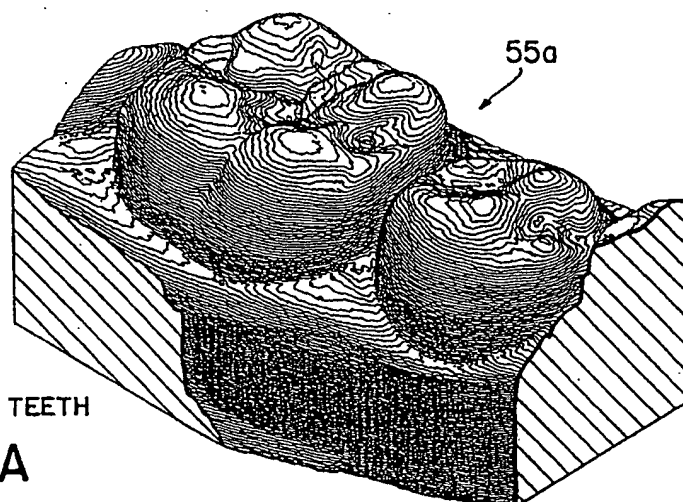


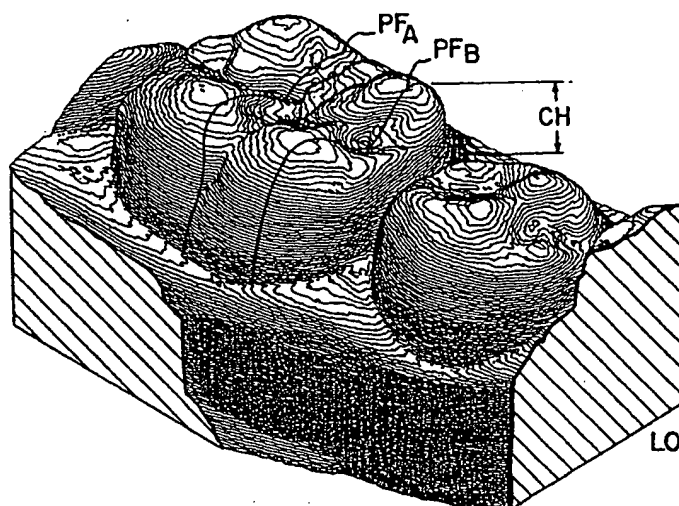
FIG. 3



LOWER FRONT TEETH
FIG. 3B



LOWER RIGHT TEETH
FIG. 3A



LOWER RIGHT TEETH
FIG. 6

RIGHT MAX-ILLARY	LEFT MAX-ILLARY	CENTRAL MAND-BUL-AR	LATERAL MAND-BUL-AR	CUSPID.	1st BICUSPID	2nd BICUSPID	1st MOLAR		
RIGHT MAND-BUL-AR	LEFT MAND-BUL-AR	CENTRAL	LATERAL	CUSPID.	1st BICUSPID	2nd BICUSPID	1st MOLAR		

FIG.3C

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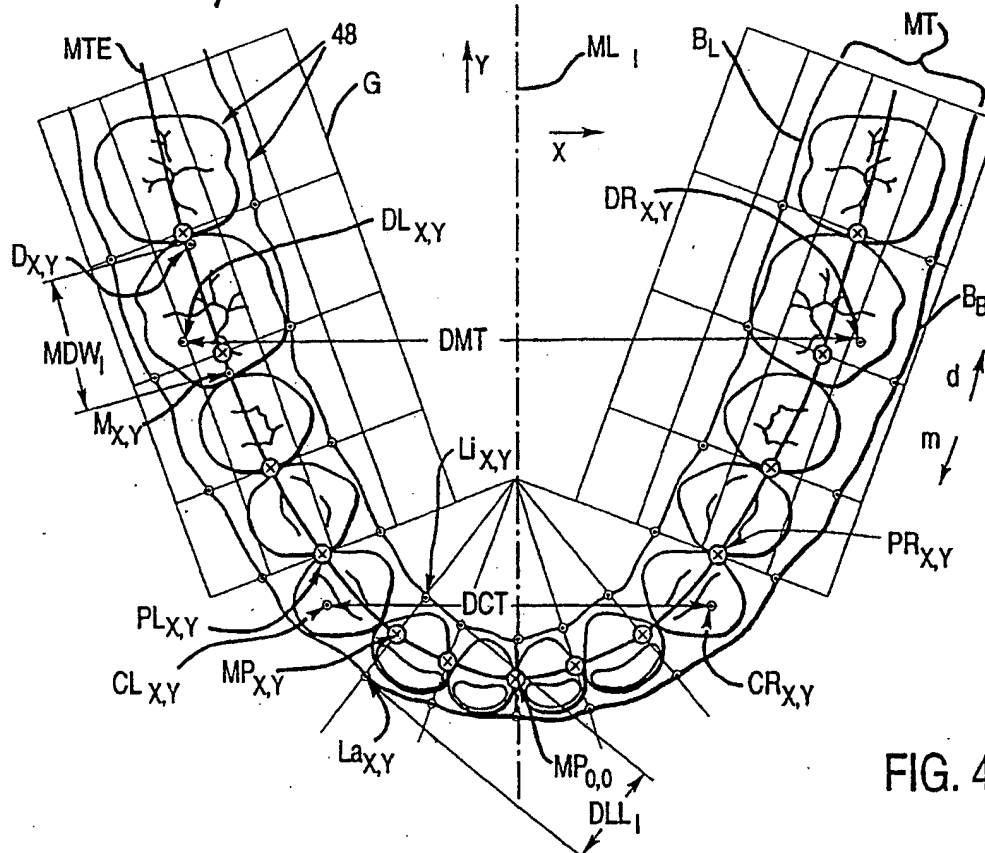
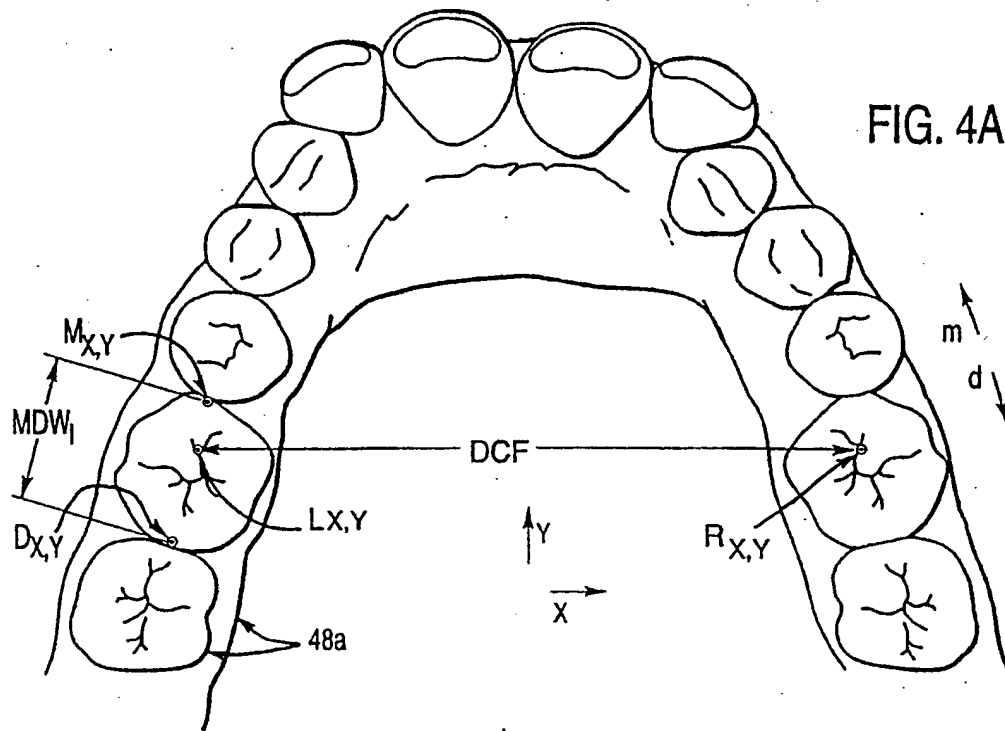


FIG. 4

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FIG. 4C

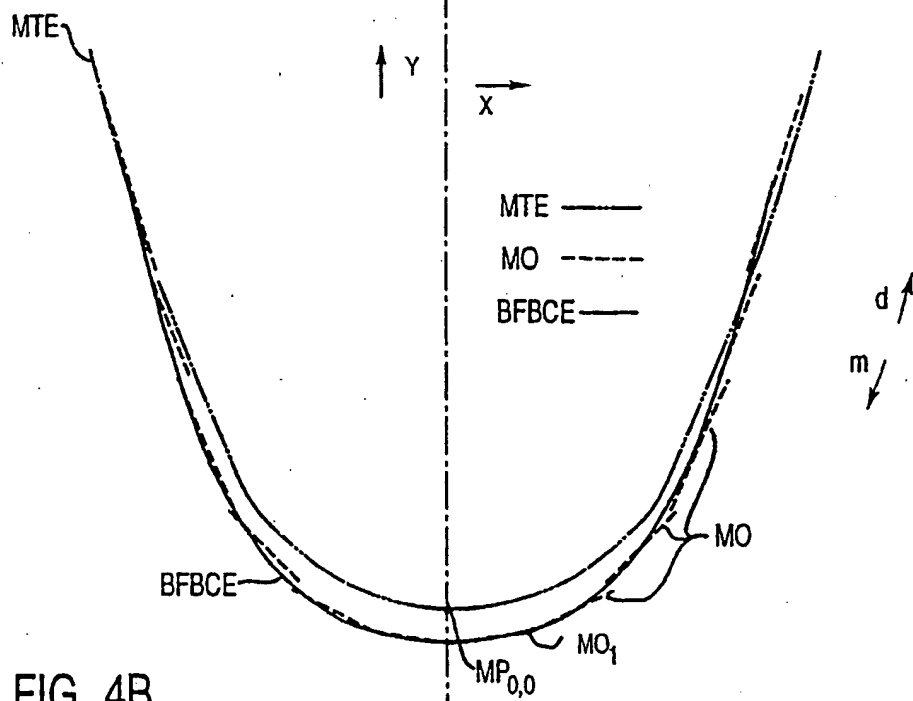
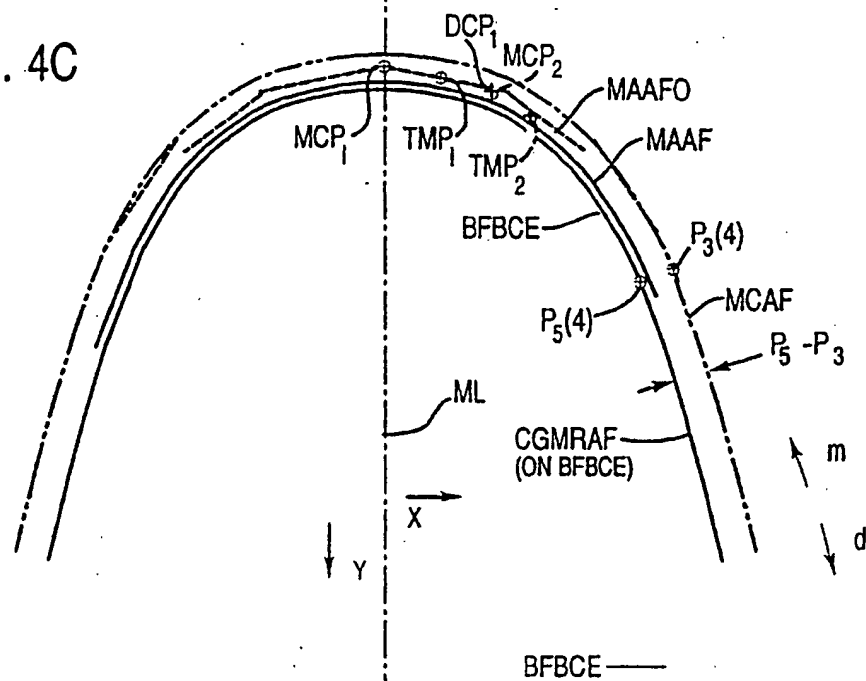


FIG. 4D

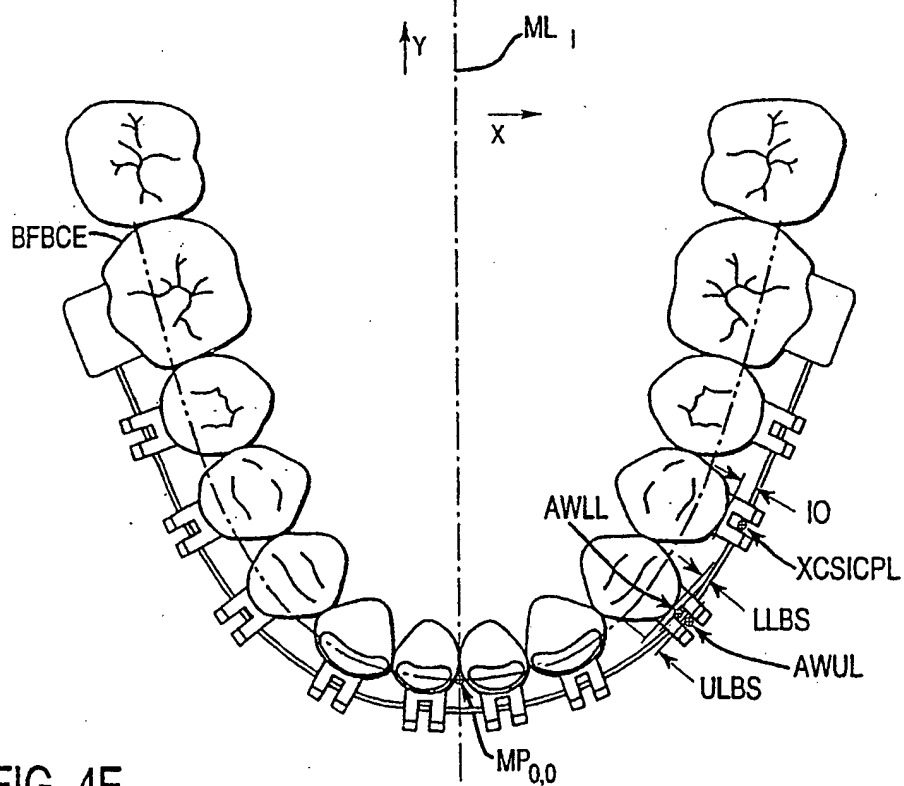
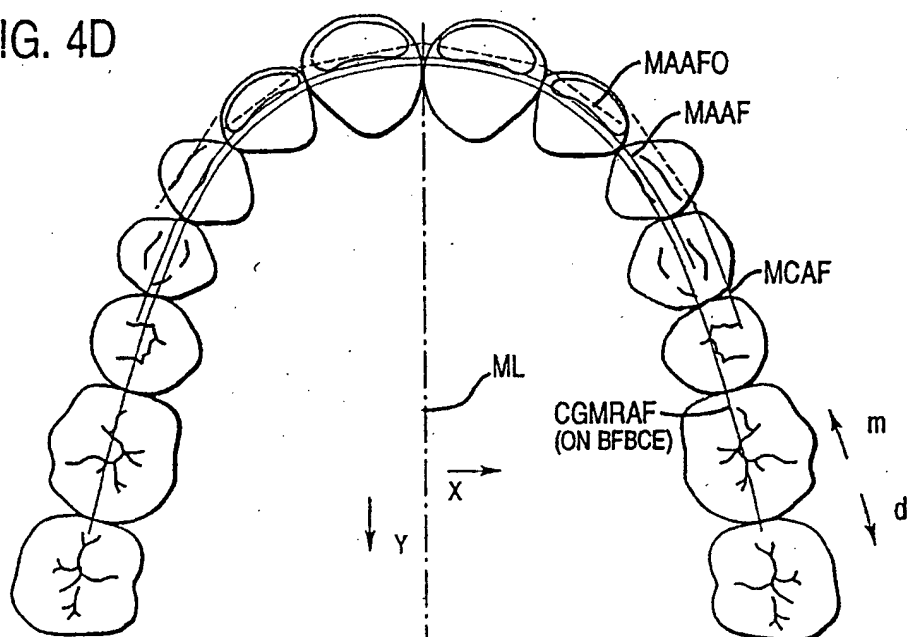


FIG. 4E

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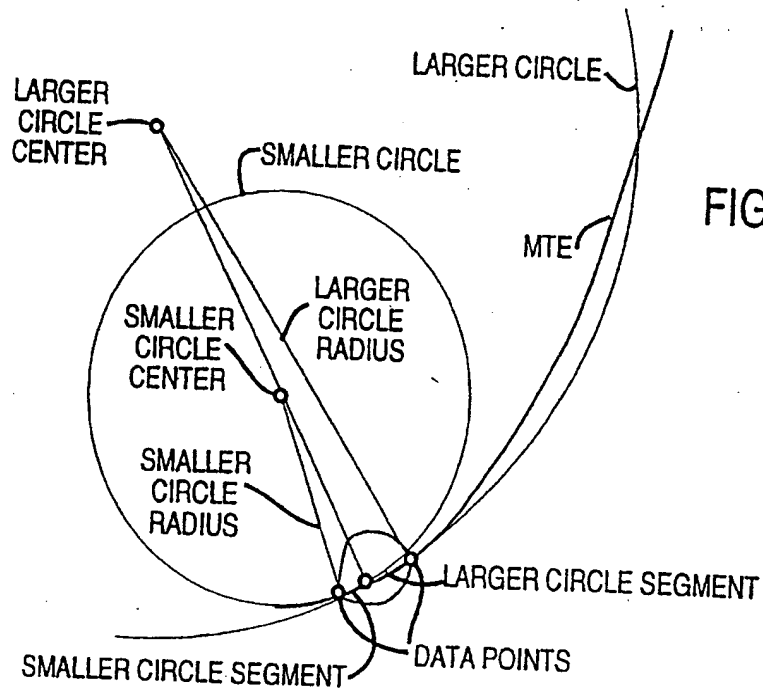


FIG. 5

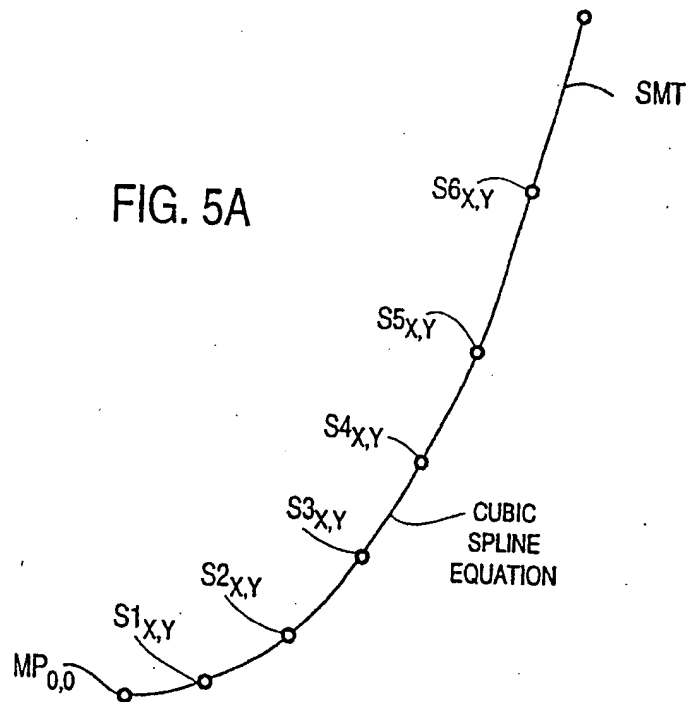


FIG. 5A

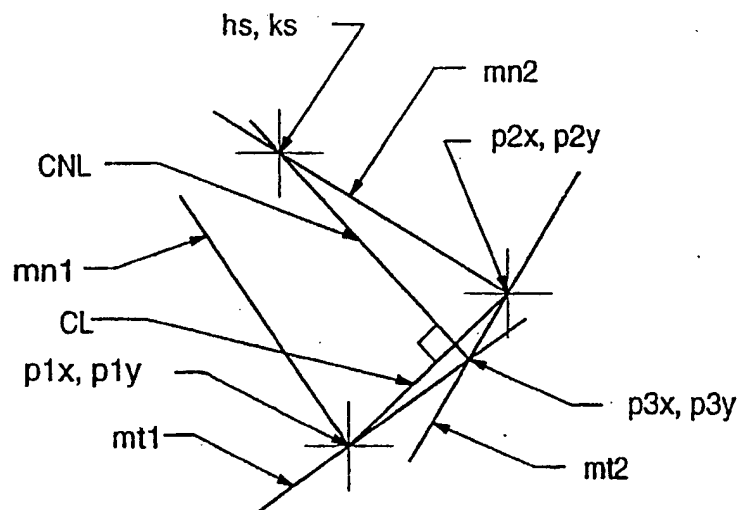
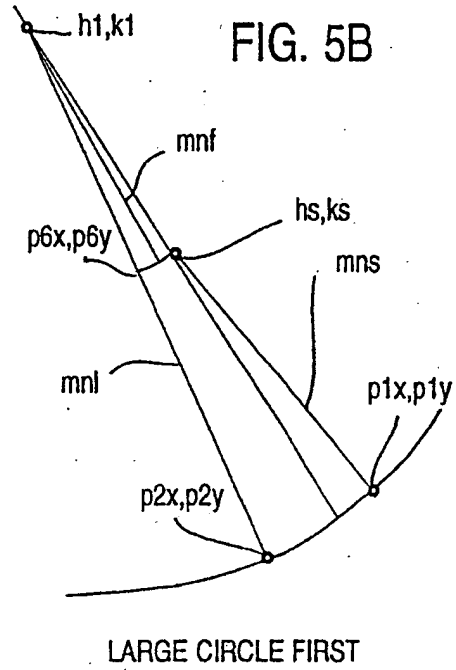
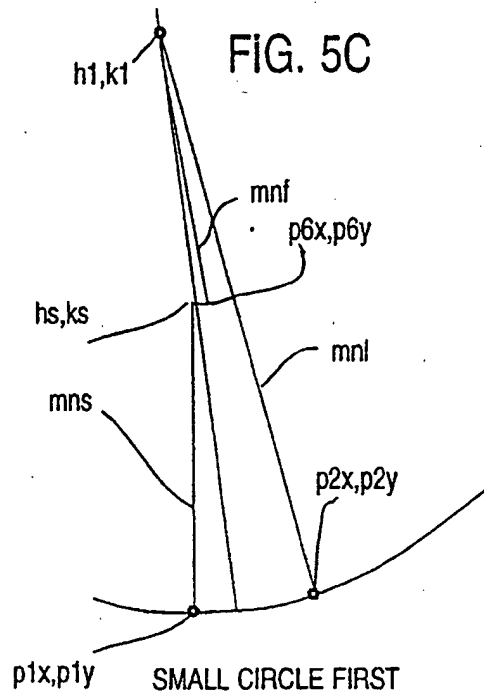
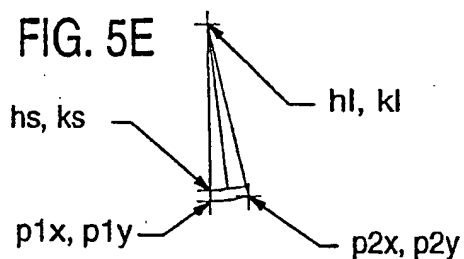


FIG. 5D

FIG. 5E



Spline Seg. No. 1
Circle Seg. Nos. 1 and 2

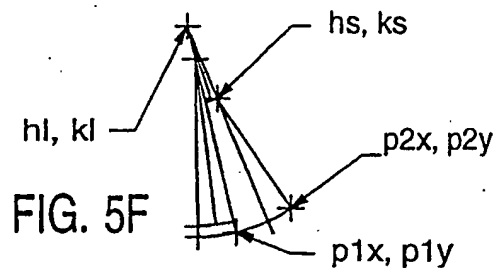
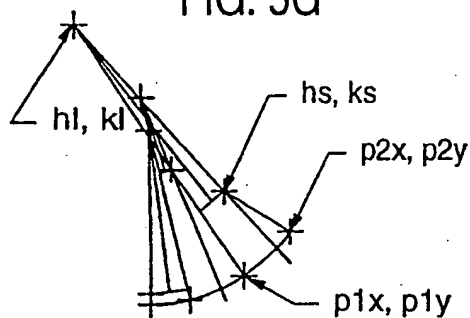


FIG. 5F

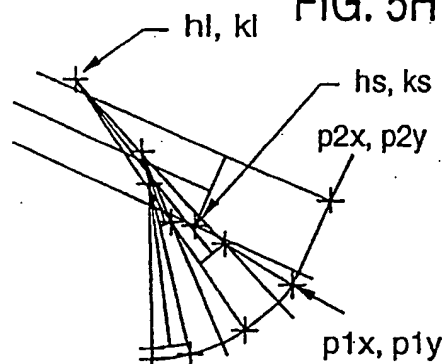
Spline Seg. No. 2
Circle Seg. Nos. 3 and 4

FIG. 5G

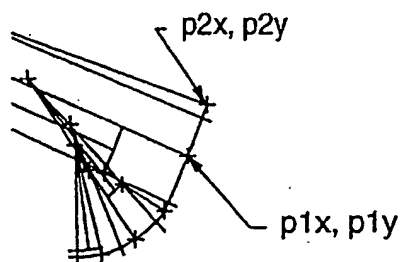


Spline Seg. No. 3
Circle Seg. Nos. 5 and 6

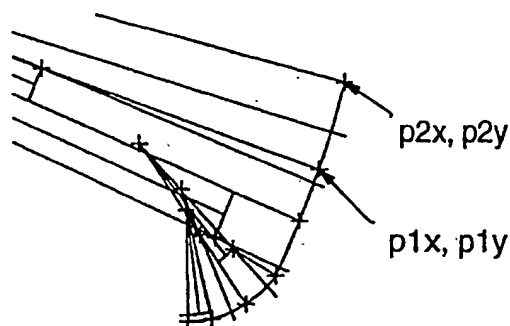
FIG. 5H



Spline Seg. No. 4
Circle Seg. Nos. 7 and 8



Spline Seg. No. 5
Circle Seg. Nos. 9 and 10

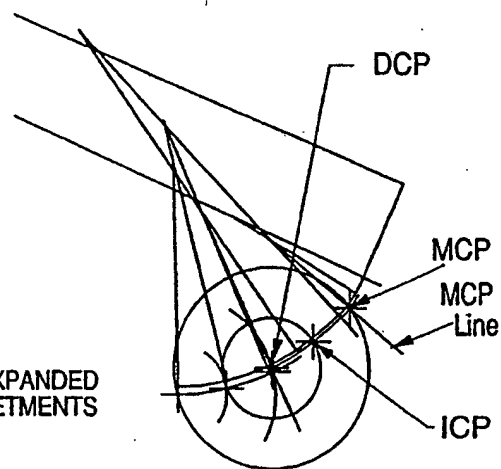
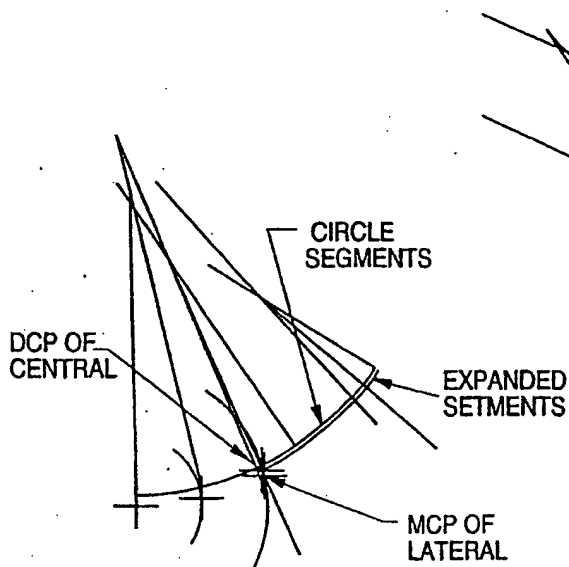
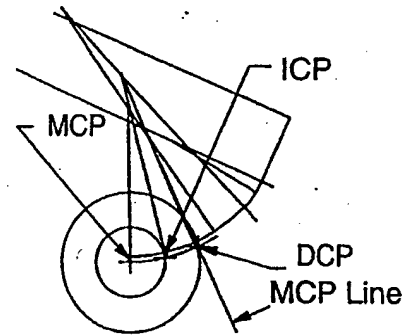
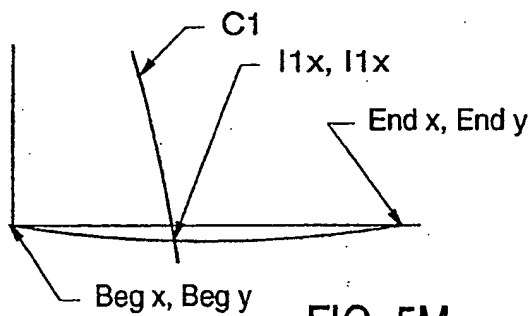
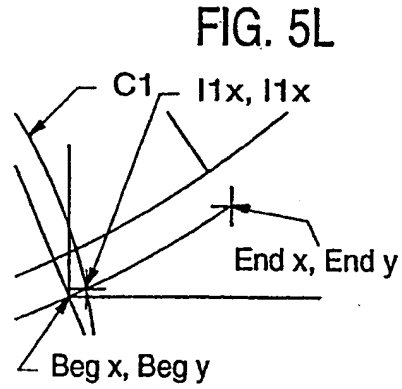
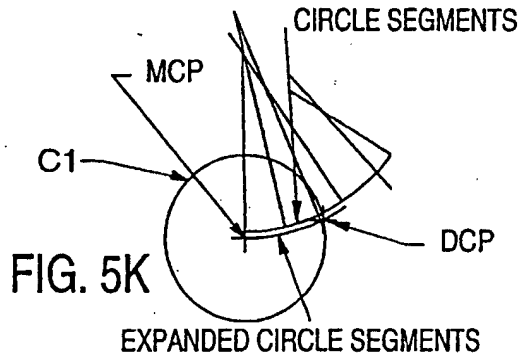


Spline Seg. No. 6
Circle Seg. Nos. 11 and 12

FIG. 5I

FIG. 5J

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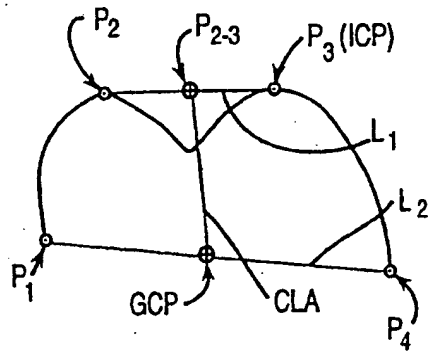


FIG. 6A

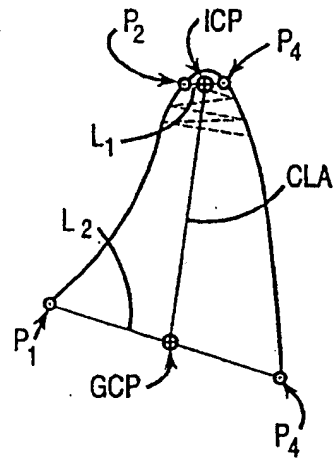


FIG. 6B

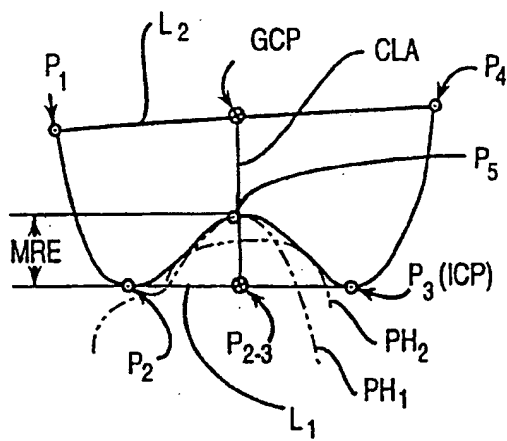


FIG. 6C

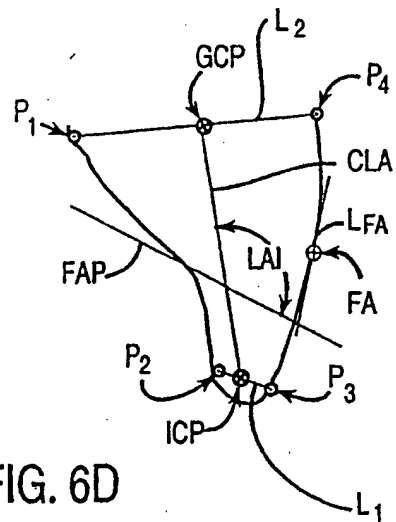


FIG. 6D

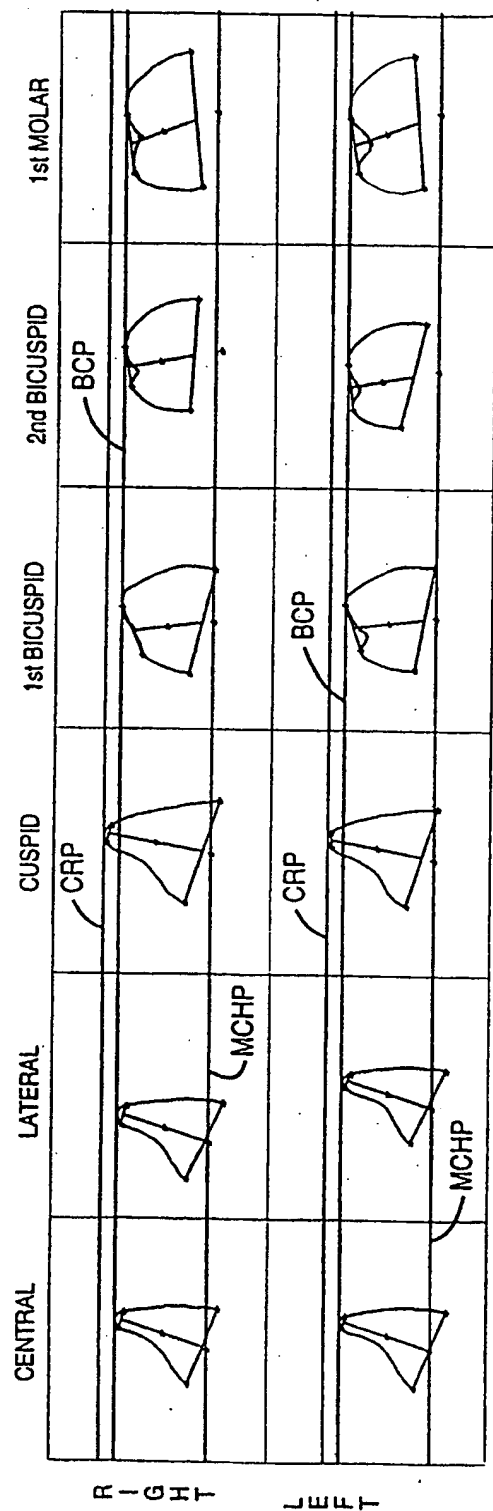


FIG. 6F

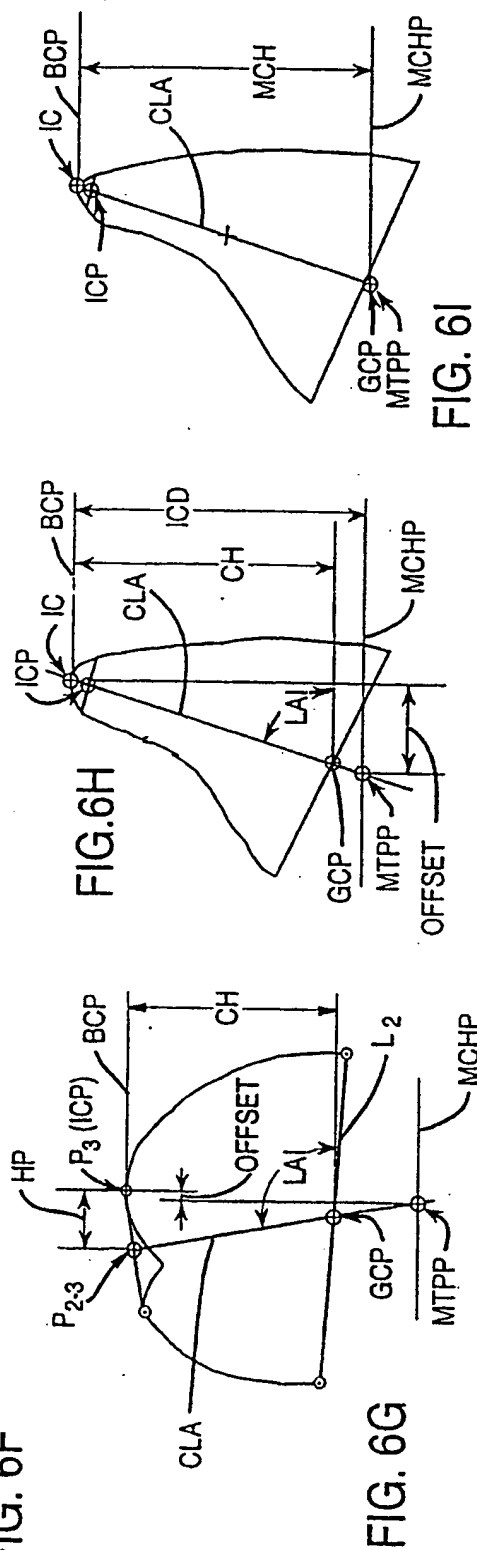


FIG. 6G

FIG. 6H

FIG. 61

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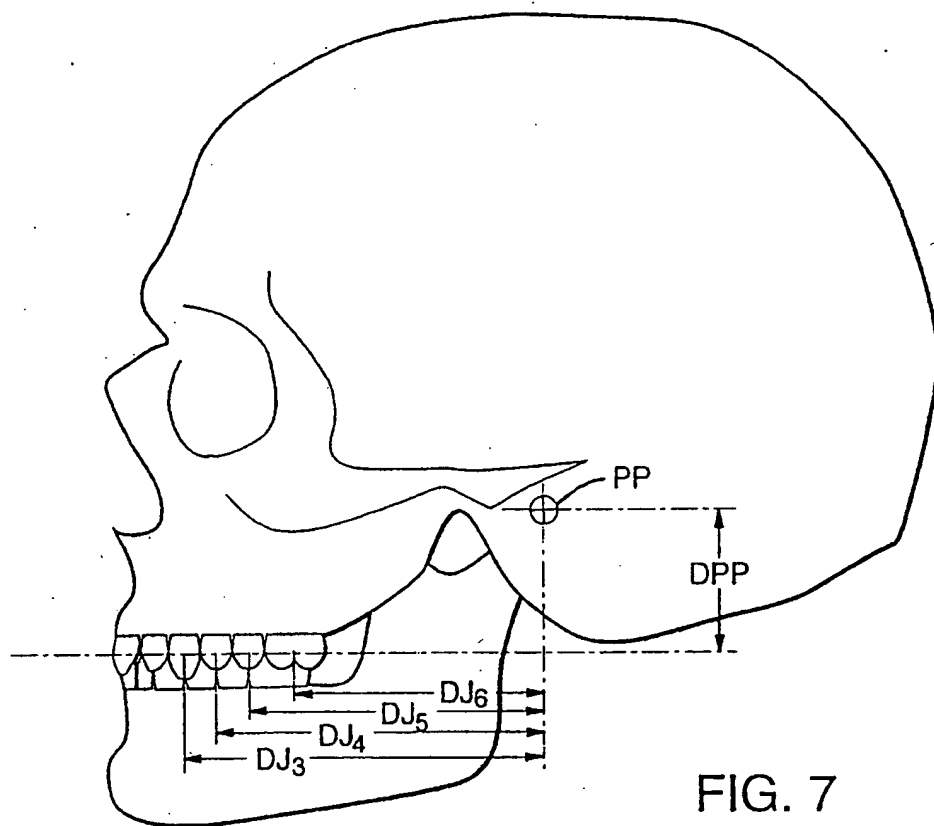


FIG. 7

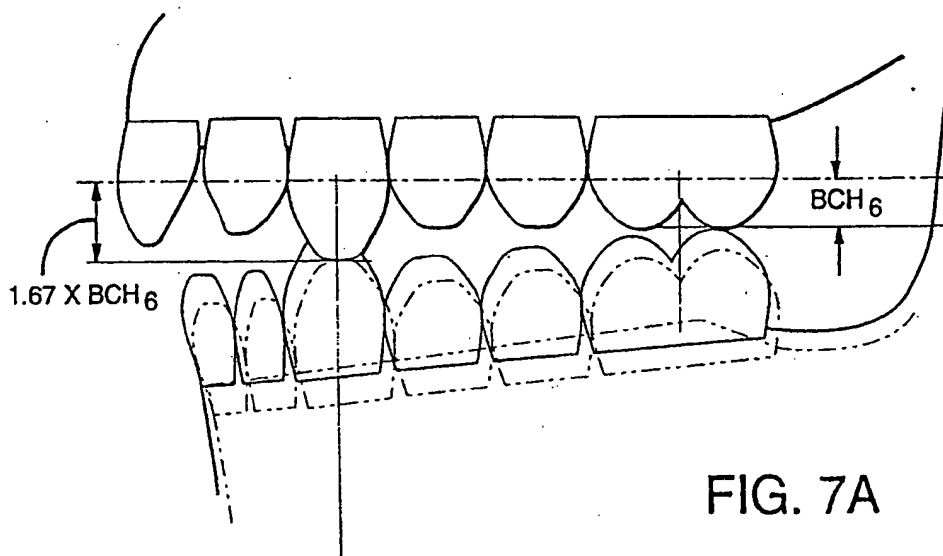
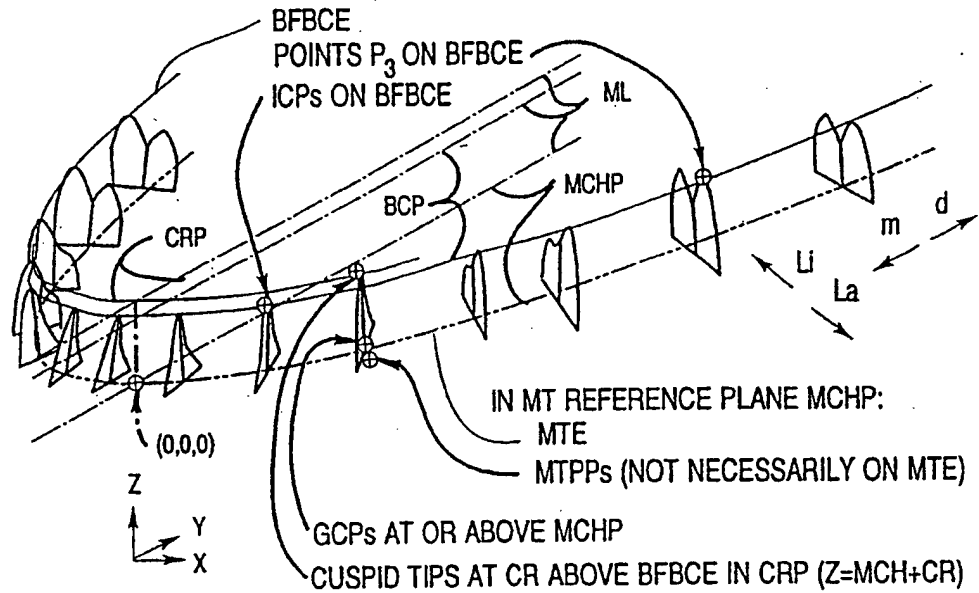


FIG. 7A

IN PLANE OF OCCLUSION BCP ($Z=MCH$):

PROFILE PLANE COORDINATES:

Y COORDINATE = Z IN ARCH PLANES

X COORDINATE = LABIAL (La) DIRECTION IN ARCH PLANES

FIG. 7C

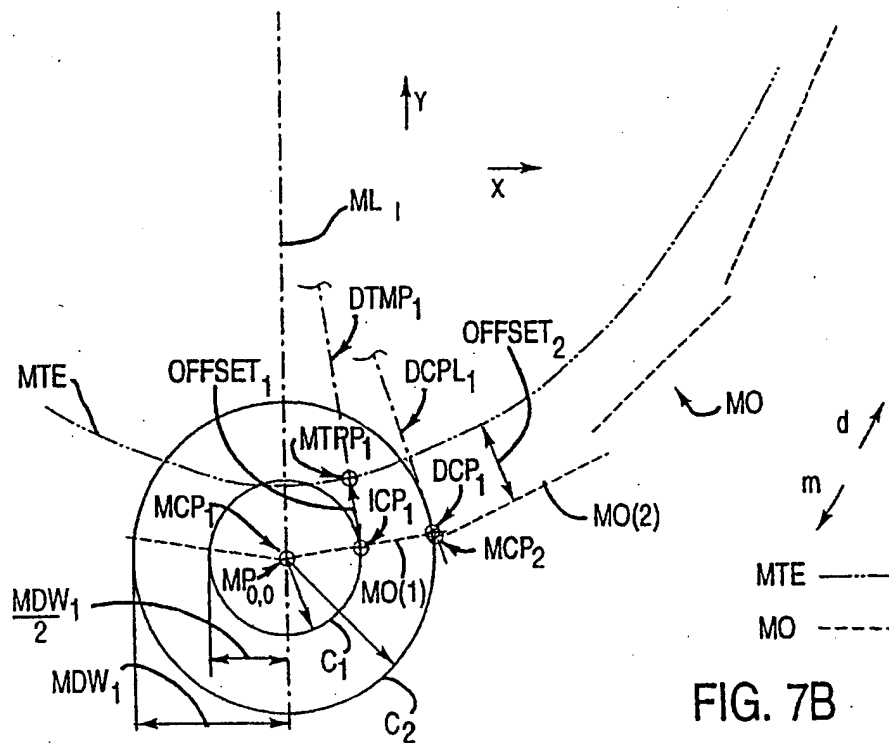
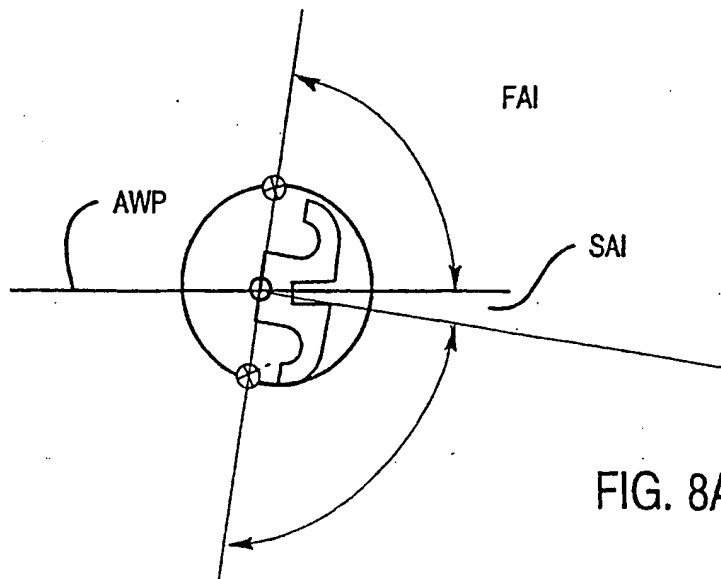
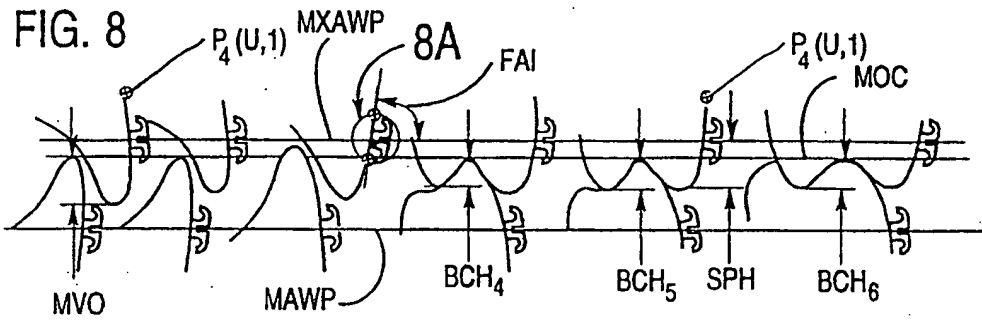
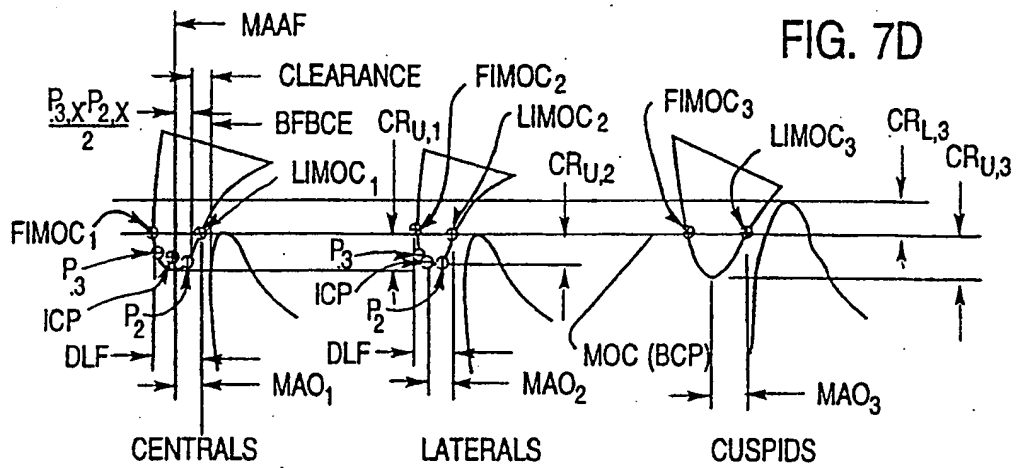


FIG. 7B

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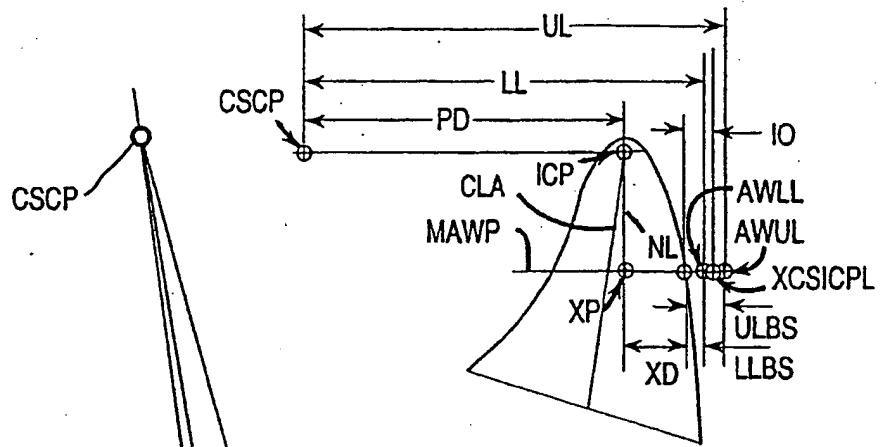


FIG. 8C

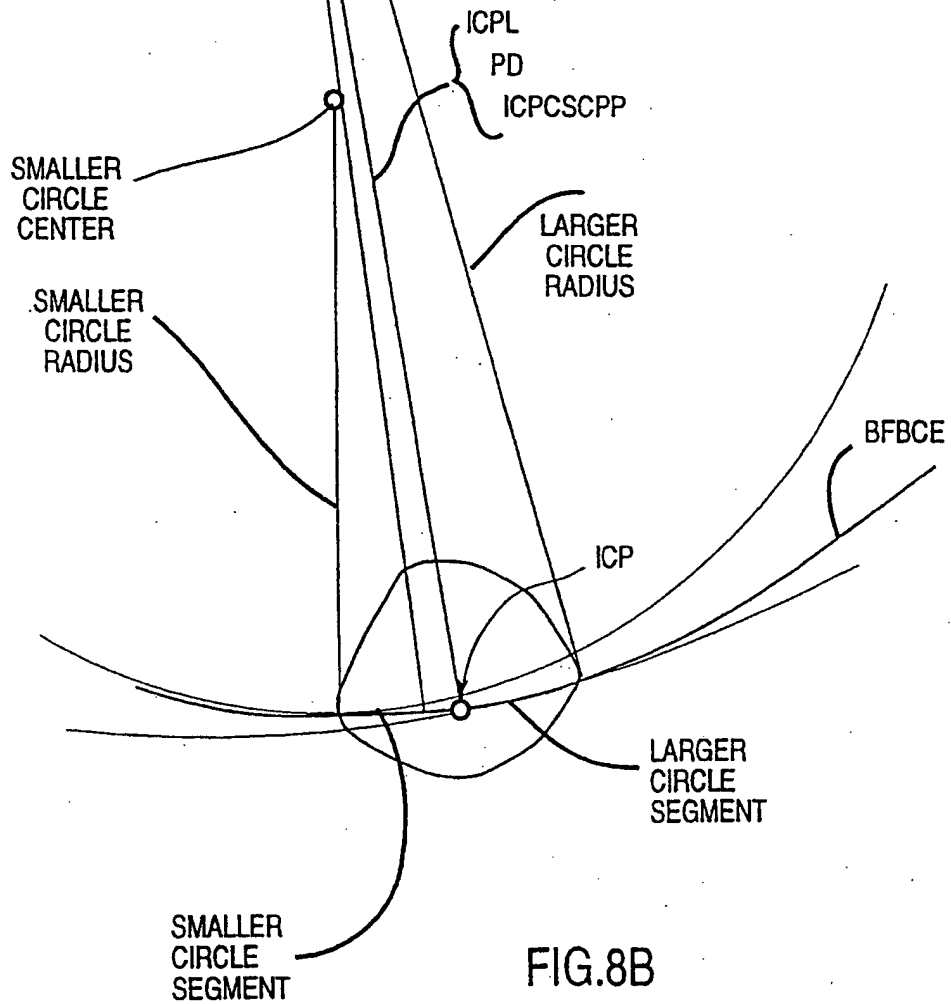


FIG. 8B

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FIG. 8D

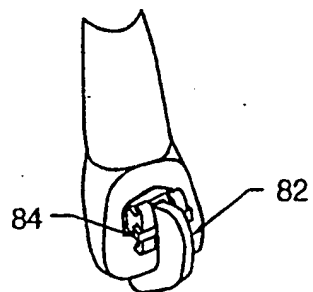


FIG. 8E

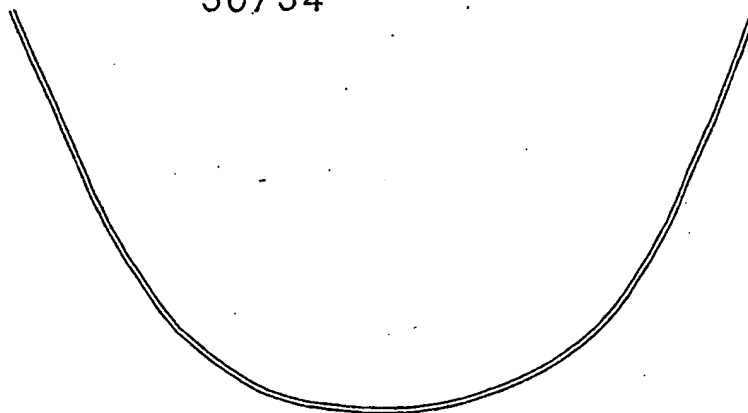
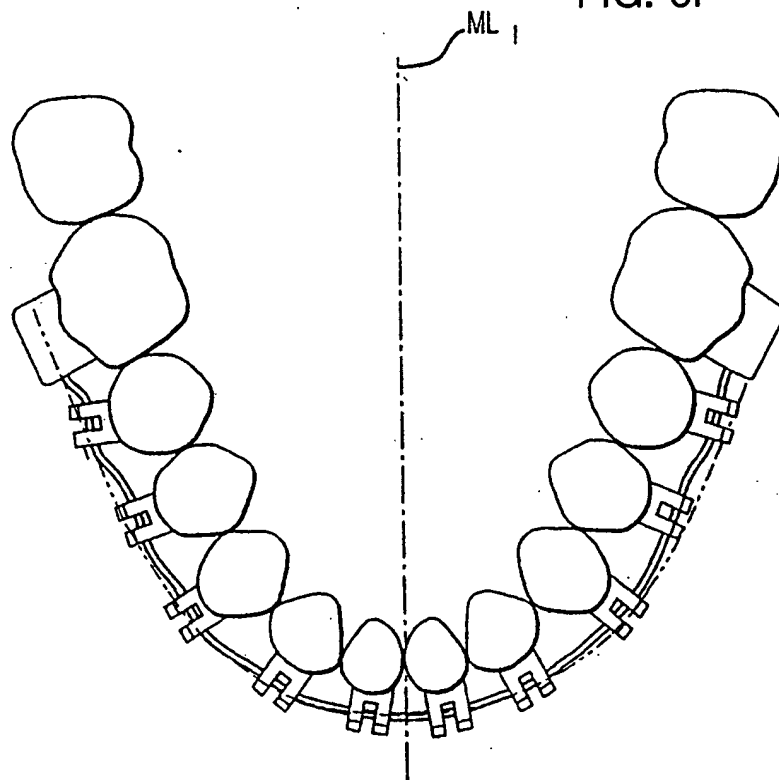


FIG. 8F



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FIG. 8I

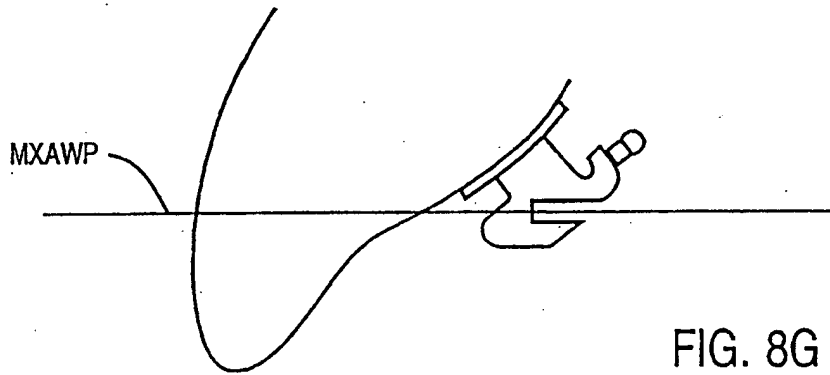
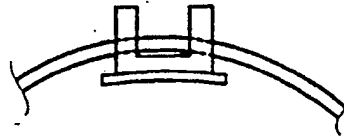
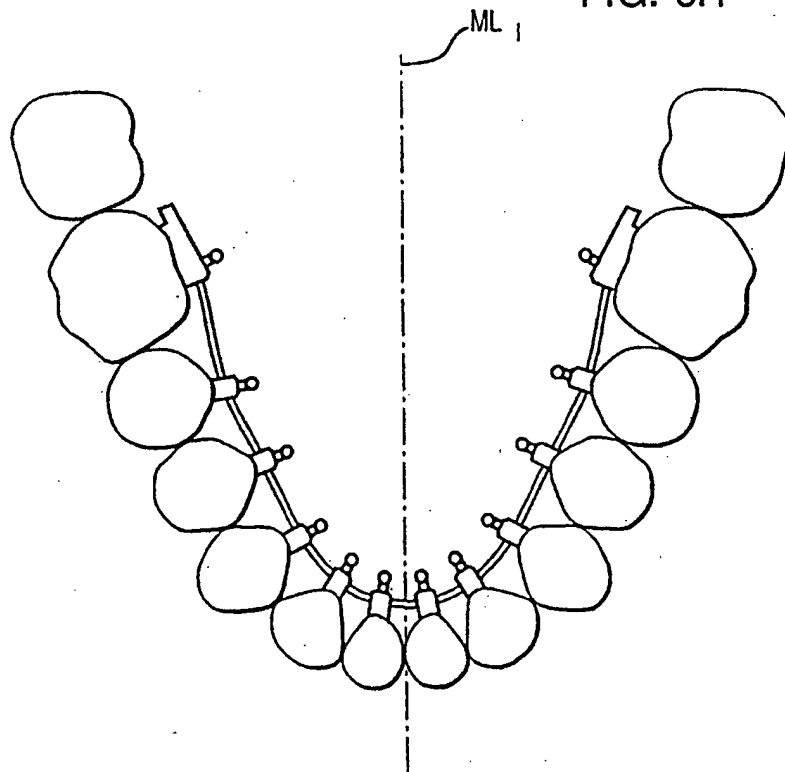
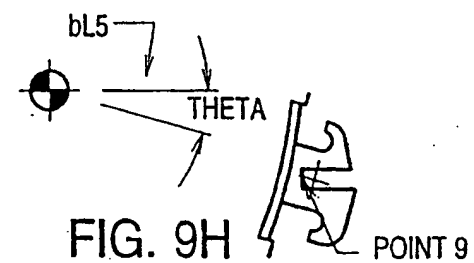
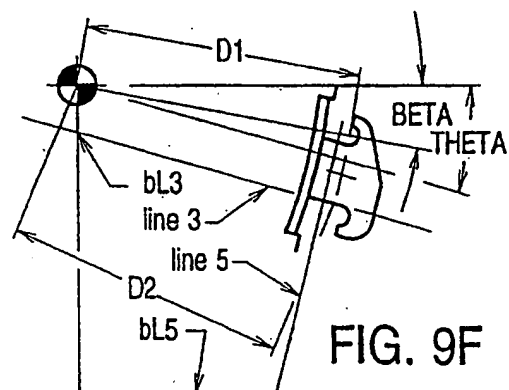
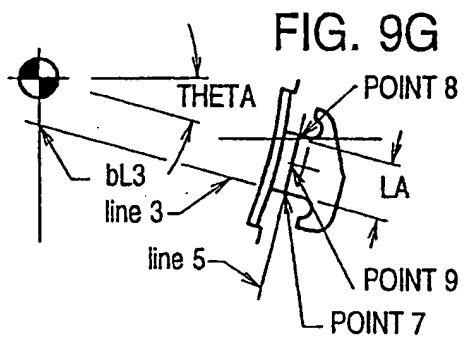
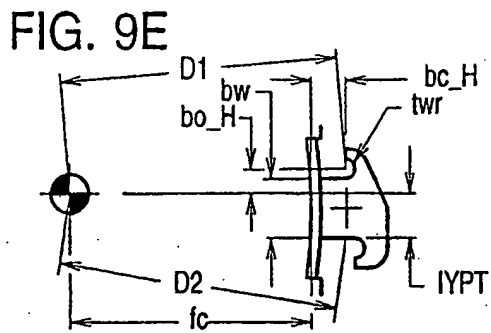
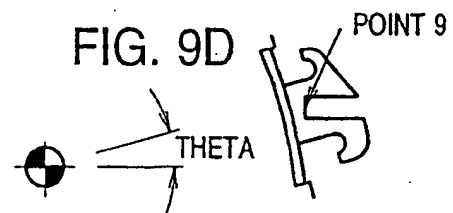
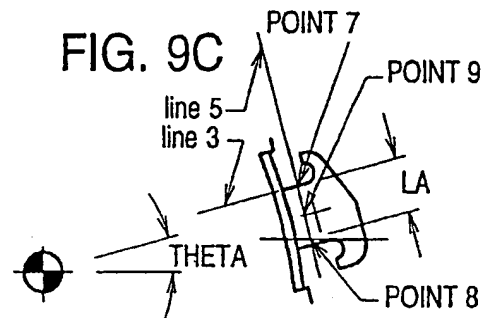
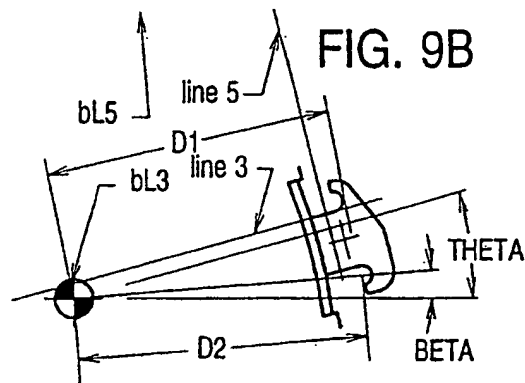
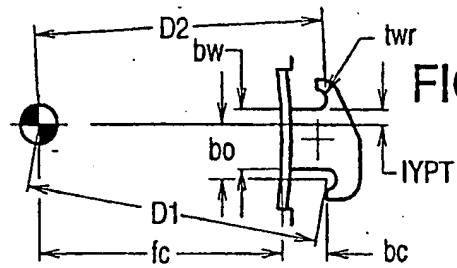
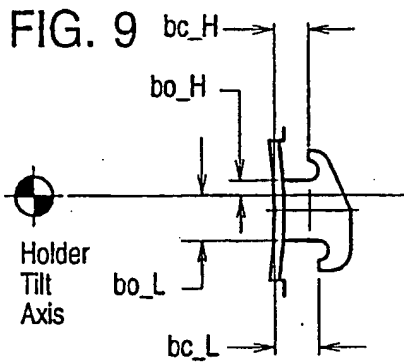


FIG. 8G

FIG. 8H



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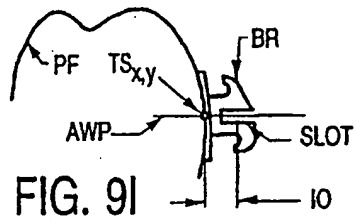


FIG. 9I

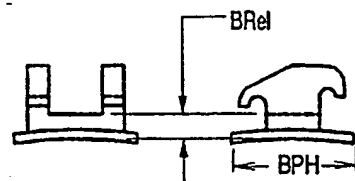


FIG. 9J

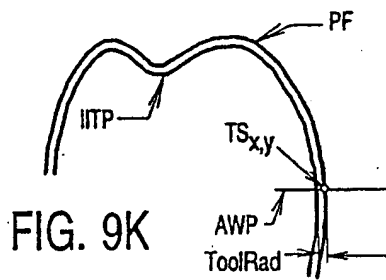


FIG. 9K

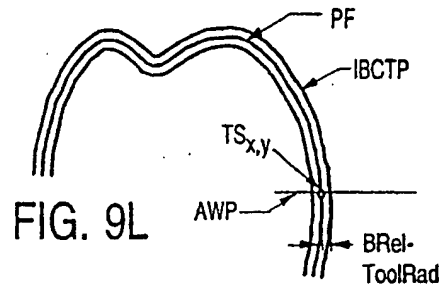


FIG. 9L

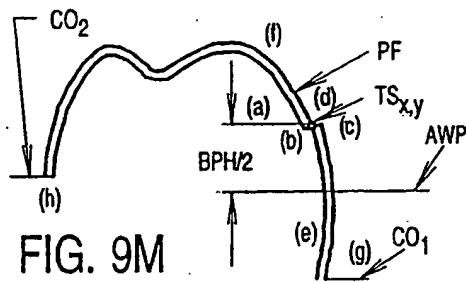


FIG. 9M

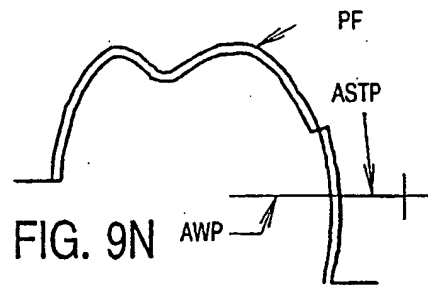


FIG. 9N

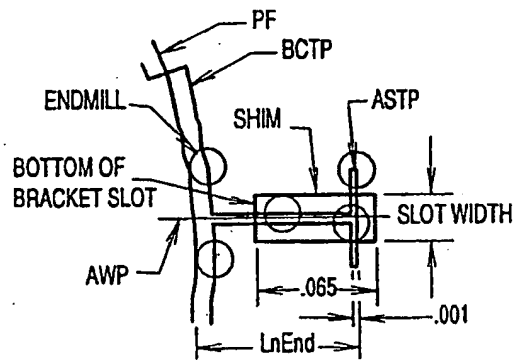


FIG. 9O

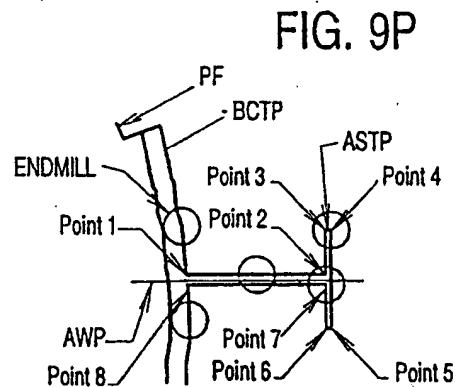
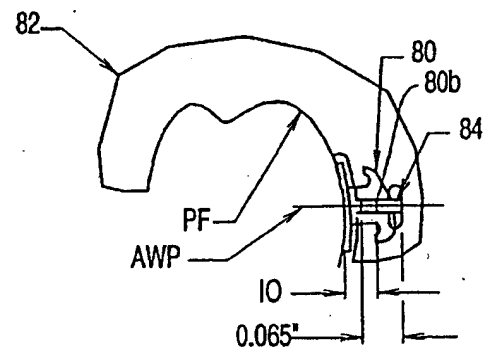
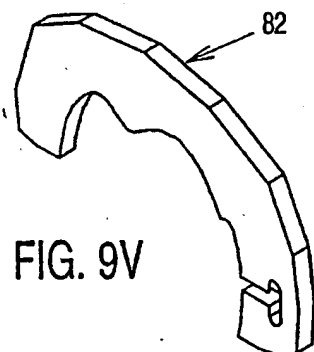
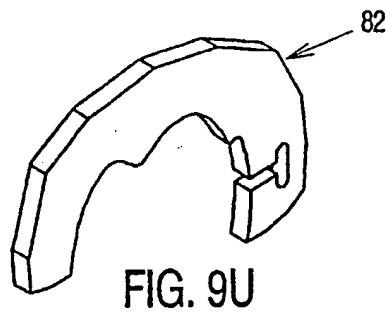
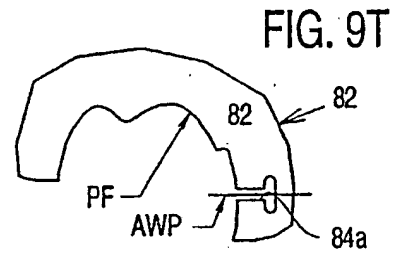
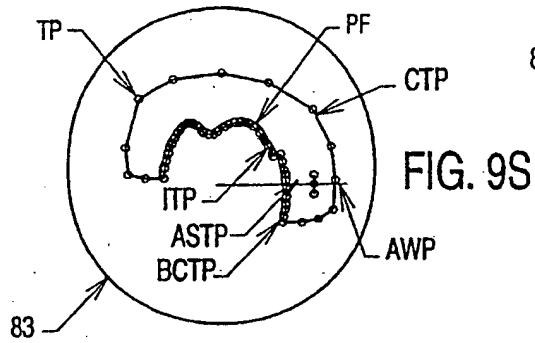
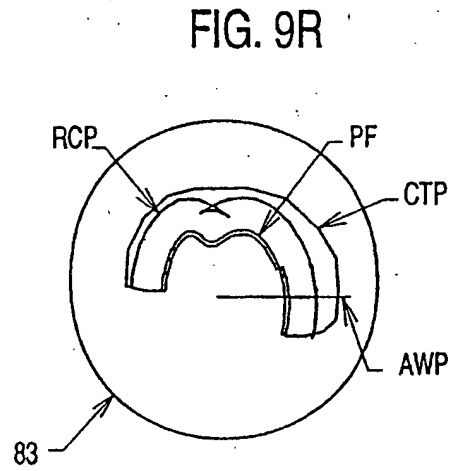
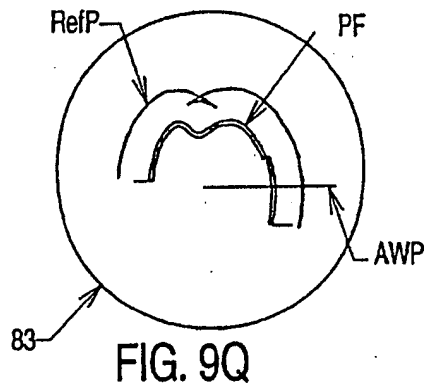


FIG. 9P



INTERNATIONAL SEARCH REPORT

Inter. Application No.

PCT/US 93/10858

A. CLASSIFICATION OF SUBJECT MATTER IPC 5 A61C7/00 A61C13/00		
According to International Patent Classification (IPC) or to both national classification and IPC		
B. FIELDS SEARCHED Minimum documentation searched (classification system followed by classification symbols) IPC 5 A61C		
Documentation searched other than minimum documentation to the extent that such documents are included in the fields searched		
Electronic data base consulted during the international search (name of data base and, where practical, search terms used)		
C. DOCUMENTS CONSIDERED TO BE RELEVANT		
Category*	Citation of document, with indication, where appropriate, of the relevant passages	Relevant to claim No.
A	EP,A,0 502 227 (ANDREIKO) 9 September 1992 see the whole document ---	1,2,6,9, 11,18, 23,29, 30,33
A	WO,A,90 08512 (DOLPHIN IMAGING SYSTEMS) 9 August 1990 see the whole document -----	1
<input type="checkbox"/> Further documents are listed in the continuation of box C. <input checked="" type="checkbox"/> Patent family members are listed in annex.		
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Date of the actual completion of the international search 22 February 1994		Date of mailing of the international search report 04. 03.94
Name and mailing address of the ISA European Patent Office, P.B. 5818 Patentlaan 2 NL - 2280 HV Rijswijk Tel. (+ 31-70) 340-2040, Tx. 31 651 epo nl, Fax (+ 31-70) 340-3016		Authorized officer Vanrunxt, J

INTERNATIONAL SEARCH REPORT

information on patent family members

International Application No

PCT/US 93/10858

Patent document cited in search report	Publication date	Patent family member(s)	Publication date
EP-A-0502227	09-09-92	NONE	
WO-A-9008512	09-08-90	US-A- 5011405 AU-A- 5097090	30-04-91 24-08-90

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